

MATHEMATICAL MODELLING FOR ALL-SOLID-STATE BATTERY

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Mathematical modelling for the next-generation All-solid-state batteries: Nucleation (SE|SSE)^(*)-Interface

Rechargeable Lithium-ion battery (LIB) is at the heart of every electric vehicle (EV), portable electronic device, and energy storage system [5]. Nowadays, LIBs enable human life more efficient and help to solve global environment issues thanks to EVs' zero emission. However, conventional LIB (c-LIB) is sensible to temperature and pressure, hence, flammable and explosive, which is undesirable. This bottleneck is mainly due to **liquid-based electrolyte** found in c-LIBs.

Next-generation All-solid-state battery (ng-ASSB) with a consideration of **nucleation criterion** defined by

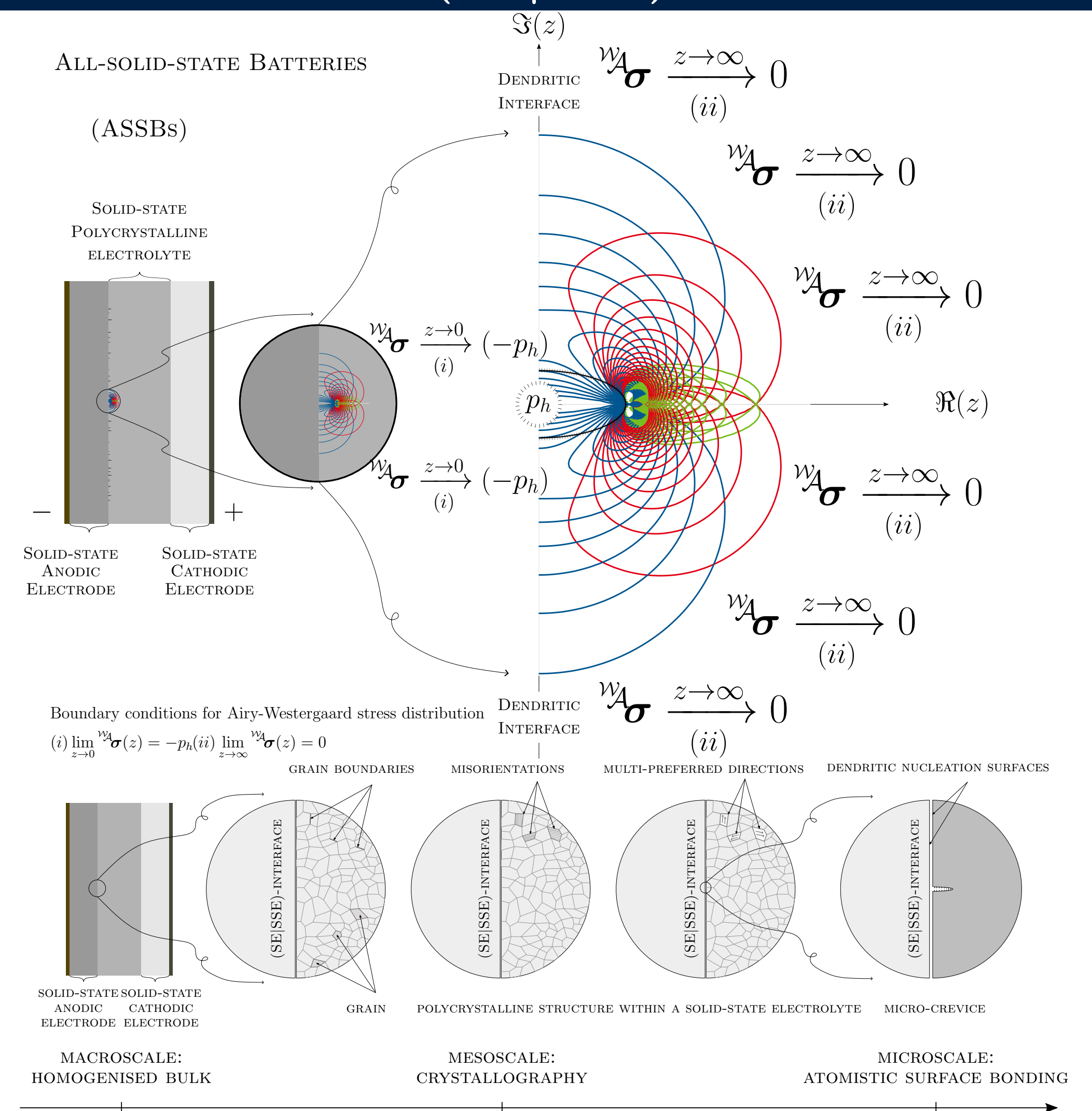
$$\partial_t \mathbf{u} + \nabla \cdot \left(\mathbf{C}^{f_{\text{allocation}}}(\lambda, \mu, \mathbf{d}_{G,i}^R, i=1, \dots, N, \mathbf{d}^E; \mathbf{x}) : \nabla \mathbf{u}^{(s)} \right) + \rho \mathbf{b} = -\rho \nabla V_e, \quad (1)$$

