

Model Predictive Control of a Sewer System

June 14, 2018

Group 1030

Jacob Naundrup Pedersen

Thomas Holm Pilgaard

Department of Electronic Systems

Aalborg University

Denmark



AALBORG UNIVERSITY
DENMARK



Agenda

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

Implementation

Kontrol

Results

Discussion/Conclusion

Overview

Jacob Naundrup Pedersen

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

2

- ▶ Implementation
- ▶ Kontrol
- ▶ Results
- ▶ Discussion
- ▶ Conclusion

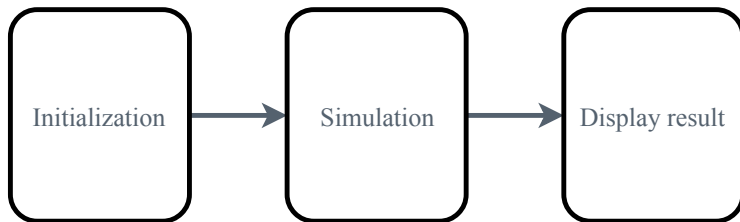


Figure: Chosen structure of simulation environment.

1. Pipe

- ▶ Length [m]
- ▶ Sections (Number of sections the pipe should be split in to)
- ▶ S_b (Slope) [‰]
- ▶ $\Delta x = \text{Length} / \text{Sections}$ [m]
- ▶ Diameter [meter]
- ▶ Theta (parameter used in Preissmann scheme)
- ▶ $Q_f [\text{m}^3/\text{s}]$
- ▶ Side/lateral inflow present
- ▶ Section location in data

2. Tank

- ▶ Size [m^3]
- ▶ Height [m]
- ▶ Area = Size / Height [m^2]
- ▶ Maximum outflow [m^3/s]
- ▶ Section location in data

Table: List of parameters for pipe and tank.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

5

Fields	length	sections	Dx	Sb	d	Theta	Qf	side_inflow	data_location
1	700	35	20	0.0030	0.9000	0.6500	0.9730	0	1
2	303	15	20.2000	0.0030	0.9000	0.6500	0.9730	0	3
3	27	2	13.5000	0.0030	1	0.6500	1.2843	1	4
4	155	8	19.3750	0.0041	1	0.6500	1.5014	0	5
5	295	14	21.0714	0.0122	0.8000	0.6500	1.4386	0	6
6	318	15	21.2000	0.0053	0.9000	0.6500	1.2932	1	7
7	110	5	22	0.0036	0.9000	0.6500	1.0658	1	8
8	38	2	19	0.0024	1	0.6500	1.1487	1	9
9	665	30	22.1667	0.0030	1	0.6500	1.2843	1	10
10	155	7	22.1429	8.0000e-04	1	0.6500	0.6632	0	11
11	955	47	20.3191	0.0029	1.2000	0.6500	2.0415	1	12
12	304	15	20.2667	0.0030	1.2000	0.6500	2.0764	0	13
13	116	5	23.2000	0.0021	1.2000	0.6500	1.7373	1	14
14	283	12	23.5833	0.0017	1.4000	0.6500	2.3463	1	15
15	31	2	15.5000	0.0019	1.4000	0.6500	2.4805	1	16
16	125	6	20.8333	0.0021	1.6000	0.6500	3.7075	0	17
17	94	4	23.5000	0.0013	1.5000	0.6500	2.4609	0	18
18	360	18	20	0.0046	1.6000	0.6500	5.4872	1	19
19	736	38	19.3684	0.0012	1.6000	0.6500	2.8026	0	20

Figure: Setup in MATLAB of pipe specification of the main line in Fredericia.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

6

Field ▲	Value
size	90
height	10
area	9
Q_out_max	0.9730
data_location	2

Figure: Setup in MATLAB of tank specifications.




Fields	 type	 component	 sections
1	'Pipe'	1	35
2	'Tank'	1	1
3	'Pipe'	18	245
4	'Total'	20	281

Figure: Display of structure showing system setup information in MATLAB.

