

## AoPS Prealgebra – AoPS Sections to Brilliant Lessons

### Chapter 1: Properties of Arithmetic

| AoPS Section                   | Brilliant Lessons   |
|--------------------------------|---|
| 1.1 Why Start with Arithmetic? | Growing and Shrinking; A Pair at Every Distance; Absolute Value                                 |
| 1.2 Addition                   | Adding Any Fractions; Adding Fractions; Adding Large Integers                                   |
| 1.3 Multiplication             | Calculating Percent Decrease; Expressing Multiples; Fraction of Any Fraction                    |
| 1.4 Negation                   | Finding Half; Combining Parts; Splitting Parts  |
| 1.5 Subtraction                | Absolute Value and Distance; Adding The Opposite; Adding in Any Order                           |
| 1.6 Reciprocals                | Fraction of Any Fraction; Dividing Fractions by Fractions; Turning Multiplication Into Division |
| 1.7 Division                   | Dividing Whole Numbers; Dividing Fractions by Fractions; Dividing Decimals                      |
| 1.8 Summary Review Problems    | Adding Large Integers; Dividing Whole Numbers; Absolute Value and Distance                      |
| Challenge Problems             |   |

### Chapter 2: Exponents

| AoPS Section                     | Brilliant Lessons   |
|----------------------------------|---|
| 2.1 Exponent Basics              | Exponent Review; Exponent Properties; Exponent Rules          |
| 2.2 Exponents and Multiplication | Exponent Properties; Exponent Rules; Rewriting Exponents      |
| 2.3 Exponents and Division       | Negative Exponents; Exponent Rules; Dividing by Powers of Ten |
| 2.4 Raising a Product            | Exponent Rules; Exponent Review; Powers of Powers             |
| 2.5 Summary Review Problems      | Exponent Review; Exponent Rules; Negative Exponents           |
| Challenge Problems               |   |

### Chapter 3: Number Theory

| AoPS Section                 | Brilliant Lessons  |
|------------------------------|--|
| 3.1 Divisibility and Primes  | Prime Patterns; Testing for Primes; Divisibility Rules               |
| 3.2 Prime Factorization      | Factor Trees; Prime Factorization; Fundamental Theorem of Arithmetic |
| 3.3 Greatest Common Divisors | Greatest Common Factor; Factoring Numbers; Prime Factors and GCF     |
| 3.4 Least Common Multiples   | Least Common Multiple; Relating LCM and GCF; Multiples and Factors   |
| 3.5 Summary Review Problems  | Prime Patterns; Greatest Common Factor; Least Common Multiple        |
| Challenge Problems           |  |

## Chapter 4: Fractions

| AoPS Section                         | Brilliant Lessons  |
|--------------------------------------|--|
| 4.1 What is a Fraction?              | Finding Half; Splitting Parts; Combining Parts                             |
| 4.2 Equivalent Fractions             | Equivalent Fractions; Splitting Parts; Combining Parts                     |
| 4.3 Comparing Fractions              | Comparing Fractions; Ordering Fractions; Benchmark Fractions               |
| 4.4 Adding and Subtracting Fractions | Adding Fractions; Subtracting Fractions; Adding Any Fractions              |
| 4.5 Multiplying Fractions            | Multiplying Fractions; Fraction of Any Fraction; Multiplying Mixed Numbers |
| 4.6 Summary Review Problems          | Adding Fractions; Multiplying Fractions; Comparing Fractions               |
| Challenge Problems                   |  |

## Chapter 5: Equations and Inequalities

| AoPS Section                | Brilliant Lessons   |
|-----------------------------|---|
| 5.1 Variables               | Using Variables; Building Expressions; Function Machines                    |
| 5.2 Expressions             | Building Expressions; Comparing Expressions; Rearranging Expressions        |
| 5.3 Equations               | Solving an Equation; Balancing with Constants; Balancing with Variables     |
| 5.4 Inequalities            | Inequalities on a Number Line; Which Is Greater; Interpreting Inequalities  |
| 5.5 Summary Review Problems | Solving an Equation; Rearranging Expressions; Inequalities on a Number Line |
| Challenge Problems          |   |

## Chapter 6: Decimals

| AoPS Section                | Brilliant Lessons  |
|-----------------------------|--|
| 6.1 Decimal Basics          | Place Value; Decimals on the Number Line; Comparing Decimals       |
| 6.2 Decimal Arithmetic      | Adding Decimals; Subtracting Decimals; Multiplying Decimals        |
| 6.3 More Decimal Arithmetic | Dividing Decimals; Scaling With Decimals; Estimating With Decimals |
| 6.4 Summary Review Problems | Adding Decimals; Dividing Decimals; Estimating With Decimals       |
| Challenge Problems          |  |

## Chapter 7: Ratios, Conversions, and Rates

| AoPS Section    | Brilliant Lessons  |
|-----------------|--|
| 7.1 Ratios      | Setting Up Ratios; Making Batches; Scale Factor                      |
| 7.2 Unit Rates  | Computing Unit Rates; How Much for One; Finding Unit Cost            |
| 7.3 Conversions | Using Unit Prices; Using Unit Prices to Find Cost; Controlling Costs |

| <b>AoPS Section</b>                               | <b>Brilliant Lessons</b>   |
|---|--|
| 7.4 More About Rates                              | Comparing Rates; Graphing Relationships; Graphing from an Equation |
| 7.5 Summary Review Problems<br>Challenge Problems | Setting Up Ratios; Computing Unit Rates; Using Unit Prices         |

