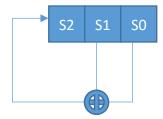
1. LFSR

- a. The degree of the key stream generator is 3.
- b. The initialization vector is 0010111.
- c. The feedback coefficients are (0,1,1).



d. The key is 0010111001011100101111. We don't use part of the plaintext as the key because if you know even a very small amount of the plaintext you could possibly get the entire key and message back with little effort.

2. Problem 2.11

- a. The initialization vector is 111111.
- b. The feedback coefficients are (0,0,0,0,1,1).
- c. The program to find the whole sequence and plaintext, 2_11.py, is below:

```
3. #CT observed J5A0EDJ2B
4. from collections import deque
5. #from bitarray import bitarray
6.
7. init_vec = [1, 1, 1, 1, 1, 1]
8. ciphertext = ['J', 5, 'A', 0, 'E', 'D', 'J', 2, 'B']
9. key = []
10.
11. cipherbin = []
12.
13. #GENERATES KEY
14. key.insert(0,'1')
15. for in range (0, 44):
     a = int(init_vec[4]) ^ int(init_vec[5])
16.
17.
       init vec.insert(0,a)
      init_vec.pop()
18.
19.
20.
      key.append(str(init vec[5]))
21.
22.
23.
24. #GENERATE BITSTREAM FROM CIPHERTEXT
25. for j in range(0,9):
      if type(ciphertext[j]) == str:
27.
           cipherbin.append(str(format((ord(ciphertext[j])-ord('A')),'05b')))
28.
       else:
29.
           cipherbin.append(str(format((ord(str(ciphertext[j])) - 22),'05b')))
30.
31. #print "The cipher " +'{}{}{}{}{}{}.format(*cipherbin)
32.
33. #XOR THE CIPHER AND THE KEY
34.
35. a = "0b" + ".join(key)
36. b = "0b"+''.join(cipherbin)
37.
```

```
39.
   40. plainbin = str(bin(int(a.strip(""),2) ^ int(b.strip(""),2)))
   41.
   43. print "Key
                   44. {}{}{}{}{}{}{}{}{}{}{}{}*.format(*key)
   45. print "Cipher 0b"+'{}{}{}{}{}{}'.format(*cipherbin)
   46. print "Plaintext " +plainbin
   47.
   48.
   49. u0 = chr(int(("0b"+''.join(plainbin[2:7])).strip(""),2)+ord("A"))
   50. u1 = chr(int(("0b"+''.join(plainbin[7:12])).strip(""),2) + 65)
   51. u2 = chr(int(("0b"+''.join(plainbin[12:17])).strip(""),2)+ord("A"))
   52. u3 = chr(int(("0b"+''.join(plainbin[17:22])).strip(""),2) + 65)
   53. u4 = chr(int(("0b"+''.join(plainbin[22:27])).strip(""),2)+ord("A"))
   54. u5 = chr(int(("0b"+''.join(plainbin[27:32])).strip(""),2)+ord("A"))
   55. u6 = chr(int(("0b"+''.join(plainbin[32:37])).strip(""),2)+ord("A"))
   56. u7 = chr(int(("0b"+''.join(plainbin[37:42])).strip(""),2) + 65)
   57. u8 = chr(int(("0b"+''.join(plainbin[42:47])).strip(""),2)+ord("A"))
print u0,u1,u2,u3,u4,u5,u6,u7,u8
Plaintext
WPIWOMBAT
```

- d. Australia.
- e. We performed a known-plaintext attack.
- 3. The implementation of DES S-box S2 and the SAC algorithm is shown below in SAC.py:

```
1 def S2(x): #Implementation of S Box 2, returns value from row
       row0 = [15, 1, 8, 14, 6, 11, 3, 4, 9, 7, 2, 13, 12, 0, 5, 10]
       row1 = [3, 13, 4, 7, 15, 2, 8, 14, 12, 0, 1, 10, 6, 9, 11, 5]
       row2 = [0,14,7,11,10,4,13,1,5,8,12,6,9,3,2,15]
6
       row3 = [13, 8, 10, 1, 3, 15, 4, 2, 11, 6, 7, 12, 0, 5, 14, 9]
      x = '0b' + bin(x^2**6)[3:]
9
      if x[2] == "0":
           if x[7] == "0":
10
               y = int(x[3:7], 2)
11
                s2 = row0[y]
           if x[7] == "1":
13
               y = int(x[3:7], 2)
14
15
                s2 = row1[y]
      if x[2] == "1":
17
          if x[7] == "0":
18
                y = int(x[3:7], 2)
19
20
                s2 = row2[y]
           if x[7] == "1":
21
               y = int(x[3:7],2)
22
                s2 = row3[v]
23
2.4
25
      return s2;
28
29 def SAC(x):
    Sum = 0
30
31
      output = [0,0,0,0,0,0]
32
33
      for i in range(0,6):
34
        output[i] = S2(x) ^ S2(x^2**i)
35
      return output;
36
37 \text{ sum} 0 = 0
38 \, \text{sum1} = 0
39 \, \text{sum} 2 = 0
40 \text{ sum} 3 = 0
41
42 for j in range(2**6):
    bit0 = 0; bit1 = 0; bit2 = 0; bit3 = 0
```

```
44
      arr = SAC(j)
     for i in range (0,6):
          bit0 += int(bin(arr[i]^(2**4))[6])
47
          bit1 += int(bin(arr[i]^(2**4))[5])
bit2 += int(bin(arr[i]^(2**4))[4])
48
49
           bit3 += int(bin(arr[i]^(2**4))[3])
51
     sum0 += (bit0 % 2)
      sum1 += (bit1 % 2)
sum2 += (bit2 % 2)
52
53
      sum3 += (bit3 % 2)
print sum0, sum1, sum2, sum3
```

This prints the sums of 32, 32, 36, and 32. Since each of these sums is greater than or equal to $2^5 = 32$, then the s-box passes the SAC.

4. Below is the code used to attempt to make an exhaustive key search of the provided plaintext and ciphertext. The code failed to find the key within the keyspace.

```
56 from Crypto.Cipher import DES
57 import codecs
58
59pt = "48656c6c6f212121"
60 ct = "d52bd481f21e25a1"
62 pt = pt.decode("hex")
63ct = ct.decode("hex")
65 iv = "00000000".decode("hex")
66 key = "000000000000000".decode("hex")
68 for x in range (4**8):
69 cipher = DES.new(key^x, DES.MODE ECB)
    msg = cipher.encrypt(pt)
70
71
     if msg == ct:
       break
```