$$\text{s.t. } a_{\text{Griffith}}^{\text{generalised}} := a^* = \arg \min_{a \in \mathbb{R}} \iint_{\Omega} f(a, \mathbf{u}, \theta; \lambda, \mu, \mathbf{d}^{(*)} \otimes \mathbf{d}^{(*)}) d\Omega - \iint_{\Gamma} f(a; \gamma) d\Gamma \Big|_{\mathbf{u}} \quad (2)$$

where $V_e: \mathbb{R}^3 \rightarrow \mathbb{R}$ is the electric potential applied globally on ASSB. Due to nature setting of ASSB taking the form (SE|SSE|SE) the electric potential becomes uniform. Additionally, \mathbf{u} is the displacement field, θ temperature field, a crevice length, λ, μ Lamé constants, $\mathbf{d}^{(*)} \otimes \mathbf{d}^{(*)}$ embedded misorientation structural tensor, and γ cracking-surface energy density, can help to improve ASSB performance [1][2].

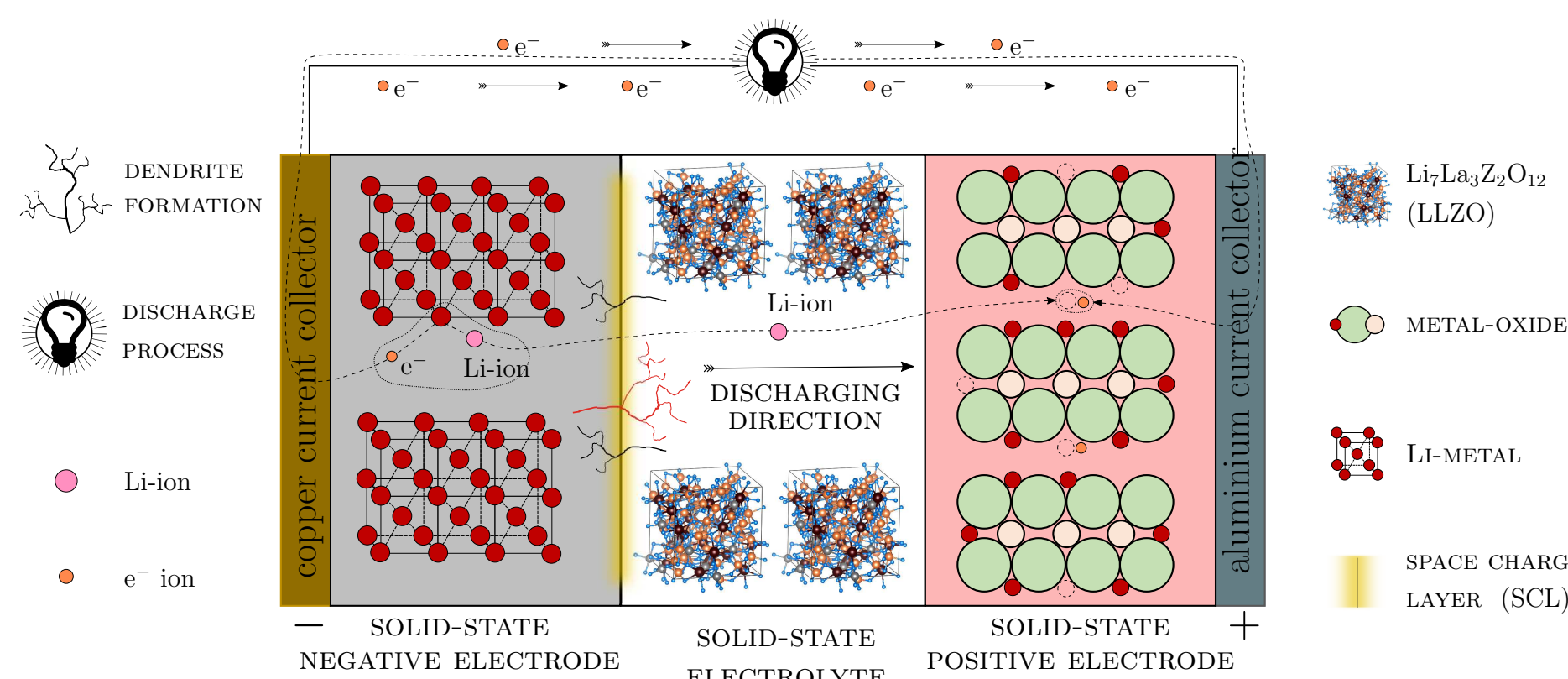
Aim: The study is with the purpose of gaining a better insight into dendrite nucleation and formation in ASSB.

