

AoPS Introduction to Algebra – AoPS Sections to Brilliant Lessons

Chapter 1: Follow the Rules

| AoPS Section | Brilliant Lessons |
|---|---|
| 1.1 Numbers | Growing and Shrinking; A Pair at Every Distance; Absolute Value |
| 1.2 Order of Operations | Order of Operations; When Does Order Matter; Exponent Rules |
| 1.3 When Does Order Matter? | When Does Order Matter; Grouping and Order; Order of Operations |
| 1.4 Distribution and Factoring | Distributing and Grouping; Factoring; Rearranging Expressions |
| 1.5 Equations | Solving an Equation; Balancing with Constants; Balancing with Variables |
| 1.6 Exponents | Exponent Review; Exponent Properties; Exponent Rules |
| 1.7 Fractional Exponents | Fractional Exponents; Roots and Exponents; Rewriting Exponents |
| 1.8 Radicals | Radicals and Roots; Simplifying Radicals; Radical Expressions |
| 1.9 Summary Review Problems Challenge Problems | Order of Operations; Distributing and Grouping; Solving an Equation |

Chapter 2: x Marks the Spot

| AoPS Section | Brilliant Lessons |
|---|---|
| 2.1 Expressions | Building Expressions; Expressions and Patterns; Comparing Expressions |
| 2.2 Arithmetic with Expressions | Arithmetic with Expressions; Combining Like Terms; Distribution and Combination |
| 2.3 Distribution, Subtraction, and Factoring | Distributing and Grouping; Factoring; Rearranging Expressions |
| 2.4 Equations With Fractions | Solving Equations With Fractions; Balancing with Fractions; Clearing Denominators |
| 2.5 Summary Review Problems Challenge Problems | Building Expressions; Distributing and Grouping; Solving Equations With Fractions |

Chapter 3: One Variable Linear Equations

| AoPS Section | Brilliant Lessons |
|------------------------------|---|
| 3.1 One Step Equations | Solving an Equation; Balancing with Constants; Inverse Operations |
| 3.2 Multi Step Equations | Solving Multi Step Equations; Rearranging Equations; Isolating the Variable |
| 3.3 Equations With Fractions | Solving Equations With Fractions; Balancing with Fractions; Clearing Denominators |

| AoPS Section | Brilliant Lessons |
|---|---|
| 3.4 Absolute Value Equations | Absolute Value and Distance; Absolute Value Equations; Which Is Greater |
| 3.5 Summary Review Problems Challenge Problems | Solving an Equation; Solving Multi Step Equations; Absolute Value Equations |

Chapter 4: More Variables

| AoPS Section | Brilliant Lessons |
|---|---|
| 4.1 Evaluating Multi Variable Expressions | Balancing with Variables; Building Expressions; Distributing |
| 4.2 Still More Arithmetic | Finding Unknowns; Solving an Equation; Apply: Rules of Thumb |
| 4.3 Distribution and Factoring | Factoring; Completing the Square; Difference of Squares |
| 4.4 Summary Review Problems Challenge Problems | Building Expressions; Rearranging Expressions; Balancing with Variables |

Chapter 5: Multi Variable Linear Equations

| AoPS Section | Brilliant Lessons |
|---|---|
| 5.1 Systems of Equations | Systems of Equations; Two Equations Two Unknowns; Intersection Points |
| 5.2 Substitution | Substitution Method; Solving With Substitution; Using Formulas |
| 5.3 Elimination | Elimination Method; Combining Equations; Linear Combinations |
| 5.4 Word Problems | Translating Word Problems; Using Variables; Comparing Offers |
| 5.5 Summary Review Problems Challenge Problems | Systems of Equations; Substitution Method; Elimination Method |

Chapter 6: Ratios and Percents

| AoPS Section | Brilliant Lessons |
|---|---|
| 6.1 Basic Ratio Problems | Computing Unit Rates; Finding Batches; Finding Unit Cost |
| 6.2 More Challenging Ratio Problems | Computing Unit Rates; Finding Batches; Finding Unit Cost |
| 6.3 Conversion Factors | Setting Up Ratios; Scaling Up; Scaling Down |
| 6.4 Percent | Calculating Percentages; Percent Discount; Working with Percentages |
| 6.5 Percentage Problems | Calculating Percentages; Percent Discount; Working with Percentages |
| 6.6 Summary Review Problems Challenge Problems | Setting Up Ratios; Scaling Up; Scaling Down |

Chapter 7: Proportion

| AoPS Section | Brilliant Lessons |
|------------------------------|--|
| 7.1 Direct Proportion | Graphing Relationships; Constant of Proportionality; Writing Equations |
| 7.2 Inverse Proportion | Graphing Relationships; Graphing Comparisons; Using Graphs |
| 7.3 Proportion Word Problems | Using Unit Prices; Comparing Offers; Controlling Costs |
| 7.4 Summary Review Problems | Graphing Relationships; Constant of Proportionality; |
| Challenge Problems | Comparing Offers |

