# Next-generation all-solid-state battery (#ASSB)

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### Mathematical modelling for the next-generation All-solid-state batteries: Nucleation (SE|SSE)<sup>(\*)</sup>-interface

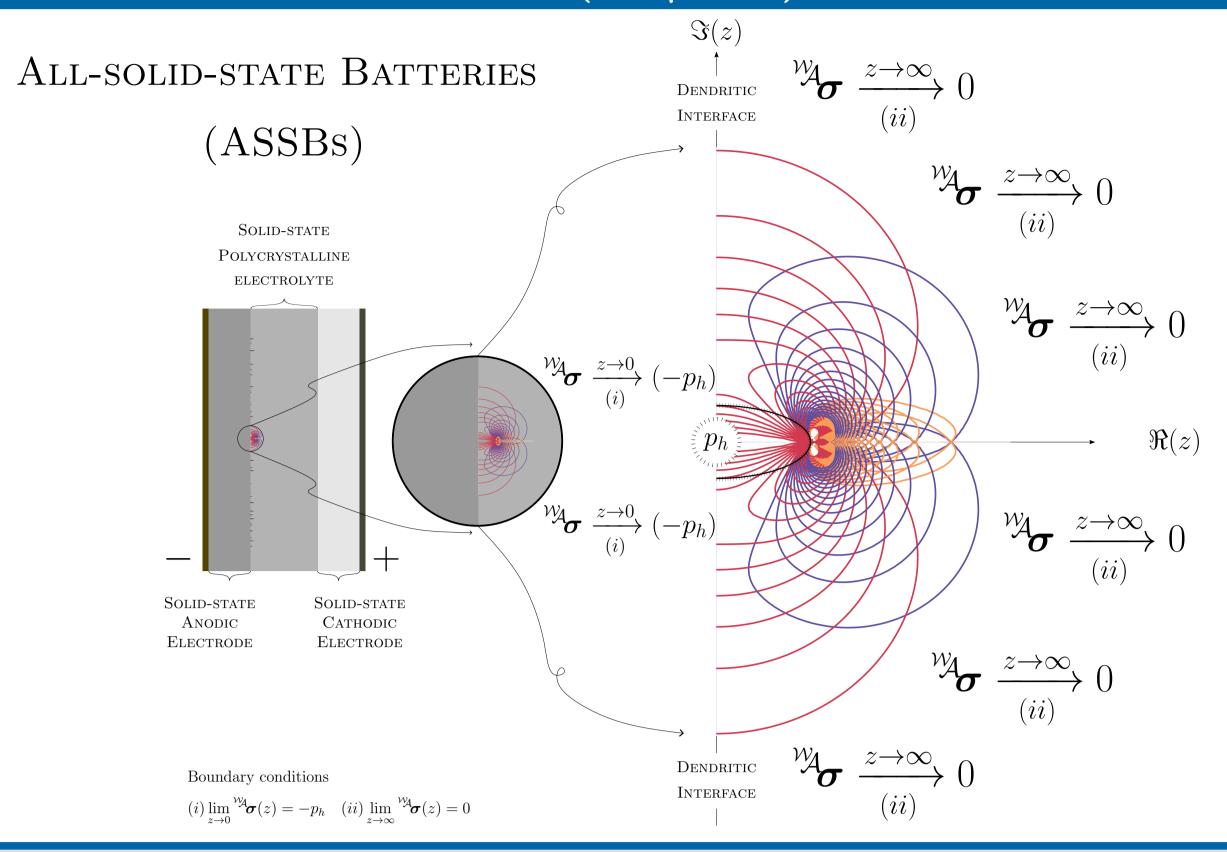
Rechargeable Lithium-ion battery (LIB) is at the heart of every electric vehicle (EV), portable electronic device, and energy storage system [1]. Nowadays, LIBs enable human life more efficient and help to solve global environment issues thanks to EVs' zero emission. However, conventional LIB (c-LIB) is sensible to temperature and pressure, hence, flammable and explosive, which is undesirable. This bottleneck is mainly due to liquid-based electrolyte found in c-LIBs.