All-solid-state battery (ASSB) is one of promising candidates to overcome bottlenecks of c-LIBs. Thanks to **solid-state electrolyte (SSE)**, ASSB is highly stable towards temperature and pressure. Nevertheless, Li-metal dendrite triggered at (SE|SSE)-Interface is the main drawback of ASSB since these dendritic threads extrapolate into SSE grain boundary network, causing crevice, degradation of ionic conductivity, and the probability of short-circuit, which is unfavorable [10].



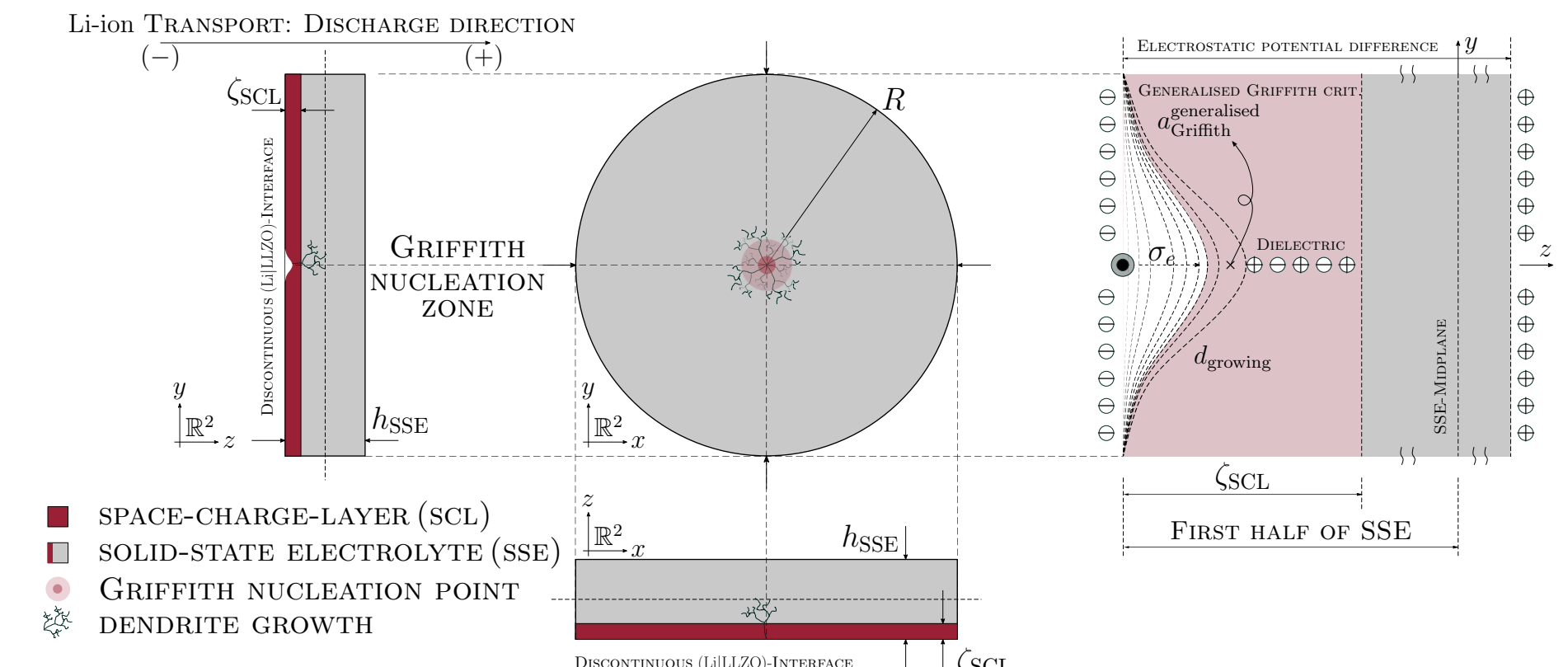
Next-generation All-solid-state battery

Griffith nucleation criterion governs (SE|SSE)-Interface.



