### Problem Set 3

## Applied Stats/Quant Methods 1 Minh Trinh (Student ID:24350478)

Due: November 11, 2024

#### Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on GitHub.
- This problem set is due before 23:59 on Sunday November 11, 2024. No late assignments will be accepted.

In this problem set, you will run several regressions and create an add variable plot (see the lecture slides) in R using the incumbents\_subset.csv dataset. Include all of your code.

# Question 1

We are interested in knowing how the difference in campaign spending between incumbent and challenger affects the incumbent's vote share.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **difflog**.

We need to declare our assumptions:

- Each observation is independent
- Observations are randomly generated
- There is a linear relationship between mean of the dependent variable and the value of independent variable
- The error term is normally distributed with mean 0 and has constant variable for all value of independent variable

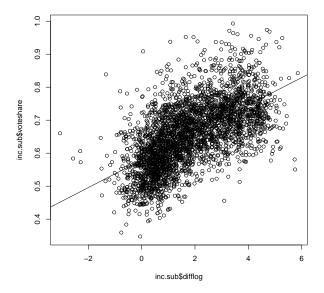
We first load the dataset into our environment and run regression with voteshare as outcome variable and difflog as the explanatory variable in R. We can then examine the regression coefficients using summary():

```
1 # read in data
2 inc.sub <- read.csv("https://raw.githubusercontent.com/ASDS-TCD/StatsI_
     Fall2024/main/datasets/incumbents_subset.csv")
4 #Q1
5 #regression between voteshare and difflog
6 model_q1 <- lm(voteshare ~ difflog, data=inc.sub)
7 summary (model_q1)
 Call:
 lm(formula = voteshare ~ difflog, data = inc.sub)
 Residuals:
      Min
                1Q
                     Median
                                   3Q
                                           Max
 -0.26832 -0.05345 -0.00377 0.04780 0.32749
 Coefficients:
             Estimate Std. Error t value Pr(>|t|)
 (Intercept) 0.579031
                        0.002251 257.19
                                            <2e-16 ***
 difflog
             0.041666
                        0.000968
                                   43.04
                                            <2e-16 ***
                 0 '*** 0.001 '** 0.01 '* 0.05 '. '0.1 ' 1
 Signif. codes:
 Residual standard error: 0.07867 on 3191 degrees of freedom
 Multiple R-squared: 0.3673, Adjusted R-squared: 0.3671
 F-statistic: 1853 on 1 and 3191 DF, p-value: < 2.2e-16
```

2. Make a scatterplot of the two variables and add the regression line. We draw the scatterplot and regression line in R:

```
plot(inc.sub$difflog,inc.sub$voteshare)
abline (model_q1)
```

Figure 1: Scatterplot between difference in campaign spending and incumbent's vote share with regression line.



3. Save the residuals of the model in a separate object.

The residual of the model can be obtained in the model object in R.

head(model\_q1\$residuals)

We will assign it to an object

- n model\_resid\_votes\_difflog <- model\_q1\$residuals</pre>
- 4. Write the prediction equation.

  General form for prediction equation is:

$$\hat{y} = \beta_0 + \beta_1 x$$

Based on the coefficients of the regression on section 1 we have the following prediction equation:

$$\widehat{\text{voteshare}} = 0.579031 + 0.041666 \times \text{difflog}$$

With *voteshare* as the predicted value for outcome variable and difflog as the explanatory variable

We are interested in knowing how the difference between incumbent and challenger's spending and the vote share of the presidential candidate of the incumbent's party are related.

1. Run a regression where the outcome variable is **presvote** and the explanatory variable is **difflog**.

We need to declare our assumptions:

- Each observation is independent
- Observations are randomly generated
- There is a linear relationship between mean of the dependent variable and the value of independent variable
- The error term is normally distributed with mean 0 and has constant variable for all value of independent variable

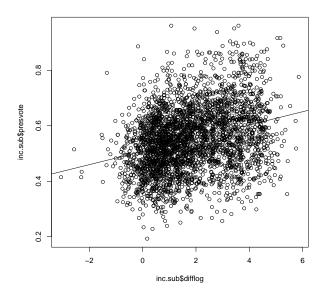
We run regression with presvote as outcome variable and difflog as the explanatory variable in R. We can then examine the regression coefficients using summary():

```
1 model_q2 <- lm(presvote ~ difflog, data=inc.sub)</pre>
2 summary (model_q2)
 Call:
 lm(formula = presvote ~ difflog, data = inc.sub)
 Residuals:
      Min
                 1Q
                     Median
                                   3Q
                                           Max
 -0.32196 -0.07407 -0.00102 0.07151
 Coefficients:
             Estimate Std. Error t value Pr(>|t|)
 (Intercept) 0.507583
                                   160.60
                                            <2e-16 ***
                         0.003161
 difflog
             0.023837
                         0.001359
                                    17.54
                                            <2e-16 ***
                 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
 Signif. codes:
 Residual standard error: 0.1104 on 3191 degrees of freedom
 Multiple R-squared: 0.08795, Adjusted R-squared: 0.08767
 F-statistic: 307.7 on 1 and 3191 DF, p-value: < 2.2e-16
```

