

From Toy to Cosmic: QFD CMB Spectra Anchored to Planck Observables

Planck-Anchored Inputs

Quantity	Symbol	Value / Definition
Acoustic scale	θ_A	≈ 301 (Planck 2018)
Characteristic ψ scale	r_ψ	≈ 147 Mpc (identified with a fundamental modulation length)
Implied comoving distance	$\chi^* = \theta_A r_\psi / \pi$	≈ 14084 Mpc
Tilt	n_s	≈ 0.96 (Planck-like)
Reionization optical depth	τ	≈ 0.054 (sets low- ℓ EE bump amplitude)
Lensing smoothing width (phenom.)	σ_ℓ	≈ 60

Key Equations

Photon–photon depth: $d\tau = a(\eta) \sigma_{\text{vis}} n_{\text{vis}}(\eta) n_{\text{radio}}(\eta) c d\eta$

Visibility: $g(\eta) = - d\tau/d\eta \cdot \exp(-\tau)$

Fundamental power: $P_\psi(k) = A k^{n_s-1} [1 + A_{\text{osc}} \cos(k r_\psi) \exp(-(k \sigma_{\text{osc}})^2)]^2$

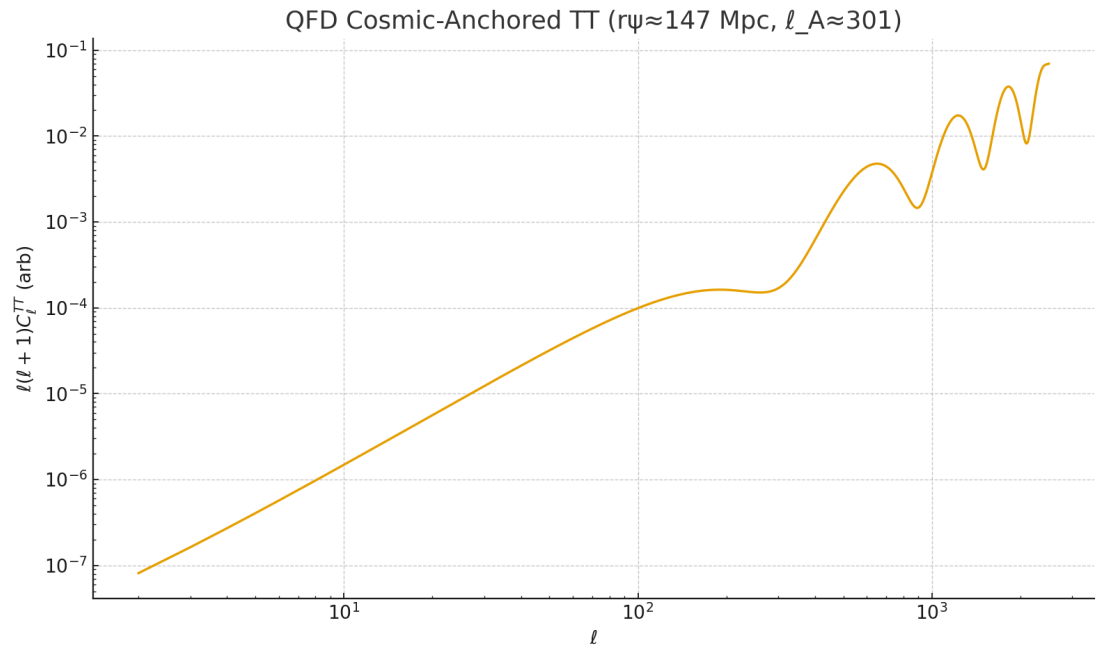
Projection (Limber-like, high- ℓ): $C_\ell \approx \int d\chi [W(\chi)^2/\chi^2] P_\psi((\ell+1/2)/\chi)$

Full line-of-sight (schematic): $\Theta_\ell(k) = \int d\eta S_T(k,\eta) j_\ell(k\eta\theta_A)$, $E_\ell(k) = \int d\eta S_E(k,\eta) \dots$