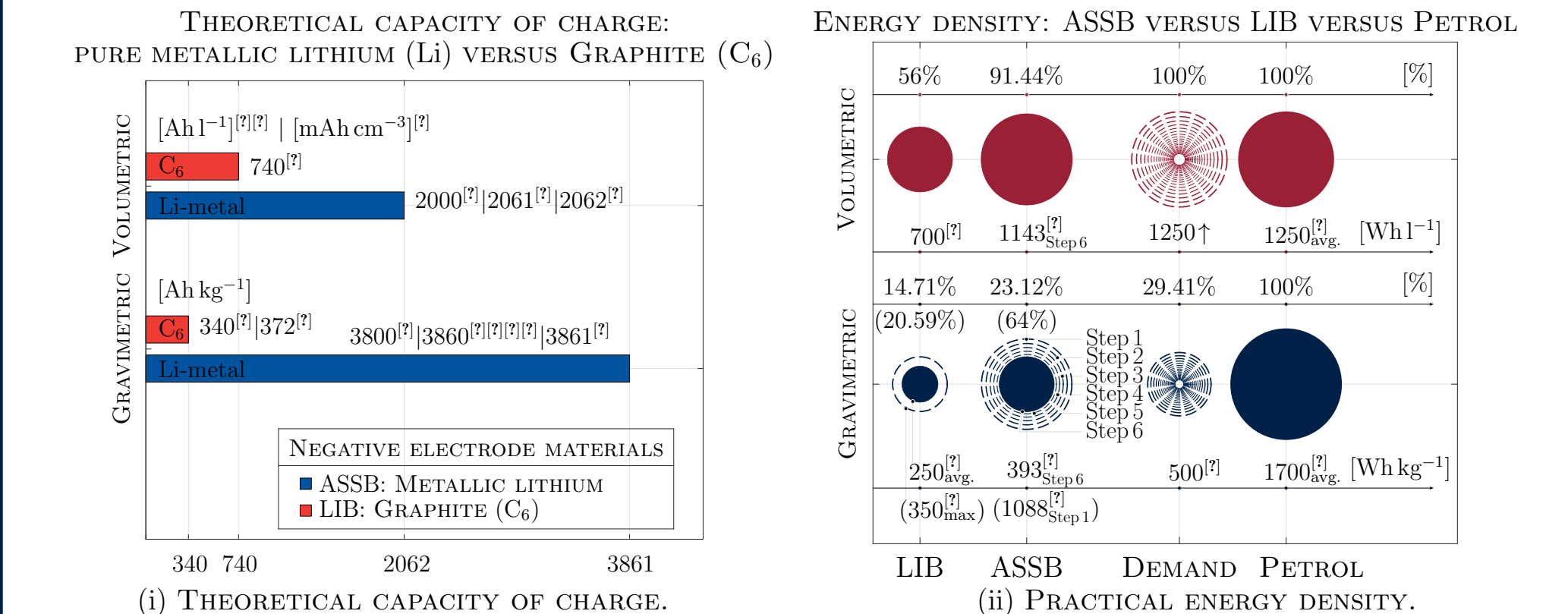
Space-charge Layer

SCL presents in ASSB [8], and likewise in Semiconductors.



