

# MATHEMATICAL MODELLING FOR ALL-SOLID-STATE BATTERY: (SE|SSE)-INTERFACE

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## Mathematical modelling for the next-generation All-solid-state batteries: Nucleation (SE|SSE)<sup>(\*)</sup>-interface

**Rechargeable Lithium-ion battery** (LIB) is at the heart of every electric vehicle (EV), portable electronic device, and energy storage system [5]. Nowadays, LIBs enable human life more efficient and help to solve global environment issues thanks to EVs' zero emission. However, conventional LIB (c-LIB) is sensible to temperature and pressure, hence, flammable and explosive, which is undesirable. This bottleneck is mainly due to **liquid-based electrolyte** found in c-LIBs.

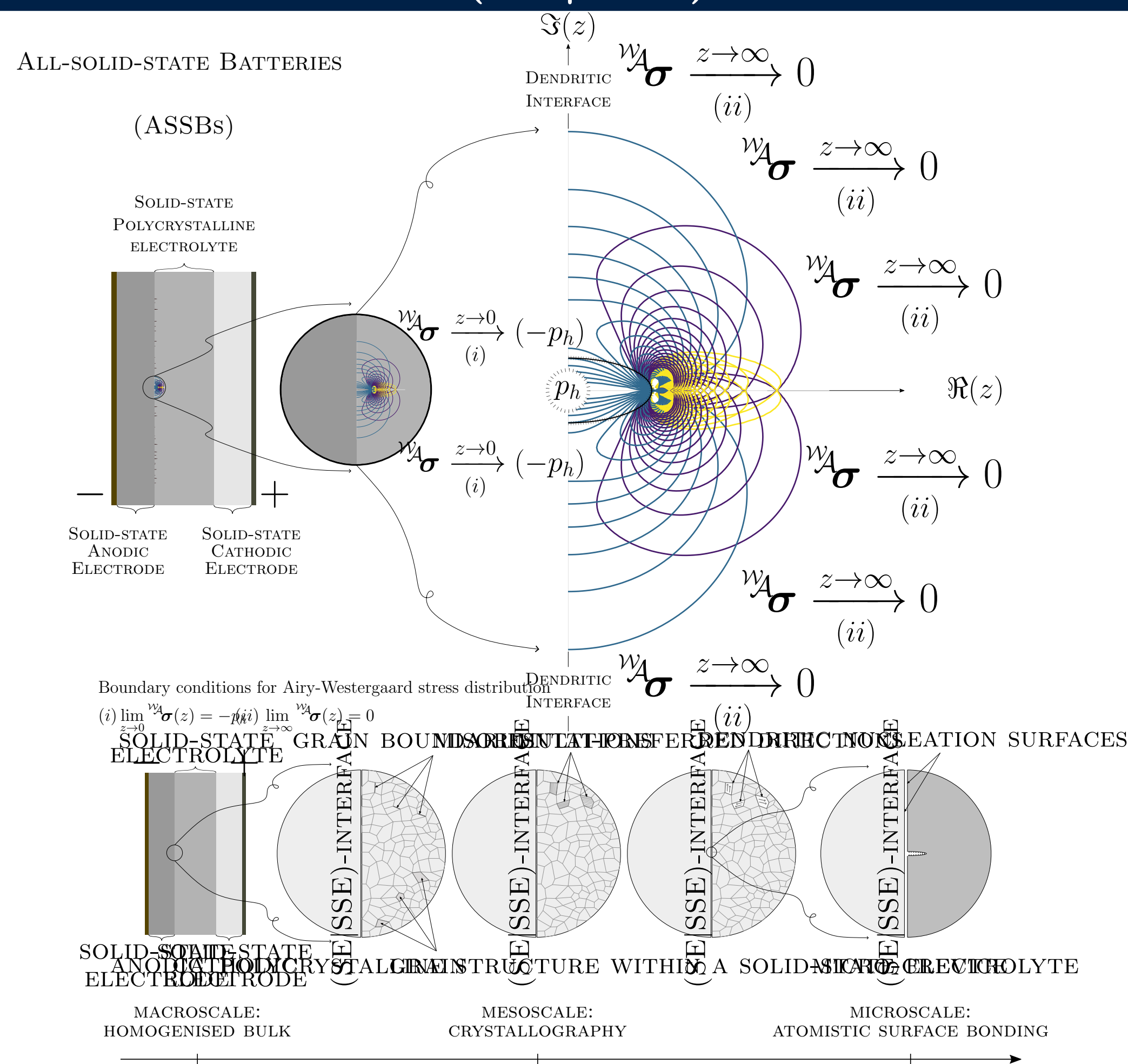
**All-solid-state battery** (ASSB) is one of promising candidates to overcome bottlenecks of c-LIBs. Thanks to **solid-state electrolyte** (SSE), ASSB is highly stable towards temperature and pressure. Nevertheless, Li-metal dendrite triggered at (SE|SSE)-interface [?] is the main drawback of ASSB since these dendritic threads extrapolate into SSE grain boundary network, causing crevice, degradation of ionic conductivity, and the probability of short-circuit, which is unfavorable.