Chapter 8: Graphing Lines

| AoPS Section | Brilliant Lessons |
|-----------------------------|---|
| 8.1 Coordinates | Plotting Points; Plotting Equivalent Ratios; Coordinates in the Plane |
| 8.2 Graphs of Equations | Graphing from an Equation; Graphing Relationships; Graphing Lines |
| 8.3 Slope | Slope Interpretation Tasks; Slope as Rate; Steepness and Direction |
| 8.4 Slope Intercept | Graphing from an Equation; Writing Equations; Graphing Comparisons |
| 8.5 Slope and Intercepts | Graphing Lines; Comparing Lines; Slope and Intercept Interpretation |
| 8.6 Comparing Lines | Comparing Lines; Graphing Comparisons; Interpreting Graphs |
| 8.7 Summary Review Problems | Plotting Points; Graphing Relationships; Comparing Lines |
| Challenge Problems | |

Chapter 9: Introduction to Inequalities

| AoPS Section | Brilliant Lessons |
|-----------------------------|---|
| 9.1 The Basics | Inequalities on a Number Line; Which Is Greater; Interpreting Inequalities |
| 9.2 Which Is Greater? | Which Is Greater; Absolute Value and Distance; Comparing Quantities |
| 9.3 Linear Inequalities | Solving Inequalities; Linear Inequalities; Graphing Inequalities |
| 9.4 Graphing Inequalities | Graphing Inequalities; Regions on the Line; Inequalities on a Number Line |
| 9.5 Optimization | Optimization with Constraints; Regions and Inequalities; Applications of Inequalities |
| 9.6 Summary Review Problems | Linear Inequalities; Graphing Inequalities; Optimization with Constraints |
| Challenge Problems | |

Chapter 10: Quadratic Equations – Part 1

| AoPS Section | Brilliant Lessons |
|--|--|
| 10.1 Getting Started With Quadratics | Quadratic Patterns; Quadratic Functions; Factoring Quadratics |
| 10.2 Factoring Quadratics I | Factoring Quadratics; Factoring Using Patterns; Factoring Practice |
| 10.3 Factoring Quadratics II | Factoring Quadratics; Factoring Challenge; Factoring by Grouping |
| 10.4 Sums and Products of Roots of a Quadratic | Roots and Coefficients; Sums and Products; Quadratic Roots |
| 10.5 ★ Extensions and Applications | Quadratic Applications; Roots and Graphs; Modeling With Quadratics |
| 10.6 Summary Review Problems Challenge Problems | Factoring Quadratics; Quadratic Patterns; Quadratic Applications |

Chapter 11: Special Factorizations

| AoPS Section | Brilliant Lessons |
|--|---|
| 11.1 Squares of Binomials | Squares of Binomials; Recognizing Patterns; Expansion and Factoring |
| 11.2 Difference of Squares | Difference of Squares; Factoring Patterns; Quadratic Identities |
| 11.3 Sum and Difference of Cubes | Sum and Difference of Cubes; Factoring Higher Powers; Polynomial Patterns |
| 11.4 Rationalizing Denominators | Rationalizing Denominators; Radical Expressions; Simplifying Fractions |
| 11.5 Simon's Favorite Factoring Trick | Factoring Challenge; Special Factoring Tricks; Rearranging Expressions |
| 11.6 Summary Review Problems Challenge Problems | Squares of Binomials; Difference of Squares; Sum and Difference of Cubes |

Chapter 12: Complex Numbers

| AoPS Section | Brilliant Lessons |
|--|--------------------------|
| 12.1 Numbers, Numbers, and More Numbers! | |
| 12.2 Arithmetic With Complex Numbers | |
| 12.3 Summary Review Problems Challenge Problems | |

Chapter 13: Quadratic Equations – Part 2

| AoPS Section | Brilliant Lessons |
|----------------------------|---|
| 13.1 Completing the Square | Completing the Square; Quadratic Transformations; Vertex Form |

| AoPS Section | Brilliant Lessons |
|--|--|
| 13.2 Quadratic Formula | Quadratic Formula; Deriving the Formula; Using the Quadratic Formula |
| 13.3 Applications | Quadratic Applications; Modeling With Quadratics; Roots and Graphs |
| 13.4 Summary Review Problems Challenge Problems | Completing the Square; Quadratic Formula; Quadratic Applications |

Chapter 14: Graphing Quadratics

| AoPS Section | Brilliant Lessons |
|--|---|
| 14.1 Parabolas | Graphing Parabolas; Vertex and Axis; Quadratic Graph Features |
| 14.2 Quadratic Transformations | Quadratic Transformations; Shifting Graphs; Stretching and Compressing |
| 14.3 Summary Review Problems Challenge Problems | Graphing Parabolas; Quadratic Transformations; Comparing Quadratic Graphs |