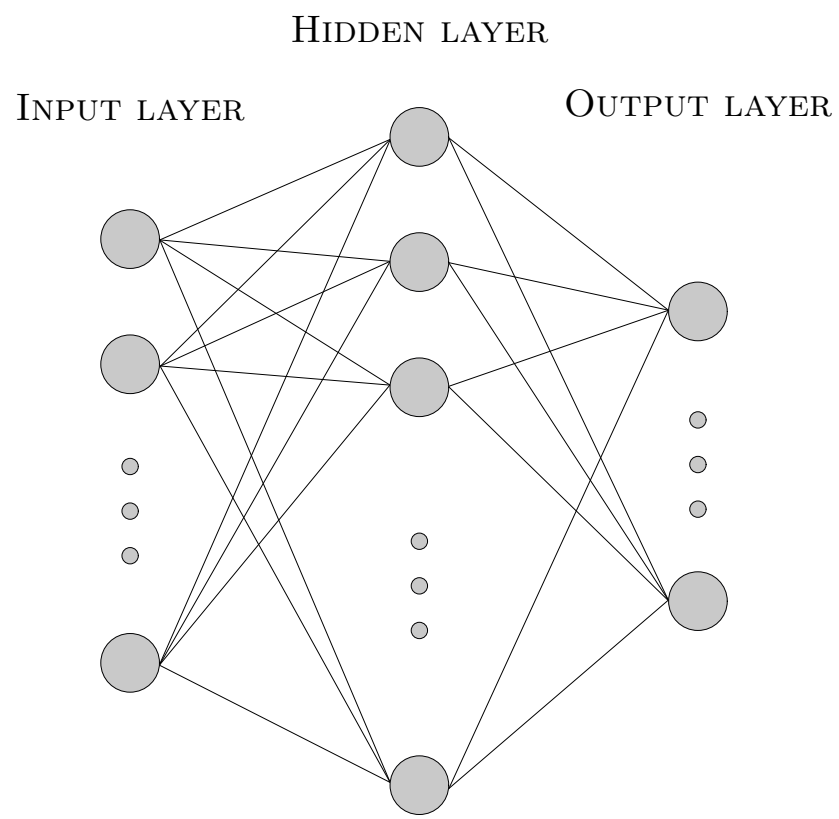
Energy density landscape

ASSB enables energy demand thanks to (i), and followed by (ii).



Artificial Neural Networks

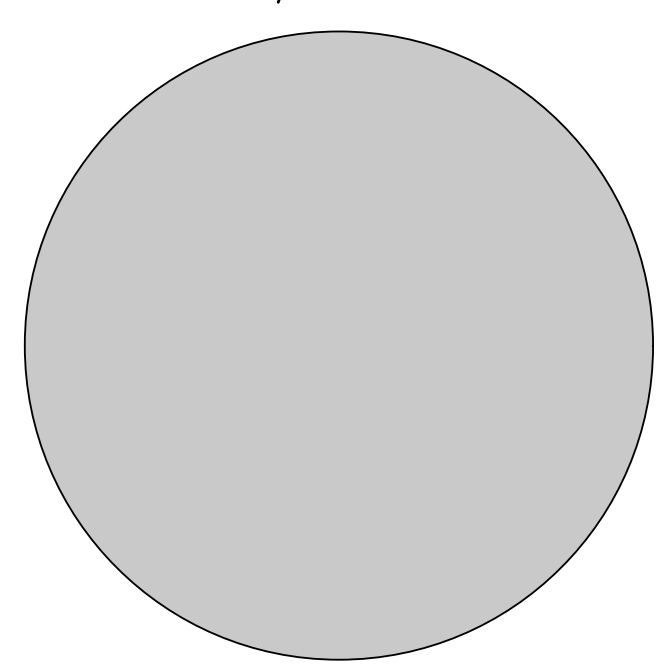
Application: Steel's property prediction.



An augmentation scheme for the prediction of the bainitic transformation temperature is validated by means of ANNs [9].

Semiconductor

Application: Start/Stop Starter Motor.



text [7]

Nucleation interface: Taking place at the critically dendritic (SE|SSE)-Interface

Coupled fields are Displacement field \mathbf{u} and temperature field θ ;

$$\mathbf{u}: \begin{cases} \Omega \times \mathbb{R}_+ \rightarrow \mathbb{R}^3, \\ (\mathbf{x}, t) \mapsto \mathbf{u}(\mathbf{x}, t), \end{cases} \quad \theta: \begin{cases} \Omega \times \mathbb{R}_+ \rightarrow \mathbb{R}, \\ (\mathbf{x}, t) \mapsto \theta(\mathbf{x}, t), \end{cases}$$