Agenda

Group 1030

Implementation

8

Kontrol

Results

Discussion/Conclusion

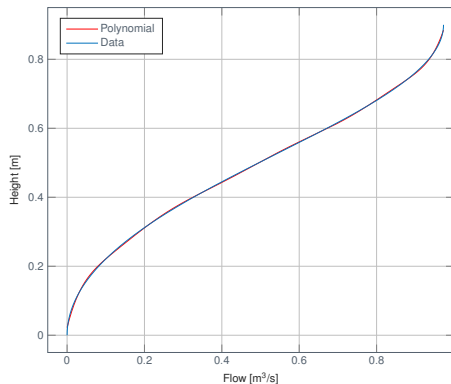


Figure: Comparison between data obtained by equation ?? and the same data curve fitted to a ninth order polynomial.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

9

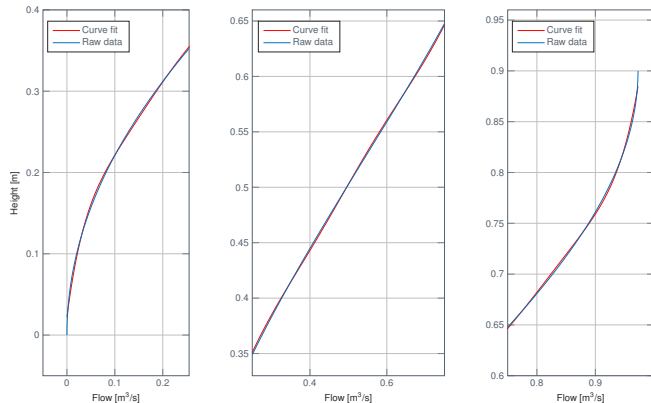


Figure: Comparison between data obtained by equation ?? and the same data curve fitted to a ninth order polynomial.

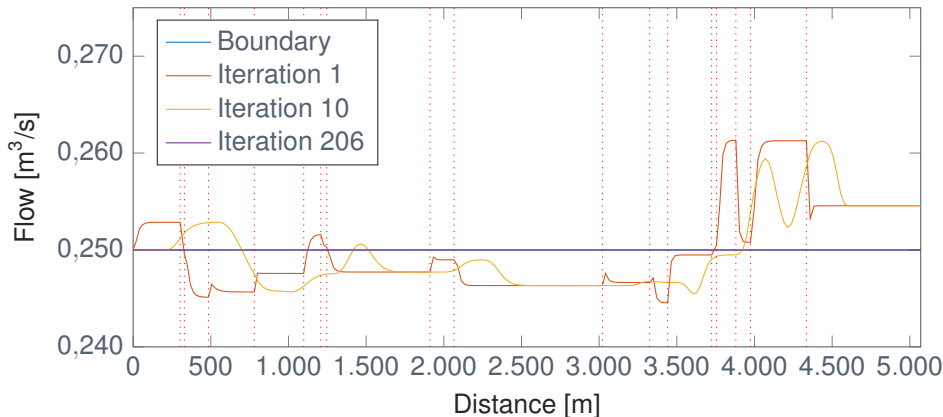


Figure: Height and flow of pipe setup from part of Fredericia where boundary conditions is found by fitted polynomial. Various amount of iterations, with constant flow input of $0,25 \text{ m}^3/\text{s}$, is performed. The dotted line indicates pipe intersections.

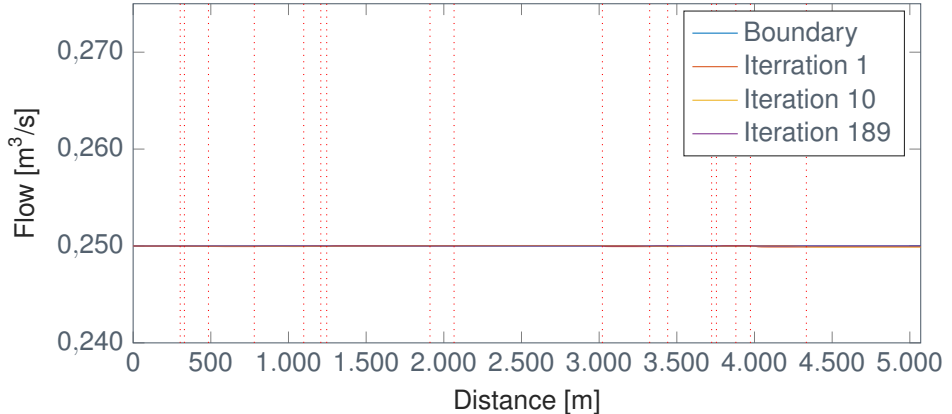


Figure: Height and flow of pipe setup from part of Fredericia where boundary conditions is found by lookup table. Various amount of iterations, with constant flow input of $0,25 \text{ m}^3/\text{s}$, is performed. The dotted line indicates pipe intersections.