Chapter 15: More Inequalities

| AoPS Section | Brilliant Lessons |
|--|--|
| 15.1 Quadratic Inequalities | Quadratic Inequalities; Regions and Parabolas; Graphing Inequality Solutions |
| 15.2 More Optimization | Optimization with Constraints; Quadratics in Optimization; Regions and Inequalities |
| 15.3 Summary Review Problems Challenge Problems | Quadratic Inequalities; Optimization with Constraints; Graphing Inequality Solutions |

Chapter 16: Functions

| AoPS Section | Brilliant Lessons |
|--|--|
| 16.1 Function Basics | Function Machines; Input and Output; Function Rules |
| 16.2 Function Notation | Function Notation; Evaluating Functions; Input Output Rules |
| 16.3 Combining Functions | Combining Functions; Function Operations; Building New Functions |
| 16.4 Summary Review Problems Challenge Problems | Function Machines; Function Notation; Combining Functions |

Chapter 17: Graphing Functions

| AoPS Section | Brilliant Lessons |
|------------------------|---|
| 17.1 Graphs and Tables | Comparing Functions; Tables and Graphs; Interpreting Graphs |

| AoPS Section | Brilliant Lessons |
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| 17.2 Features of Graphs | Features of Graphs; Maxima and Minima; Intercepts and Intervals |
| 17.3 Transformations of Graphs | Transformations of Functions; Shifting and Scaling; Coordinate Transformations |
| 17.4 Summary Review Problems Challenge Problems | Comparing Functions; Features of Graphs; Transformations of Functions |

Chapter 18: Polynomials

| AoPS Section | Brilliant Lessons |
|--|---|
| 18.1 Polynomial Basics | Polynomial Vocabulary; Combining Like Terms; Polynomial Degree |
| 18.2 Polynomial Arithmetic | Polynomial Addition and Subtraction; Multiplying Polynomials; Distributing and Grouping |
| 18.3 Factoring Polynomials | Factoring Polynomials; Factoring by Grouping; Factoring Patterns |
| 18.4 Summary Review Problems Challenge Problems | Polynomial Addition and Subtraction; Multiplying Polynomials; Factoring Polynomials |

Chapter 19: Exponents and Logarithms

| AoPS Section | Brilliant Lessons |
|--|--|
| 19.1 Exponential Functions | Exponential Functions; Growth and Decay; Rewriting Exponents |
| 19.2 Show Me the Money | Show Me the Money; Interest Calculations; Compound Growth |
| 19.3 Interest interesting Problems | Compound Interest; Interest Calculations; Exponential Growth |
| 19.4 What is a Logarithm? | What is a Logarithm; Logarithms and Exponents; Inverse Relationships |
| 19.5 Summary Review Problems Challenge Problems | Exponential Functions; Show Me the Money; What is a Logarithm |

Chapter 20: Special Functions

| AoPS Section | Brilliant Lessons |
|-------------------------|--|
| 20.1 Radicals | Radical Functions; Radical Expressions; Graphing Radicals |
| 20.2 Absolute Value | Absolute Value Functions; Absolute Value and Distance; Graphing Absolute Value |
| 20.3 Floor and Ceiling | Step Functions; Floor and Ceiling Functions; Piecewise Behavior |
| 20.4 Rational Functions | Rational Functions; Graphing Rational Functions; Asymptotes and Behavior |

| AoPS Section | Brilliant Lessons |
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| 20.5 Piecewise Defined Functions | Piecewise Defined Functions; Interpreting Piecewise Graphs; Modeling With Piecewise Functions |
| 20.6 Summary Review Problems Challenge Problems | Absolute Value Functions; Radical Functions; Piecewise Defined Functions |

Chapter 21: Sequences & Series

| AoPS Section | Brilliant Lessons |
|--|--|
| 21.1 Arithmetic Sequences | Exponential Patterns; Repeated Change; Sequences and Patterns |
| 21.2 Arithmetic Series | Sequences and Sums; Series and Patterns; Summing Patterns |
| 21.3 Geometric Sequences | Exponential Growth; Geometric Sequences; Repeated Multiplication |
| 21.4 Geometric Series | Series and Growth; Geometric Series; Summing Infinite Series (intro level) |
| 21.5 ★ Telescoping | Telescoping Patterns; Series and Cancellation; Special Series Tricks |
| 21.6 Summary Review Problems Challenge Problems | Sequences and Patterns; Sequences and Sums; Geometric Sequences |

Chapter 22: Special Manipulations

| AoPS Section | Brilliant Lessons |
|--|--------------------------|
| 22.1 Raising Equations to Powers | |
| 22.2 Self similarity | |
| 22.3 Symmetry | |
| 22.4 Summary Review Problems Challenge Problems | |