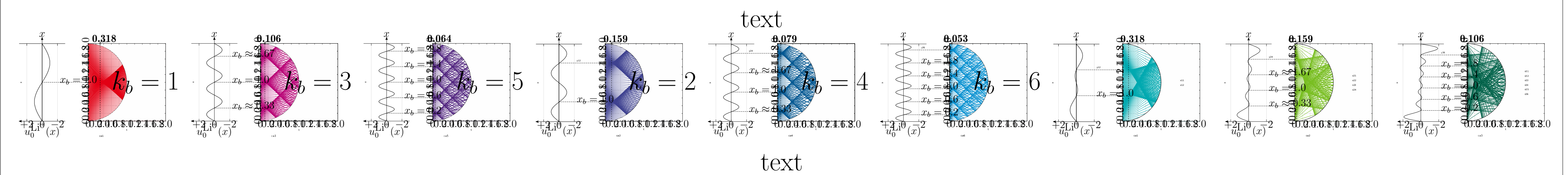
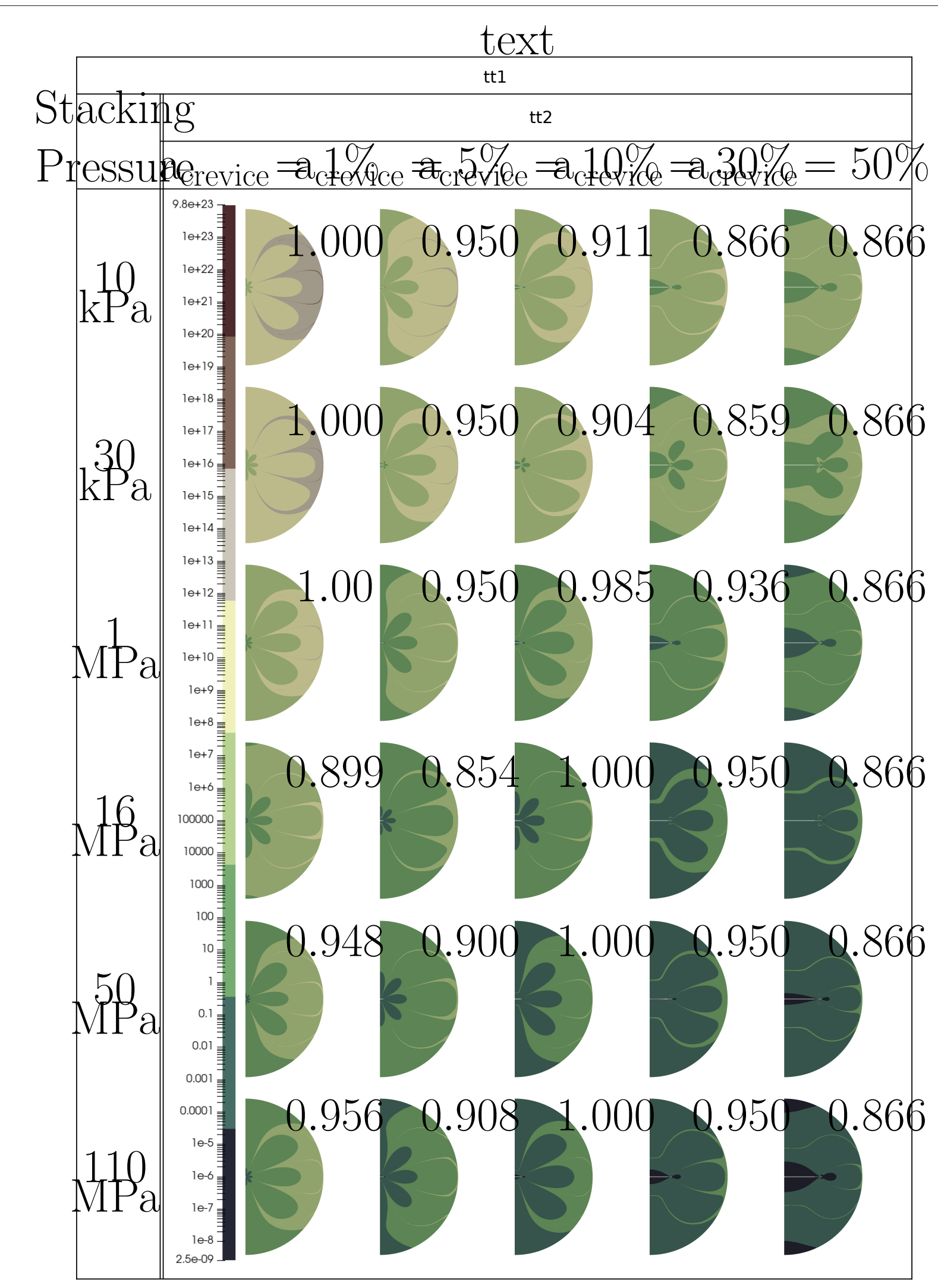
Governing conservation equations used to describe balance of mass, conservation of linear momentum, conservation of angular momentum, and conservation of energy with $\rho(\mathbf{x}, t)$ is mass density per unit volume (puv); $\mathbf{b}(\mathbf{x}, t)$ body force puv; $\mathbf{v}(\mathbf{x}, t)$ velocity; $e(\mathbf{x}, t)$ internal energy puv; $\mathbf{q}(\mathbf{x}, t)$ heat flux; $r(\mathbf{x}, t)$ heat source puv; $\boldsymbol{\sigma}$ Cauchy stress and $\boldsymbol{\varepsilon}$ infinitesimal strain.