Implementation

Simulation

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

12

► Preissmann scheme

Implementation Display

Agenda

Group 1030

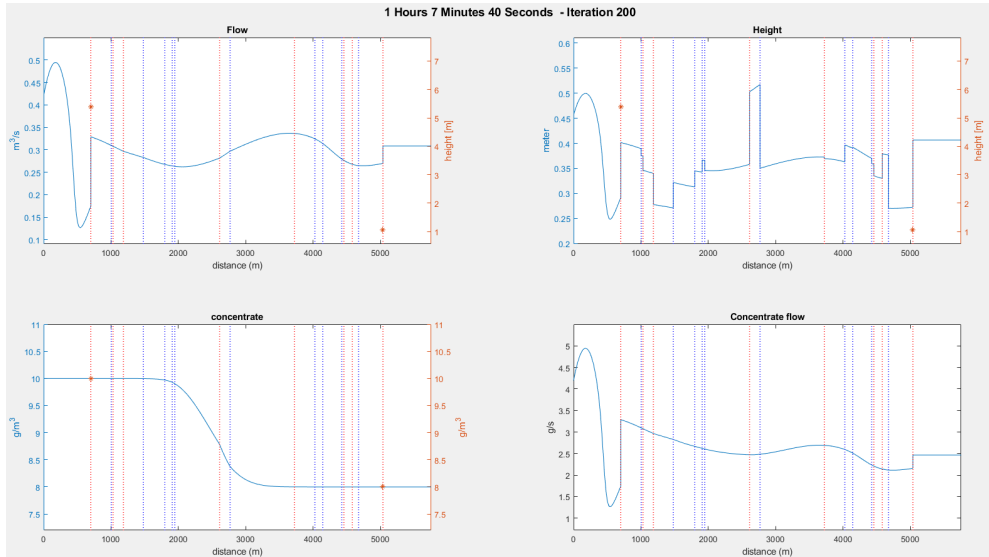
Implementation

Kontrol

Results

Discussion/Conclusion

13



Figure

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

14

- Linearisering af ulinear model
- Opstilles på state space form

$$\frac{\partial A(x, t)}{\partial t} + \frac{\partial Q(x, t)}{\partial x} = 0 \quad (1)$$

$$\frac{\partial A(h)}{\partial h} \frac{\partial h(x, t)}{\partial t} + \frac{\partial Q(h)}{\partial h} \frac{\partial h(x, t)}{\partial x} = 0 \quad (2)$$

► Priessmann scheme

$$\begin{aligned} & \frac{\partial A(h)}{\partial h} \left(\frac{1}{2} \frac{h_{j+1}^{i+1} - h_{j+1}^i}{\Delta t} + \frac{1}{2} \frac{h_j^{i+1} - h_j^i}{\Delta t} \right) + \\ & \frac{\partial Q(h)}{\partial h} \left(\theta \frac{h_{j+1}^{i+1} - h_j^{i+1}}{\Delta x} + (1 - \theta) \frac{h_{j+1}^i - h_j^i}{\Delta x} \right) = 0 \end{aligned} \quad (3)$$

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

16

$$\underbrace{\begin{bmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & b_1 & 0 & \cdots & 0 \\ 0 & a_1 & b_2 & \cdots & \vdots \\ \vdots & \vdots & \ddots & \ddots & 0 \\ 0 & 0 & 0 & a_{m-1} & b_m \end{bmatrix}}_{\xi} \underbrace{\begin{bmatrix} h_0^{i+1} \\ h_1^{i+1} \\ h_2^{i+1} \\ \vdots \\ h_m^{i+1} \end{bmatrix}}_{x(k+1)} = \underbrace{\begin{bmatrix} 0 & 0 & 0 & \cdots & 0 \\ c_0 & d_1 & 0 & \cdots & 0 \\ 0 & c_1 & d_2 & \cdots & 0 \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & 0 & c_{m-1} & d_m \end{bmatrix}}_A \underbrace{\begin{bmatrix} h_0^i \\ h_1^i \\ h_2^i \\ \vdots \\ h_m^i \end{bmatrix}}_{x(k)} + \underbrace{\begin{bmatrix} 1 \\ -a_0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}}_B h_0^{i+1} + \underbrace{\begin{bmatrix} \frac{dh}{dQ} \\ 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}}_{B_d} d_0^{i+1} \quad (4)$$