**Next-generation All-solid-state battery** (ng-ASSB) with a consideration of **nucleation criterion** defined by

$$\partial_t \bar{\mathbf{u}} + \nabla \cdot \left( \mathbb{C} f_{\text{allocation}}(\lambda, \mu, \mathbf{d}_{G,i=1,\dots,N}^E; \mathbf{x}) : \nabla \mathbf{u}^{(s)} \right) + \rho \mathbf{b} = -\rho \nabla V_e, \quad (1)$$

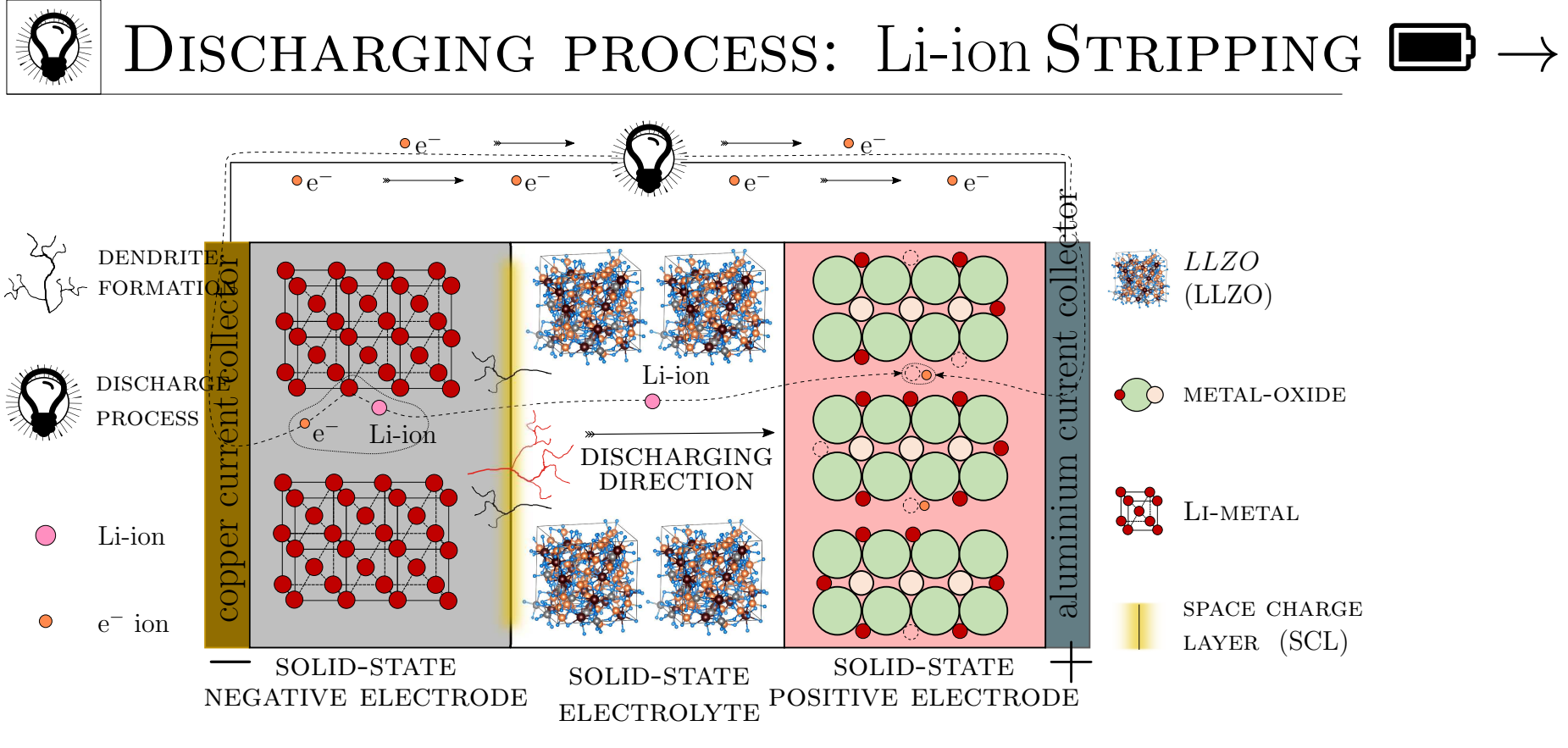
$$\text{s.t. } a_{\text{Griffith}} := a^* = \arg \min_{a \in \mathbb{R}} \iint_{\Omega} f(a, \mathbf{u}, \theta; \lambda, \mu, \mathbf{d}^{(*)} \otimes \mathbf{d}^{(*)}) d\Omega - \iint_{\Gamma} f(a; \gamma) d\Gamma \Big|_{\bar{\mathbf{u}}} \quad (2)$$