Strain energy is based on the deformation of SSE due to dendrite formation at (SE|SSE)-interface

$$\iint_{\Omega} f(a, \mathbf{u}; \lambda, \mu, \mathbf{d} \otimes \mathbf{d}) d\Omega$$

Surface energy is analysed based on the open crevice cracking at (SE|SSE)-interface affected by prescribed pressure

$$\iint_{\Gamma} f(a; \gamma) d\Gamma$$



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References

- [1] **T. Vo**, C. Hüter, S. Braun, M. Torrilhon, *Math. modelling for ASSB: (SE|SSE)-Interface*. Poster, Oxford Batt. Modelling Symp., University of Oxford, OBMS23, P.66, **2023**.
- [2] **T. Vo**, C. Hüter, S. Braun, M. Torrilhon, *Next-gen. All-solid-state Battery (#ASSB)*. Poster, SIAM Computational Science and Eng. Conference, CSE23, Amsterdam, **2023**.
- [3] **T. Vo**, *Math. modelling for ASSB*. Presentation, Numerical Modelling in Applied Physics with OpenFOAM Summer School, NUMAP-FOAM, University of Cambridge, **2022**.
- [4] **T. Vo**, C. Hüter, S. Braun, R. Spatschek, *Mathematical modelling for All-solid-state battery: Griffith criterion*. Doctoral presentation, IEK-2, Forschungszentrum Jülich, **2020**.
- [5] **T. Vo**, *Modeling the swelling phenomena of li-ion batt. cells based on a numerical chemo-mech. coupled approach*. Master thesis, Robert Bosch Battery Systems GmbH, **2018**.
- [6] **T. Vo**, A. Gallet-Segarra, C. Bertsch, *Integration of Modelica powertrain models into Hardware in the loop env.*. PreMaster, Robert Bosch GmbH, FEBER, EAM-P2695, **2015**.
- [7] **T. Vo**, *Simulation environment for NTC-based voltage drop reduction in Start/Stop appl. and its optimization*. Semiconductor. Bachelor thesis, Robert Bosch GmbH, **2014**.
- [8] **S. Braun**, C. Yada, A. Latz, *Thermodynamically consistent model for Space-Charge-Layer formation in a solid electrolyte*. J. Physical Chemistry C, 119, 22281-22288, **2015**.
- [9] **C. Hüter**, X. Yin, T. Vo, S. Braun, *A pragmatic dataset augmentation approach for transformation temp. prediction in steels*. Comp. Mat. Science, Vol. 176, 109488, **2020**.
- [10] **C. Hüter**, S. Fu, M. Finsterbusch, E. Figgemeier, L. Wells, and R. Spatschek, *Electrode-electrolyte interface stability in SSE system*. AIMS Materials Science, 4(4):867-877, **2017**.

Acknowledgments

T. Vo expresses sincere gratitude to the JARA-CSD research project, led by Dr. S. Braun and Dr. C. Hüter, for their crucial support. Special thanks to Prof. Dr. R. Spatschek for hosting at IEK-2, FZ Jülich. Moreover, T. Vo's role as a teaching assistant in the courses of Mathematische Grundlagen I, II, III, IV, and NumPDE at Computational Engineering Science (CES), RWTH Aachen University (2019-2023), was accomplished and enriched thanks to the guidance and mentorship of Prof. Dr. M. Torrilhon, Prof. Dr. M. Schlottke-Lakemper, Dr. R. Speck, Prof. Dr. B. Berkels, Dr. S. Braun, Prof. Dr. J. Kowalski, Dr. A. Jha, Prof. Dr. B. Stamm, Dr. A. Litvinenko, and Dr. M. Kirshhart.