**All-solid-state battery** (ASSB) is one of promising candidates to overcome bottlenecks of c-LIBs. Thanks to solid-state electrolyte (SSE), ASSB is highly stable towards temperature and pressure. Nevertheless, Limetal dendrite triggered at (SE|SSE)-interface [5] is the main drawback of ASSB since these dendritic threads extrapolate into SSE grain boundary network, causing crevice, degradation of ionic conductivity, and the probability of short-circuit, which is unfavorable.

Next-generation All-solid-state battery (ng-ASSB) with a consideration of nucleation criterion defined by

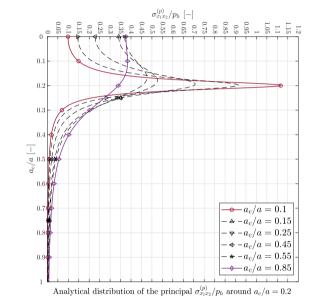
$$a_{ ext{Griffith}} := a^* = \arg\min_{a \in \mathbb{R}} \left. \iint_{\Omega} f(a, \boldsymbol{u}, \theta; \lambda, \mu, \boldsymbol{d} \otimes \boldsymbol{d}) \, d\Omega - \left. \iint_{\Gamma} f(a; \gamma) \, d\Gamma \right|_{\boldsymbol{u}^{(s)}}$$

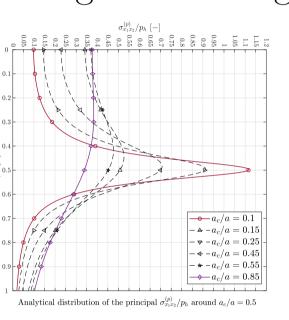
where  $\boldsymbol{u}$  displacement field,  $\theta$  temperature field, a crevice length,  $\lambda, \mu$  Lamé constants,  $\boldsymbol{d} \otimes \boldsymbol{d}$  embedded misorientation structural tensor, and  $\gamma$  cracking-surface energy density, can help to improve ASSB performance.

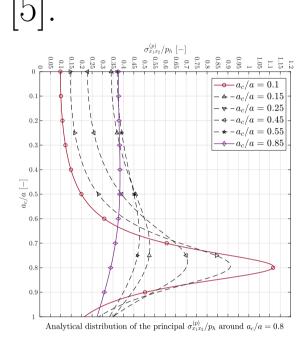


### Interface Analysis

Interface between solid electrode and solid-state electrolyte (SE|SSE) taking place at space charge layer (SCL) [2] found in ASSBs critically exhibits mechanical and electrochemical instability [3]. This evidence points directly to the fact that the soft metallic li anode is erroneously prone to triggering dendrites, under cycles of electric charge & discharge [5].



