

1.8

解:

$$(1) n-1 \quad (2) n-1 \quad (n=1 \text{ 时, 为 } 1) \quad (3) n-1$$

$$(4) n + (n-1) + (n-2) + \dots + 1 = \frac{n(n+1)}{2} \quad (\text{从 } i=1 \text{ 开始})$$

$$(5) 1 + (1+2) + (1+2+3) + \dots + (1+2+3+\dots+n) = \sum_{i=1}^n \frac{i(i+1)}{2} =$$

$$\frac{1}{12} n(n+1)(2n+1) + \frac{1}{4} n(n+1) = \frac{1}{6} n(n+1)(n+2)$$

$$(6) n$$

$$(7) \lfloor \sqrt{n} \rfloor \quad \text{向下取整}$$

$$(8) 1100$$

1.10 按增长率由小至大的顺序排列下列各函数:

$$2^{100}, \left(\frac{3}{2}\right)^n, \left(\frac{2}{3}\right)^n, \left(\frac{4}{3}\right)^n, n^n, n^{\frac{3}{2}}, n^{\frac{2}{3}}, \sqrt{n}, n!, n, \log_2 n,$$

$$\frac{n}{\log_n 2}, (\log_2 n)^2, \log_2(\log_2 n), n \log_2 n, n^{\log_2 n}$$

解

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$$\left(\frac{2}{3}\right)^n, 2^{100}, \log_2(\log_2 n), \log_2 n, (\log_2 n)^2, \sqrt{n}, n^{\frac{2}{3}}, n,$$

$$\frac{n}{\log_n 2} = n \log_2 n, n^{\frac{3}{2}}, n^{\log_2 n}, \left(\frac{4}{3}\right)^n, \left(\frac{3}{2}\right)^n, n!, n^n$$

1.12

解: (1) 对 (2) 对 (按定义来) (3) 错 (4) 对 (5) 错