where  $V_e : \mathbb{R}^3 \rightarrow \mathbb{R}$  is the electric potential applied globally on ASSB. Due to nature setting of ASSB taking the form (SE|SSE|SE) the electric potential becomes uniform. Additionally,  $\mathbf{u}$  is the displacement field,  $\theta$  temperature field,  $a$  crevice length,  $\lambda, \mu$  Lamé constants,  $\mathbf{d}^{(*)} \otimes \mathbf{d}^{(*)}$  embedded misorientation structural tensor, and  $\gamma$  cracking-surface energy density, can help to improve ASSB performance.

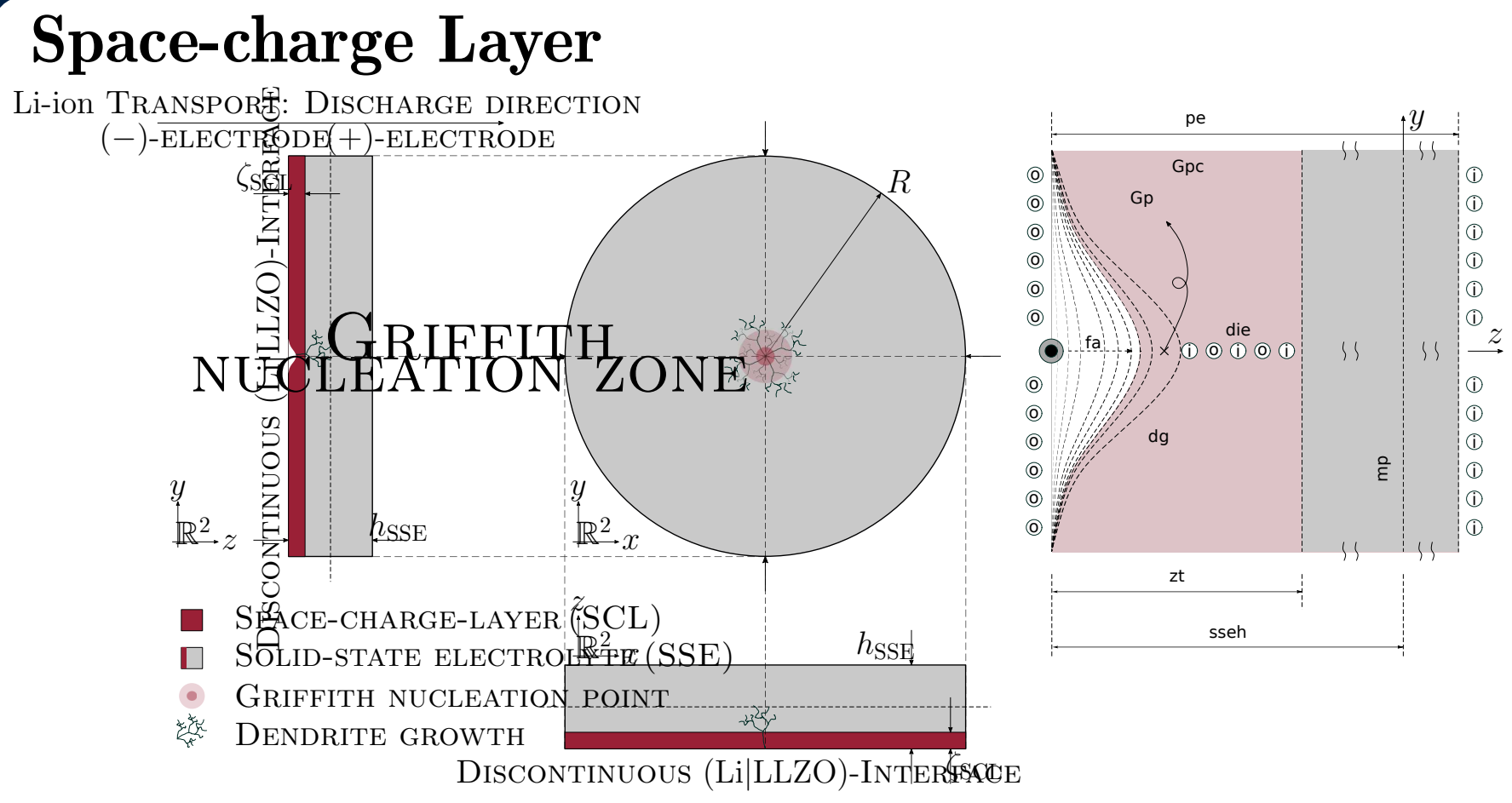