## Chapter 8: Percents

| <b>AoPS Section</b>                               | <b>Brilliant Lessons</b>   |
|---|--|
| 8.1 Percent Basics                                | Calculating Percentages; Working with Percentages; Percent Discount  |
| 8.2 Percent Increase and Decrease                 | Calculating Percentages; Percent Discount; Working with Percentages  |
| 8.3 Percent of a Quantity                         | Calculating Percentages; Working with Percentages; Using Unit Prices |
| 8.4 Summary Review Problems<br>Challenge Problems | Calculating Percentages; Percent Discount; Comparing Offers          |

## Chapter 9: Square Roots

| <b>AoPS Section</b>                               | <b>Brilliant Lessons</b>  |
|---|---|
| 9.1 Squares                                       | Area and Squares; Squaring Numbers; Perfect Squares                                 |
| 9.2 Square Roots                                  | Square Roots; Estimating Square Roots; Square Roots on the Number Line              |
| 9.3 Approximating Square Roots                    | Estimating Square Roots; Square Roots on the Number Line; Approximating Irrationals |
| 9.4 Summary Review Problems<br>Challenge Problems | Square Roots; Estimating Square Roots; Perfect Squares                              |

## Chapter 10: Angles

| <b>AoPS Section</b>                                | <b>Brilliant Lessons</b>  |
|--|---|
| 10.1 Angle Basics                                  | Measuring Angles; Types of Angles; Angle Vocabulary                                       |
| 10.2 Angle Relationships                           | Angle Relationships; Complementary and Supplementary Angles; Vertical Angles              |
| 10.3 Parallel Lines and Transversals               | Angles With Parallel Lines; Interior and Exterior Angles; Transversal Angle Relationships |
| 10.4 Summary Review Problems<br>Challenge Problems | Angle Relationships; Measuring Angles; Angles With Parallel Lines                         |

## Chapter 11: Perimeter and Area

| AoPS Section                 | Brilliant Lessons  |
|------------------------------|--|
| 11.1 Perimeter               | Perimeter of Polygons; Measuring Perimeter; Perimeter and Scale              |
| 11.2 Area of Triangles       | Area of Triangles; Decomposing Shapes; Relating Parallelograms and Triangles |
| 11.3 Area of Quadrilaterals  | Area of Parallelograms; Area of Trapezoids; Decomposing Shapes               |
| 11.4 Area of Circles         | Area of Circles; Circumference and Area; Using Pi in Area                    |
| 11.5 Summary Review Problems | Perimeter of Polygons; Area of Triangles; Area of Parallelograms             |
| Challenge Problems           |  |

## Chapter 12: Right Triangles and Quadrilaterals

| AoPS Section                 | Brilliant Lessons  |
|------------------------------|--|
| 12.1 Pythagorean Theorem     | Pythagorean Theorem; Distance in the Plane; Right Triangle Distances           |
| 12.2 Special Right Triangles | Special Right Triangles; Pythagorean Triples; Applying the Pythagorean Theorem |
| 12.3 Quadrilateral Review    | Quadrilateral Types; Properties of Quadrilaterals; Classifying Quadrilaterals  |
| 12.4 Summary Review Problems | Pythagorean Theorem; Special Right Triangles; Quadrilateral Types              |
| Challenge Problems           |  |

## Chapter 13: Data and Statistics

| AoPS Section                 | Brilliant Lessons  |
|------------------------------|--|
| 13.1 Displaying Data         | Visualizing Data Distributions; Dot Plots; Histograms                          |
| 13.2 Measures of Center      | Mean and Median; Comparing Center and Spread; Interpreting Measures of Center  |
| 13.3 Measures of Spread      | Range and Interquartile Range; Variability; Interpreting Spread                |
| 13.4 Summary Review Problems | Visualizing Data Distributions; Mean and Median; Range and Interquartile Range |
| Challenge Problems           |  |

## Chapter 14: Counting and Probability

| AoPS Section             | Brilliant Lessons  |
|--------------------------|--|
| 14.1 Counting Strategies | Counting Outcomes; Systematic Listing; Multiplication Principle        |
| 14.2 Basic Probability   | Sample Space Exploration; Simple Probability; Interpreting Probability |
| 14.3 Compound Events     | Simple Compound Events; Independent Events; Dependent Events           |

| AoPS Section                                       | Brilliant Lessons   |
|--|---|
| 14.4 Summary Review Problems<br>Challenge Problems | Counting Outcomes; Sample Space Exploration; Simple Compound Events |

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## Chapter 15: Problem-Solving Strategies

| AoPS Section                                       | Brilliant Lessons |
|--|-------------------|
| 15.1 Find a Pattern                                |                   |
| 15.2 Make a List                                   |                   |
| 15.3 Draw a Picture                                |                   |
| 15.4 Work Backwards                                |                   |
| 15.5 Summary Review Problems<br>Challenge Problems |                   |

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