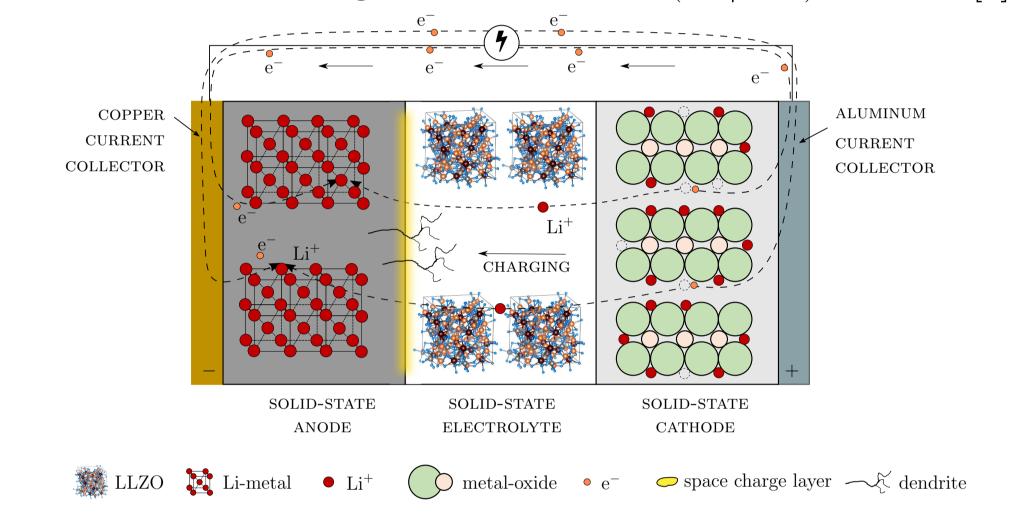




<u>Distribution</u>: ana. max. shear stress  ${}^{\mathcal{W}}\!\!\sigma_{x_1x_2}^{\Pi}$  around crack tip  $a_c$ .

### Next-generation All-solid-state battery

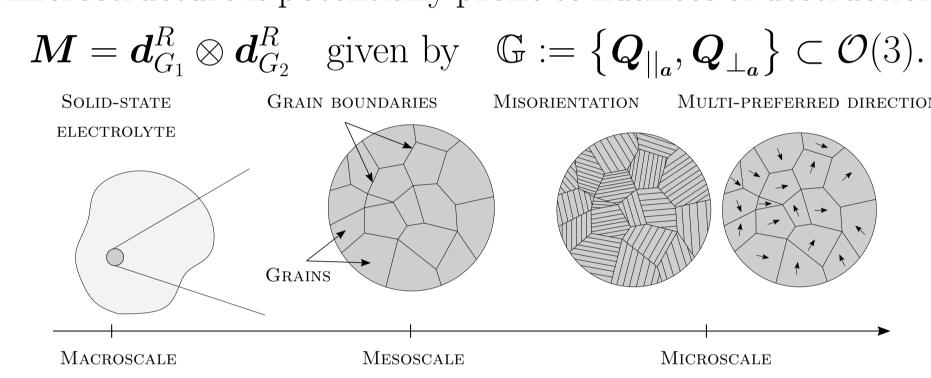
**Nucleation** criterion governs the instable (SE|SSE)-interface [3]



**Thermodynamic consistency** is satisfied, followed by [2].  $\checkmark$  Closure  $\Omega$  is fulfilled by 15 moments, followed by [4].

# Embedded structural-tensor SSE

Polycrystalline garnet-type SSE [5] such as LLZO exhibit grain boundary network, and grains with variation of {size, shape} under microscopic observation. Hence, this microstructure is potentially prone to nuances of destruction.



Consequentially, dendrites contribute to degradation of ionic conductivity and tiny-cracks tracing along grain boundaries.

## Nucleation interface: Taking place at the critical dendritic interface

Coupled fields: Displacement vector field and temperature scalar field

$$\boldsymbol{u}: \begin{cases} \Omega \times \mathbb{R}_{+} \to \mathbb{R}^{3}, \\ (\boldsymbol{x},t) \mapsto \boldsymbol{u}(\boldsymbol{x},t), \end{cases} \quad \theta: \begin{cases} \Omega \times \mathbb{R}_{+} \to \mathbb{R}, \\ (\boldsymbol{x},t) \mapsto \theta(\boldsymbol{x},t), \end{cases} \quad \theta: \begin{cases} \Omega \times \mathbb{R}_{+} \to \mathbb{R}, \\ (\boldsymbol{x},t) \mapsto \theta(\boldsymbol{x},t), \end{cases}$$

Governing conservation equations

$$\frac{d}{dt} \int_{\Omega} (\cdot) \ d\Omega = \int_{\Omega} (\cdot)^{\text{action}} \ d\Omega + \int_{\partial \Omega} (\cdot)^{\text{action}} \ d\partial\Omega + \int_{\Omega} (\cdot)^{\text{production/source/sink}} \ d\Omega$$