## Next-generation All-solid-state battery

**Nucleation** criterion governs the instable (SE|SSE)-interface [9]

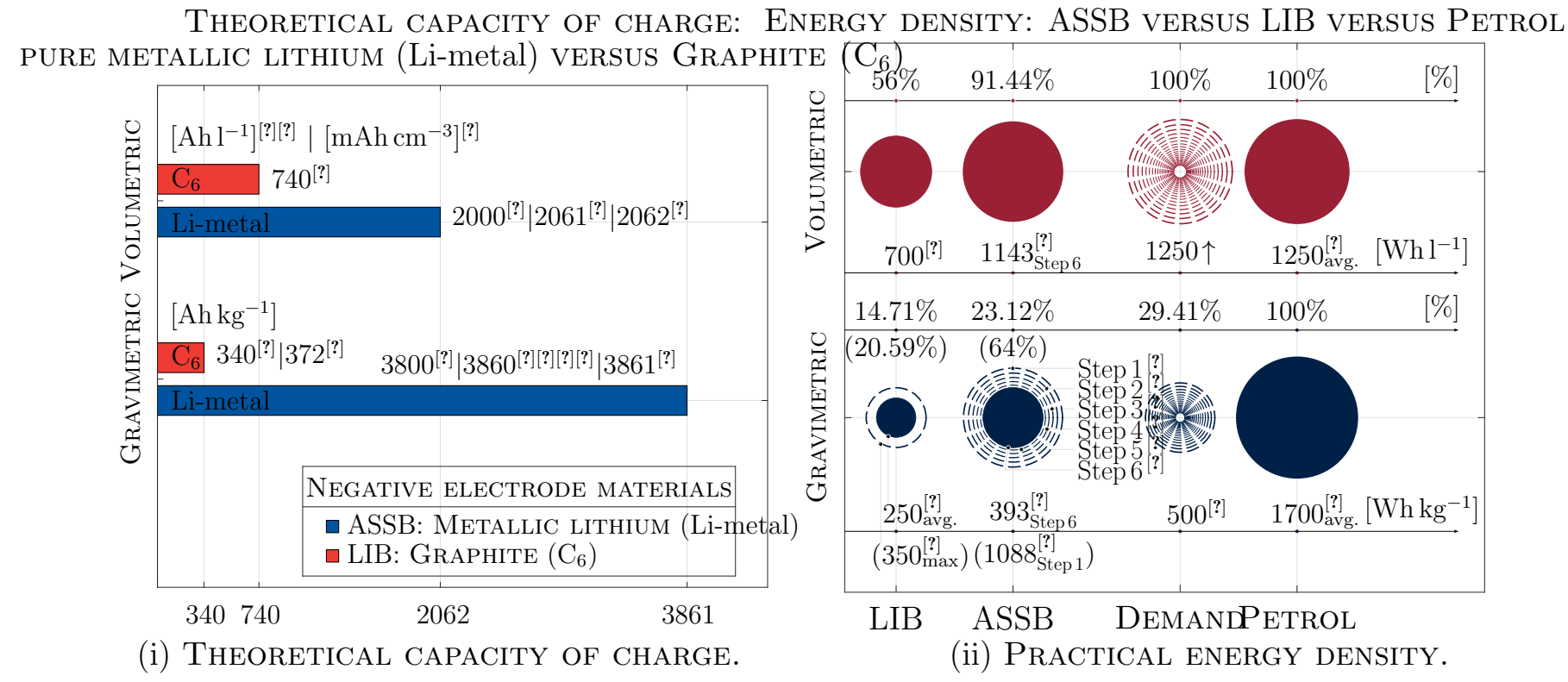


## Space-charge Layer



## Energy density demand landscape

**Interface** between solid electrode and solid-state electrolyte (SE|SSE) taking place at space charge layer (SCL) [7] critically exhibits mechanical and electrochemical instability [9].



## Artificial Neural Networks

Application: Steel property prediction [8]

## Semiconductor

Application: Start/Stop Starter [6]