$$\underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & b_{1,1} & 0 & 0 & 0 & 0 & 0 \\ 0 & a_{1,1} & b_{1,2} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & a_{2,1} & b_{2,2} & 0 \\ 0 & 0 & 0 & 0 & 0 & a_{2,2} & b_{2,3} \end{bmatrix}}_{\xi} \underbrace{\begin{bmatrix} h_{1,0}^{i+1} \\ h_{1,1}^{i+1} \\ h_{1,2}^{i+1} \\ h_{tank}^{i+1} \\ h_{2,0}^{i+1} \\ h_{2,1}^{i+1} \\ h_{2,2}^{i+1} \end{bmatrix}}_{x(k+1)} = \underbrace{\begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ c_{1,0} & d_{1,1} & 0 & 0 & 0 & 0 & 0 \\ 0 & c_{1,1} & d_{1,2} & 0 & 0 & 0 & 0 \\ 0 & 0 & e & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & c_{2,0} & d_{2,1} & 0 \\ 0 & 0 & 0 & 0 & 0 & c_{2,1} & d_{2,2} \end{bmatrix}}_A \underbrace{\begin{bmatrix} h_{1,0}^i \\ h_{1,1}^i \\ h_{1,2}^i \\ h_{tank}^i \\ h_{2,0}^i \\ h_{2,1}^i \\ h_{2,2}^i \end{bmatrix}}_{x(k)} + \underbrace{\begin{bmatrix} 1 & 0 \\ -a_0 & 0 \\ 0 & 0 \\ 0 & -f \\ 0 & g \\ 0 & 0 \\ 0 & 0 \end{bmatrix}}_B \begin{bmatrix} h_0^{i+1} \\ u_{tank} \end{bmatrix} \quad (5)$$

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

18

► Sinus input

Type	Components	Sections
Pipe	1	35
Tank	1	1
Pipe	18	227
Total	20	263

Table: System setup.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

19

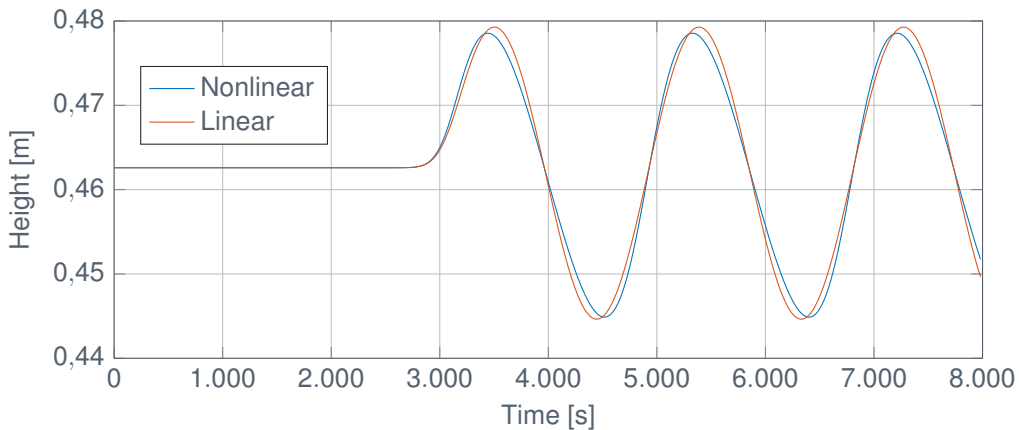


Figure: Comparison of the nonlinear and linear model at the last pipe in the setup.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

20

- ▶ Cost function
 - ▶ Begrænset til minimiere af output
- ▶ Constraints
 - ▶ Højde
 - ▶ Kontrol input
- ▶ Linear model

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

21

- ▶ Bestemmelse af Prediction horizon
 - ▶ Flow profiler
 - ▶ Industri
- ▶ Begrænsning af Prediction horizon