 $\rho(\boldsymbol{x},t)$  is mass density per unit volume (puv);  $\boldsymbol{b}(\boldsymbol{x},t)$  body force puv;  $\boldsymbol{v}(\boldsymbol{x},t)$  velocity;  $e(\boldsymbol{x},t)$  internal energy puv;  $\boldsymbol{q}(\boldsymbol{x},t)$  heat flux;  $r(\boldsymbol{x},t)$  heat source puv;  $\boldsymbol{\sigma}$  Cauchy stress and  $\varepsilon$  infinitesimal strain. Helmholtz energy functional

$$a_{\text{Griffith}} := a^* = \arg\min_{a \in \mathbb{R}} \left. \iint_{\Omega} f(a, \boldsymbol{u}; \lambda, \mu, \boldsymbol{d} \otimes \boldsymbol{d}) \, d\Omega - \left. \iint_{\Gamma} f(a; \gamma) \, d\Gamma \right|_{\boldsymbol{u}^{(s)}}$$

Governing PDE

$$a_{ ext{Griffith}} := a^* = \arg\min_{a \in \mathbb{R}} \left. \iint_{\Omega} f(a, \boldsymbol{u}; \lambda, \mu, \boldsymbol{d} \otimes \boldsymbol{d}) \, d\Omega - \left. \iint_{\Gamma} f(a; \gamma) \, d\Gamma \right|_{\boldsymbol{u}^{(s)}}$$

abc

Strain energy: Interface between solid electrode and solid-state electrolyte (SE|SSE) taking place at space charge

 $\iiint_{\Omega} f(a, \boldsymbol{u}; \lambda, \mu, \boldsymbol{d} \otimes \boldsymbol{d}) d\Omega$ 

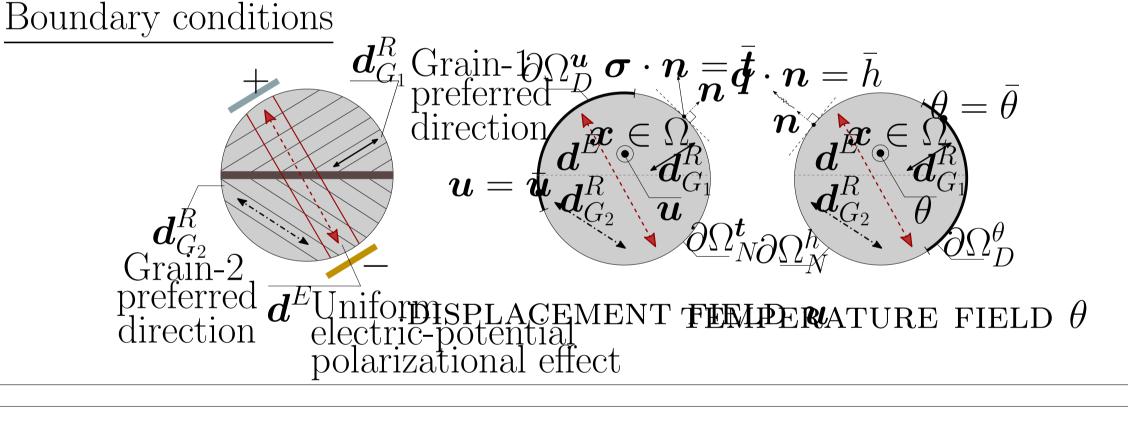
Interface between Surface energy: solid electrode and solid-state electrolyte (SE|SSE) taking place

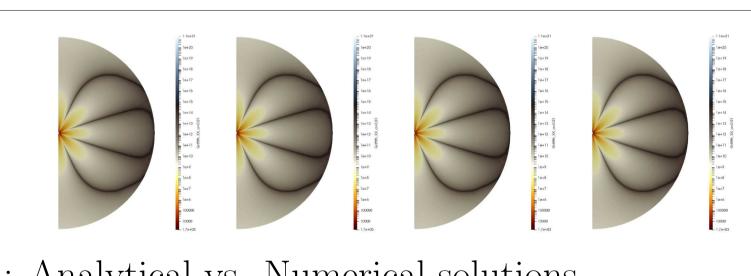
$$\iint_{\Gamma} f(a;\gamma) \, d\Gamma$$