## Nucleation interface: Taking place at the critically dendritic (SE|SSE)-interface

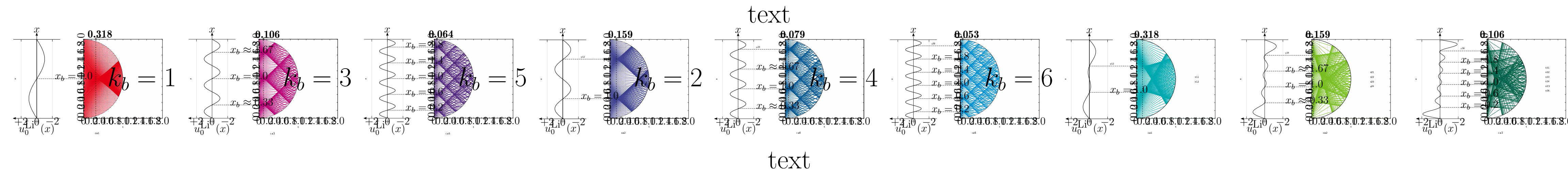
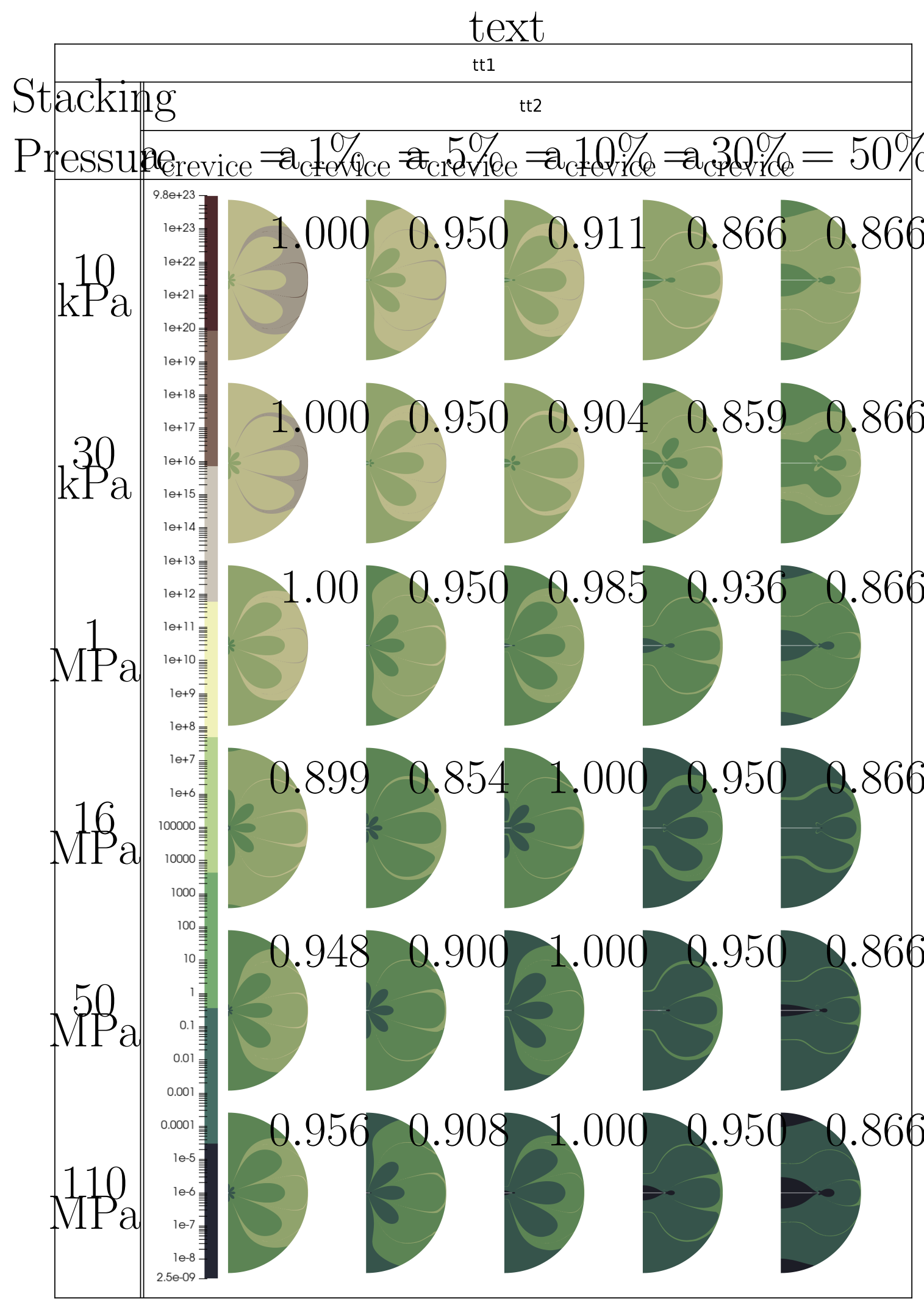
**Coupled fields** are Displacement field  $\mathbf{u}$  and temperature field  $\theta$ ;