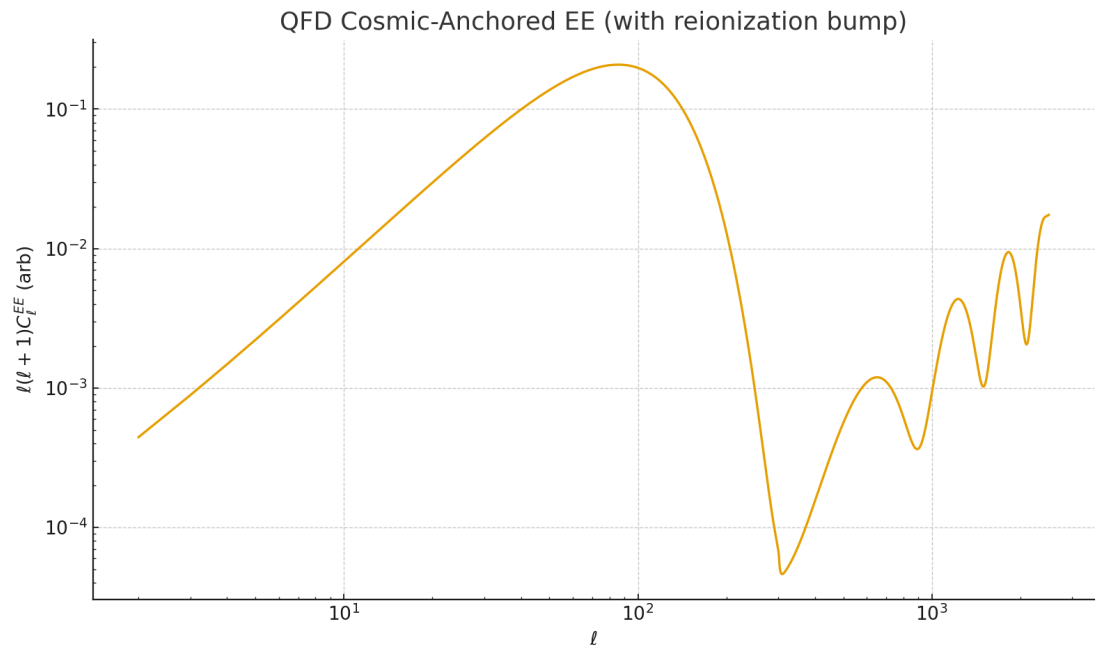
Peak-spacing relation: $\Delta\ell \approx \theta_A \approx \pi \chi^* / r_\psi \Rightarrow r_\psi \approx \pi \chi^* / \theta_A$

Cosmic-Anchored Spectra

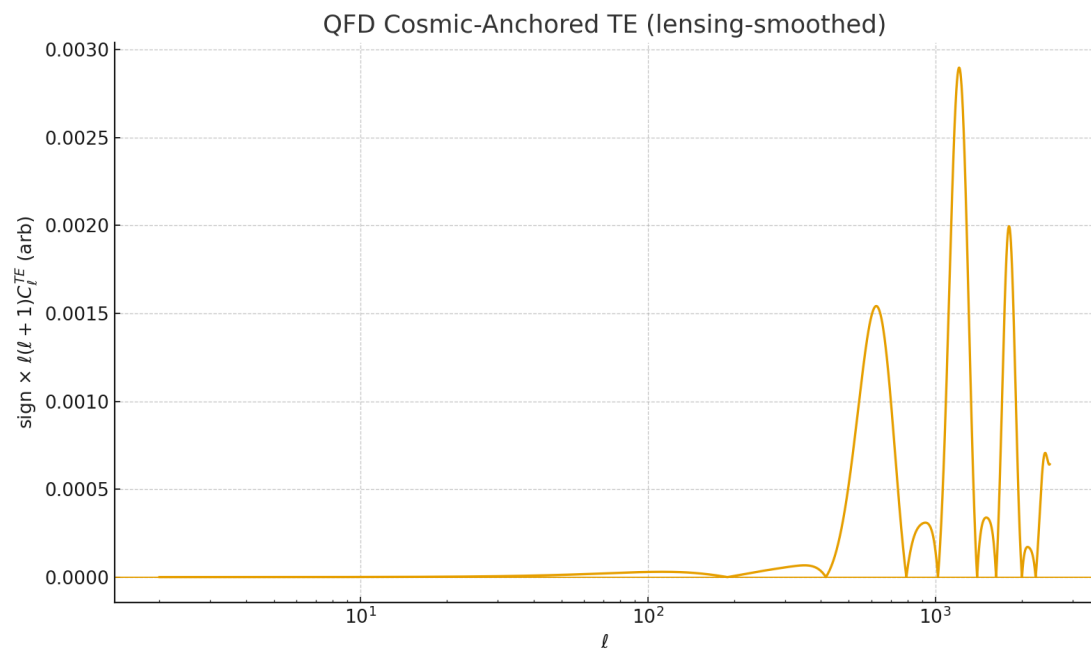
TT Spectrum



EE Spectrum (with reionization bump)



TE Spectrum (sign shown)



Λ CDM vs QFD- $\gamma\gamma$ (Recap)

Aspect	Λ CDM / Inflation	QFD with $\gamma\gamma$ scattering
Peak spacing origin	$\theta^* = r_s / D_M \Rightarrow \ell_A \approx \pi/\theta^*$	$\Delta\ell \approx \pi \chi^* / r_\psi \Rightarrow r_\psi \leftrightarrow \text{modulation length}$
Polarization	Thomson kernel	\sin^2 kernel (same quadrupole geometry)
Low- ℓ EE	Reionization (τ)	Reionization (τ), same geometry
Lensing	Peak smoothing + B from lensing	Same lensing phenomenology applied post-projection
BAO link	r_s imprints BAO	