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

22

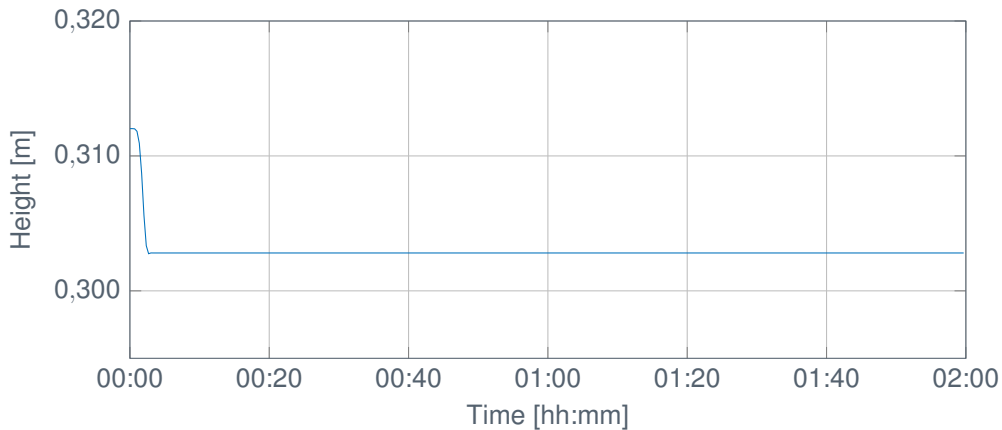


Figure: Output of the last pipe.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

23

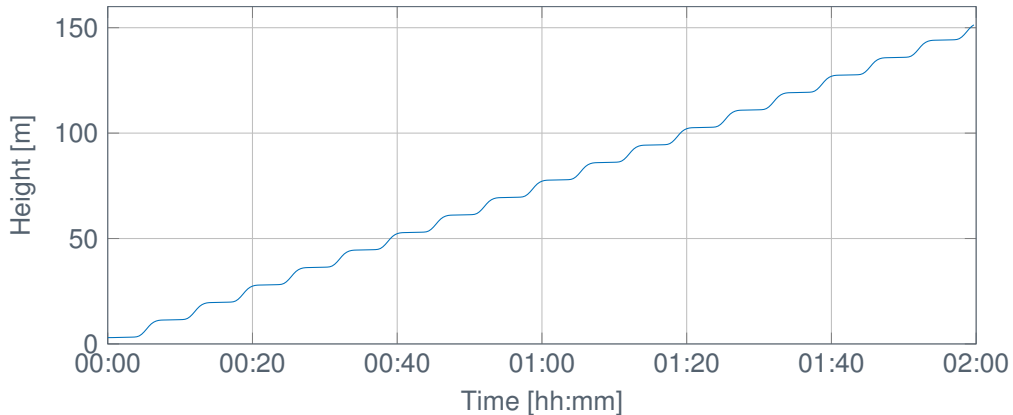


Figure: Height in the tank.

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

24

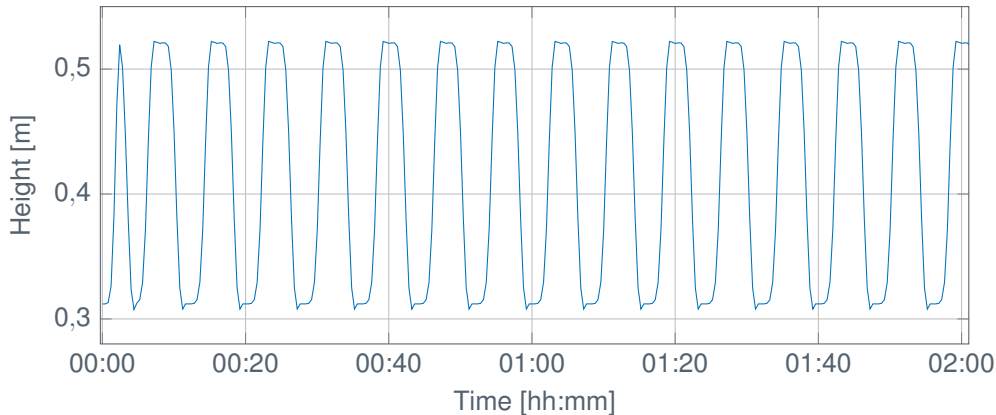


Figure: Output of the last pipe in the second simulation run.

Results

First test

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

25

- System setup
- Flow profiles

Type	Component	Sections
Pipe	1	35
Tank	1	1
Pipe	17	207
Tank	1	1
Pipe	1	38
Total	21	282

Table: System setup.