2. Make a scatterplot of the two variables and add the regression line. We draw the scatterplot and regression line in R:

```
plot(inc.sub$difflog,inc.sub$presvote)
abline(model_q2)
```

Figure 2: Scatterplot between difference in campaign spending and the presidential candidate of the incumbent's party with regression line.



3. Save the residuals of the model in a separate object.

The residual of the model can be obtained in the model object in R.

1 head (model\_q2\$residuals)

We will assign it to an object

4. Write the prediction equation.

General form for prediction equation is:

$$\hat{y} = \beta_0 + \beta_1 x$$

Based on the coefficients of the regression on section 1 we have the following prediction equation:

$$\overrightarrow{\text{presvote}} = 0.507583 + 0.023837 \times \text{difflog}$$

With  $\widehat{presvote}$  as the predicted value for outcome variable and difflog as the explanatory variable

We are interested in knowing how the vote share of the presidential candidate of the incumbent's party is associated with the incumbent's electoral success.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **presvote**.

We need to declare our assumptions:

- Each observation is independent
- Observations are randomly generated
- There is a linear relationship between mean of the dependent variable and the value of independent variable
- The error term is normally distributed with mean 0 and has constant variable for all value of independent variable

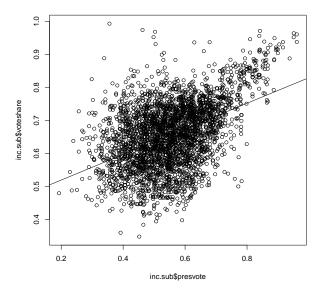
We run regression with voteshare as outcome variable and presvote as the explanatory variable in R. We can then examine the regression coefficients using summary():

```
model_q3 <- lm(voteshare ~ presvote, data=inc.sub)
2 summary (model_q3)
 Call:
 lm(formula = voteshare ~ presvote, data = inc.sub)
 Residuals:
      Min
                1Q
                     Median
                                   3Q
                                           Max
 -0.27330 -0.05888 0.00394 0.06148
                                      0.41365
 Coefficients:
             Estimate Std. Error t value Pr(>|t|)
                                    58.08
 (Intercept) 0.441330
                        0.007599
                                            <2e-16 ***
             0.388018
                        0.013493
                                    28.76
                                            <2e-16 ***
 presvote
                 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
 Signif. codes:
 Residual standard error: 0.08815 on 3191 degrees of freedom
 Multiple R-squared: 0.2058, Adjusted R-squared:
                827 on 1 and 3191 DF, p-value: < 2.2e-16
 F-statistic:
```

2. Make a scatterplot of the two variables and add the regression line. We draw the scatterplot and regression line in R:

```
plot(inc.sub$presvote,inc.sub$voteshare)
abline(model_q3)
```

Figure 3: Scatterplot between the presidential candidate of the incumbent's party and incumbent's vote share with regression line.



3. Write the prediction equation.

General form for prediction equation is:

$$\hat{y} = \beta_0 + \beta_1 x$$

Based on the coefficients of the regression on section 1 we have the following prediction equation:

$$\widehat{\text{voteshare}} = 0.441330 + 0.388018 \times \text{presvote}$$

With voteshare as the predicted value for outcome variable and presvote as the explanatory variable

The residuals from part (a) tell us how much of the variation in **voteshare** is *not* explained by the difference in spending between incumbent and challenger. The residuals in part (b) tell us how much of the variation in **presvote** is *not* explained by the difference in spending between incumbent and challenger in the district.

1. Run a regression where the outcome variable is the residuals from Question 1 and the explanatory variable is the residuals from Question 2.

We need to declare our assumptions:

- Each observation is independent
- Observations are randomly generated
- There is a linear relationship between mean of the dependent variable and the value of independent variable
- The error term is normally distributed with mean 0 and has constant variable for all value of independent variable