$$\mathbf{u} : \begin{cases} \Omega \times \mathbb{R}_+ \rightarrow \mathbb{R}^3, \\ (\mathbf{x}, t) \mapsto \mathbf{u}(\mathbf{x}, t), \end{cases} \quad \theta : \begin{cases} \Omega \times \mathbb{R}_+ \rightarrow \mathbb{R}, \\ (\mathbf{x}, t) \mapsto \theta(\mathbf{x}, t), \end{cases}$$

Governing conservation equations used to describe balance of mass, conservation of linear momentum, conservation of angular momentum, and conservation of energy with  $\rho(\mathbf{x}, t)$  is mass density per unit volume (puv);  $\mathbf{b}(\mathbf{x}, t)$  body force puv;  $\mathbf{v}(\mathbf{x}, t)$  velocity;  $e(\mathbf{x}, t)$  internal energy puv;  $\mathbf{q}(\mathbf{x}, t)$  heat flux;  $r(\mathbf{x}, t)$  heat source puv;  $\boldsymbol{\sigma}$  Cauchy stress and  $\boldsymbol{\varepsilon}$  infinitesimal strain.

**Strain energy** is based on the deformation of SSE due to dendrite formation at (SE|SSE)-interface

**Surface energy** is analysed based on the open crevice cracking at (SE|SSE)-interface affected by prescribed pressure



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## References

- [1] **T.Vo**, C.Hüter, S.Braun, *Math. modelling for All-solid-state batt.: (SE|SSE)-Interface*. Poster, Oxford Batt. Modelling Symp., Univ. of Oxford, OBMS23, Page 66, **2023**.
- [2] **T.Vo**, C.Hüter, S.Braun, M.Torrilhon, *Mathematical modelling for All-solid-state batt.: (SE|SSE)-Interface*. Poster, SIAM Comp. Sci. and Eng. Conference, Amsterdam, **2023**.
- [3] **T.Vo**, *Mathematical modelling for All-solid-state batt.: Griffith criterion*. Presentation, NUMAP-FOAM Summer School, Univ. of Cambridge, **2022**.
- [4] **T.Vo**, C.Hüter, S.Braun, R.Spatschek, *Mathematical modelling for All-solid-state batt.: Griffith criterion*. Doctoral presentation, Forschungszentrum Jülich, **2020**.
- [5] **T.Vo**, *Modeling the swelling phenomena of li-ion batt. cells based on a numerical chemo-mech. coupled approach*. Master thesis, Robert Bosch Battery Systems GmbH, **2018**.
- [6] **T.Vo**, *Simulation environment for NTC-based voltage drop reduction in Start/Stop applications and its optimization*. Bachelor thesis, Robert Bosch GmbH, **2014**.
- [7] **S.Braun**, C.Yada, and A.Latz, *Thermodynamically consistent model for Space-Charge-Layer formation in a solid electrolyte*. Jr. Phys. Chem., 119, 22281-22288, **2015**.
- [8] **C.Hüter**, X.Yin, T.Vo, S.Braun, *A pragmatic dataset augmentation approach for transformation temp. prediction in steels*. Comp. Mat. Science, Vol. 176, 109488, **2020**.
- [9] **C.Hüter**, S.Fu, M.Finsterbusch, E.Figgemeier, L.Wells, and R.Spatschek, *Electrode-electrolyte interface stability in solid state electrolyte system: influence of coating thickness under varying residual stresses*. AIMS Materials Science, 4(4):867-877, **2017**.
- [10] **M.Torrilhon**, *Modeling nonequilibrium gas flow based on moment equations*. Annual Review of Fluid Mechanics, 48(1):429-458, **2016**.

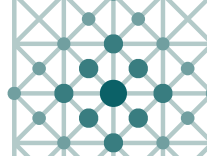


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