31

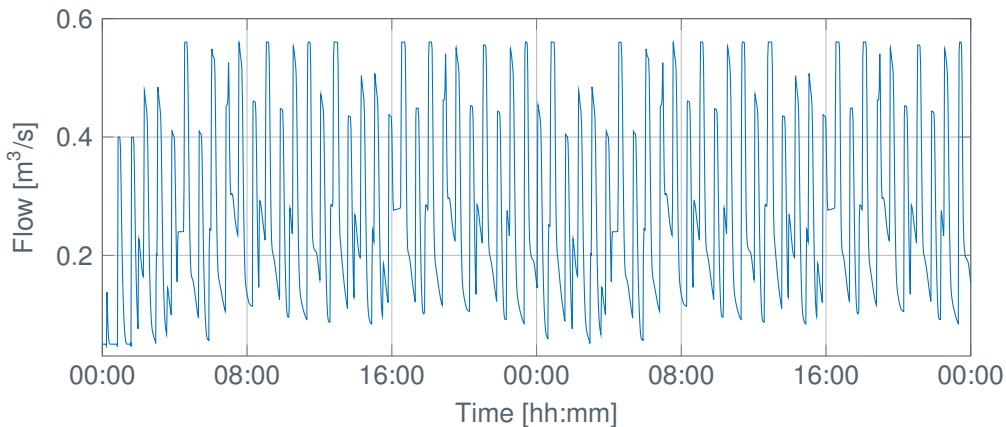


Figure: Output of the last pipe into the WWTP.

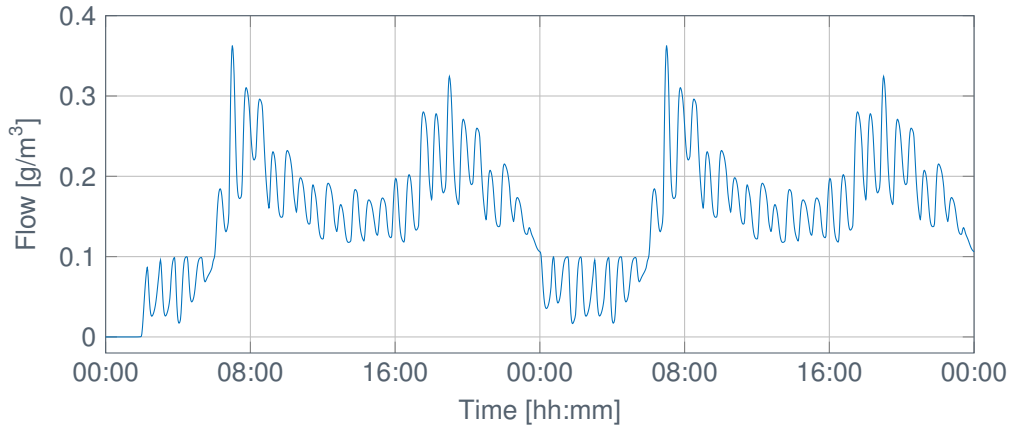


Figure: Simulation of COD output of the last pipe into the WWTP.



Results

Second test

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

28

- ▶ Over dimensioneret tank
- ▶ Konstant output af tank

31

Results

Second test

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

29

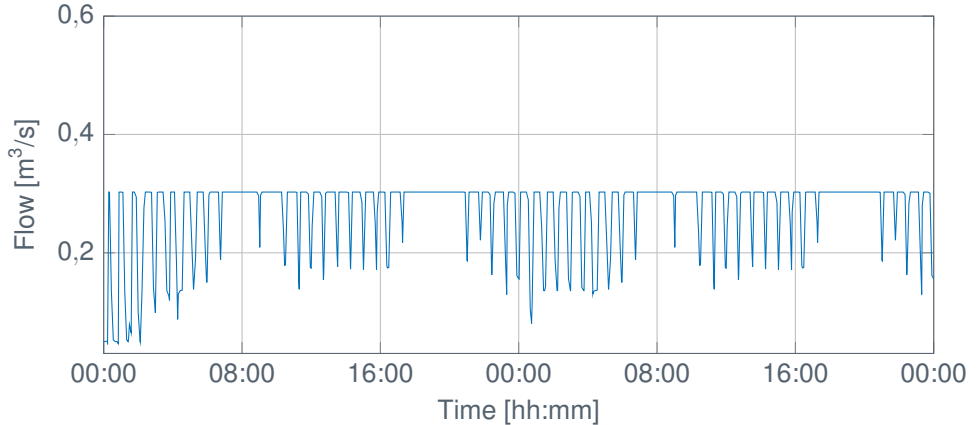


Figure: Output of the last pipe in to the WWTP, where a tank has been placed in front to reduce variation in flow into WWTP.



Discussion

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

30

- ▶ Courant's number
- ▶ Model reduction

31



Conclusion

Agenda

Group 1030

Implementation

Kontrol

Results

Discussion/Conclusion

31

- ▶ Simulation
- ▶ MPC