We will first combine the two residual vector into a dataframe. Lets call the residual from Q1 r\_votes\_difflog and Q2 r\_presv\_difflog. We run regression with r\_votes\_difflog as outcome variable and r\_presv\_difflog as the explanatory variable in R. We can then examine the regression coefficients using summary():

```
1 #combine resid q1 q2 data
2 df <- data.frame(r_votes_difflog = model_resid_votes_difflog, r_presv_
     difflog = model_resid_presv_difflog
3 #regression between resid Q1 and resid Q2
_{4} \mod_{q} = - \ln(r_{votes_{difflog_{r_{int}}}} r_{presv_{difflog_{int}}}, data = df)
5 summary (model_q4)
 Call:
 lm(formula = r_votes_difflog ~ r_presv_difflog, data = df)
 Residuals:
      Min
                 1Q
                      Median
                                     3Q
                                             Max
 -0.25928 -0.04737 -0.00121 0.04618 0.33126
 Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
                  -1.942e-18 1.299e-03
                                             0.00
 (Intercept)
                                                          1
 r_presv_difflog 2.569e-01 1.176e-02
                                            21.84
                                                     <2e-16 ***
 Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

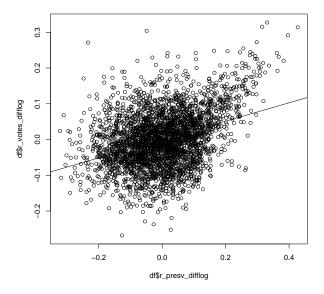
Residual standard error: 0.07338 on 3191 degrees of freedom Multiple R-squared: 0.13, Adjusted R-squared: 0.1298 F-statistic: 477 on 1 and 3191 DF, p-value: < 2.2e-16

One point to note is that the coefficient of the intercept is not statistically significant. Actually it is so small that it is not so much different than 0

2. Make a scatterplot of the two variables and add the regression line. We draw the scatterplot and regression line in R:

```
plot (df$r_presv_difflog , df$r_votes_difflog)
bline (model_q4)
```

Figure 4: Scatterplot between r\_votes\_difflog and r\_presv\_difflog with regression line.



3. Write the prediction equation.

General form for prediction equation is:

$$\hat{y} = \beta_0 + \beta_1 x$$

Based on the coefficients of the regression on section 1 we have the following prediction equation:

$$r_{\text{votes\_difflog}} = -1.942 \times 10^{-18} + 0.2569 \times r_{\text{presv\_difflog}}$$

With r\_votes\_difflog as the predicted value for outcome variable and r\_presv\_difflog as the explanatory variable

What if the incumbent's vote share is affected by both the president's popularity and the difference in spending between incumbent and challenger?

1. Run a regression where the outcome variable is the incumbent's voteshare and the explanatory variables are difflog and presvote.

We need to declare our assumptions:

- Each observation is independent
- Observations are randomly generated
- There is a linear relationship between mean of the dependent variable and the value of independent variables
- The error term is normally distributed with mean 0 and has constant variable for all value of independent variable

We run regression with voteshare as outcome variable and presvote and difflog as the explanatory variables in R. We can then examine the regression coefficients using summary():

```
model_q5 \leftarrow lm(voteshare ~ presvote + difflog, data = inc.sub)
2 summary (model_q5)
 Call:
 lm(formula = voteshare ~ presvote + difflog, data = inc.sub)
 Residuals:
      Min
                1Q
                     Median
                                   3Q
                                           Max
 -0.25928 -0.04737 -0.00121 0.04618
 Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                                    70.88
 (Intercept) 0.4486442 0.0063297
                                             <2e-16 ***
             0.2568770 0.0117637
                                     21.84
                                             <2e-16 ***
 presvote
                                    37.59
 difflog
             0.0355431 0.0009455
                                             <2e-16 ***
                 0 '***, 0.001 '**, 0.01 '*, 0.05 '., 0.1 ', 1
 Signif. codes:
 Residual standard error: 0.07339 on 3190 degrees of freedom
 Multiple R-squared: 0.4496, Adjusted R-squared: 0.4493
 F-statistic: 1303 on 2 and 3190 DF, p-value: < 2.2e-16
```

2. Write the prediction equation.

General form for prediction equation is:

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n$$

Based on the coefficients of the regression on section 1 we have the following prediction equation:

$$\widehat{\text{voteshare}} = 0.4486442 + 0.2568770 \times \text{presvote} + 0.0355431 \times \text{difflog}$$

With voteshare as the predicted value for outcome variable and presvote, difflog as the explanatory variables

3. What is it in this output that is identical to the output in Question 4? Why do you think this is the case?

The model coefficient, standard error, t-value and p-values for variable presvote in question 5 are identical to the model coefficient, standard error, t-value and p-values for variable r\_presv\_difflog in question 4.

The coefficient for presvote in question 5 is the effect of the variable to voteshare when we have already takes into account the effect of difflog on both presvote and voteshare. At the same time, the residual in question 1 is the unexplained variation of voteshare that is not explained by difflog. The residual in question 2 is the unexplained variation of presvote that is not explained by difflog. If we regress the first residual on the second residual it should be the same as the remaining effect of presvote on the remaining unexplained variation of voteshare that's has taken into account all the effect of difflog