Therefore

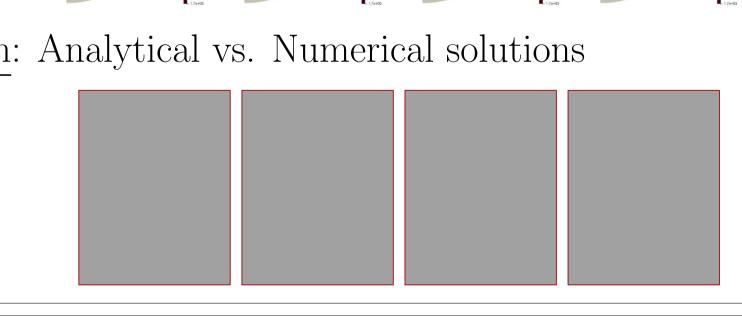
abc

$$\rho \, \partial_{t^2}^2 \boldsymbol{u}^{(s)} + \nabla \cdot \left( \stackrel{4}{\mathbb{C}} f_{(\lambda,\mu)}^{\mathbb{D}(\Omega)} : \nabla \boldsymbol{u}^{(s)} \right) + \rho \nabla V_e = \boldsymbol{0},$$
s.t.  $a_{\text{Griffith}} := a^* = \arg\min_{a \in \mathbb{R}} \left. \iint_{\Omega} f(a, \boldsymbol{u}; \lambda, \mu, \boldsymbol{d} \otimes \boldsymbol{d}) \, d\Omega - \left. \iint_{\Gamma} f(a; \gamma) \, d\Gamma \right|_{\boldsymbol{u}^{(s)}}$ 





Comparison: Analytical vs. Numerical solutions



 $\varepsilon_{ij} = \frac{1}{2} \left( u_{i,j} + u_{j,i} \right)$  $\sigma_{ij} = \mathbb{C}^{f^{GL}}_{ijkl}(y) \; \varepsilon_{kl}$ Strain energy density  $\mathcal{E}_{ ext{strain}} := \frac{1}{2} \sigma_{ij} \varepsilon_{ij}$ abc

FEM: Strain energy density

Partial differential equation

 $\left| \nabla \cdot \left( \mathbb{C}^{f^{GL}}(\boldsymbol{y}) \nabla_{s} \boldsymbol{u} \right) + \rho \boldsymbol{b} = 0 \right|$ 

Displacement solution

Airy-Westergaard function used for max. shear stress analysis

$$\mathcal{V}\!\!\mathcal{A}: \mathbb{C} \to \mathbb{C}, z \mapsto \mathcal{V}\!\!\mathcal{A}(z) := \Re(\iint_{\Gamma} \mathcal{K}^{(\star)} dz) + x_2 \Im(\oint_{\Gamma} \mathcal{K}^{(\star)} dz), \mathcal{K}^c(z) := -p_h + p_h/\sqrt{1 - a^2/z^2},$$

where  $\{p_h, a\} \in \mathbb{R}_+$  is the.

FEM implementation: element matrix  $\mathbf{K}^e$  approx. by Gauss quadrature; indices imply 4+2=6 for-loop:

$$K_{ik}^{e^{\alpha\beta}} = \int_{\Omega^{\xi}} \left( \mathcal{L}_{1}^{\alpha} \, \mathbb{C}_{i1k1}^{f^{GL}}(y) \, \mathcal{R}_{1}^{\beta} + \mathcal{L}_{1}^{\alpha} \, \mathbb{C}_{i1k2}^{f^{GL}}(y) \, \mathcal{R}_{2}^{\beta} + \mathcal{L}_{2}^{\alpha} \, \mathbb{C}_{i2k1}^{f^{GL}}(y) \, \mathcal{R}_{1}^{\beta} + \mathcal{L}_{2}^{\alpha} \, \mathbb{C}_{i2k2}^{f^{GL}}(y) \, \mathcal{R}_{2}^{\beta} \right) \det(\boldsymbol{J}) \, d\Omega^{\xi}$$

where  $\mathcal{L}_i^{\alpha}$  and  $\mathcal{R}_l^{\beta}$  are gradients of basis functions at node  $\alpha^{th}$  and  $\beta^{th}$ , respectively.

#### Contact

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### References

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