## CHAPTER 2

**LITERATURE REVIEW**

## 2.1 REVIEW IN THE LITERATURE

**Kim BH, Choi BK and El-Midany et al.[1]** compared the machining time for direction- and contour-parallel paths by considering the feed rate acceleration and deceleration. In both researches, the machining times for different direction- and contour-parallel paths were compared by using a linear feed rate acceleration/deceleration model. El-Midany et al. concluded that the selection of the optimal path topology depends on the geometry of the surface’s boundary and the cutting conditions. Kim and Choi mentioned that although pure zigzag path (with sharp corners) results in a longer machining time compared to contour parallel path, it is practically preferred to contour parallel in die and mold machining because of enhanced constant cutting loads.

An investigation of optimal path pattern selection for layer by-layer rough cutting has been carried out by **Li H. et al [2] (1994).** In this method, the optimal path topology for each layer was selected by fuzzy pattern analysis among a variety of topologies in a path topology database. So for each roughing process, more than one pattern could be selected to machine all layers based on the geometry of these layers.

**Cox JJ et al. (1994)** **[3]** introduced the space filling curves (SFCs) for finish tool path generation of free form surfaces considering that parallel or spiral line pattern is not the best way of traversing the tool in an area. They used truncated Palmer’s and Moore’s curves to avoid overlapping and crossing points in the generated tool paths. However this truncation method doubles the number of lines to be traversed and sharp edges still remain in the tool paths.

In the research by Han ZL et al. (2001), a free form surface was approximated by a ruled surface based on the isophote method. Iso-inclination curves were used as generators for the ruled surface and also as the boundary curves for the tool path generation.

Choi BK et al. (1997) and Morishige et al. (1997) employed the configuration space (C-space) technique in tool path generation. The configuration space (C-space) of a rigid object with a certain degrees of freedom is defined as the space of the parameters corresponding to the degrees of freedom. Each point in the C-space represents one configuration. By considering the design tolerance and mapping the obstacles corresponding to the local and global gouges in the C-space, the problem of tool path planning can be converted into the problem of planning the movements of a point in the C-space. The 2D C-space of the tool at the CC point is constructed by only considering two orientation parameters of the tool (α and ω) and removing the configurations with collision from the available space. Then the optimal parameters are selected in the C-space based on the maximum .machining efficiency.

Hosseinkhani Y. et al. (2007) developed a method called the penetration–elimination method (PEM) for rear gouging avoidance. Similar as RBM and AIM, the PEM is only applicable to open face collision-free areas. A new concept for gouge quantification was introduced based on radial and axial depths of gouge. If a point is inside the tool area, it is assigned a negative radial depth of gouge. The gouging intensity function is defined as the multiplication of radial and axial depths of gouge. Hence, a point in the gouge area has a negative gouge intensity value. The penetration–elimination is conducted by incremental checking of the tool shadow area and adjusting the tilt angle, while each time the points calculated with positive gouge intensity values are deleted from the checking seed points. Together with an optimized root finding method, this method greatly reduces the calculation time by dynamically removing the safe areas out of the calculation loop.

Approximation of rear gouging area by a quadric surface has been used by Fan Jet al. (2008) for the tool orientation in 5-axis machining. A major advantage is the computational efficiency of fitting and distance calculation and the applicability to implicit, polyhedral and point based surfaces. However the required sample point patterns exaggerate the gouge prone area under the tool shadow, and hence increase the time of gouge checking. Another group of methods tends to locate the work piece in a few setups by using tilt/rotary tables. Note that this is different from 5-axis machining when the tool rotations are controlled by the machine table. In these methods, setups are generated based on partitioning the surfaces into a few areas and then machining by a multi-axis machine. This partitioning process has been conducted by the shape classification and machinability in, accessibility domain analysis in and G-map (Gaussian map) based area normal matching. Then tool orientation is adjusted in every setup by tilt/rotary table to machine with 3, 3 1/2 1/2, or 4 axis NC machine.

**Shuai He a, et al [1]** This work establishes an accurate freeform surface topography model considering geometric errors, tracking errors, and cutting forces. Regarding geometric errors, based on the theory of multibody systems and homogeneous coordinate transformation, the transfer relationship between various geometric errors and the tool error in the workpiece coordinate system is described. Using the continuous acceleration Position-Velocity-Time (PVT) interpolation method, the offset discrete points caused by geometric errors are interpolated and rediscretized, and the accurate mathematical model between the tool errors (position and posture) in the workpiece coordinate system and the topography of the freeform surface is established. Based on the model, the influence of geometric errors on the contour errors of freeform surfaces is accurately calculated, and the contribution and similarity of the effects of various geometric errors on the contour errors of freeform surfaces are analyzed. For dynamic-dependent factors, a second-order system with two degrees of freedom on the X or Z axis is established. According to the simplified result of the equivalent system, the contour error of the freeform surface caused by the tracking error and cutting force is analyzed. For the tracking error, under the condition of constant rotation velocity of the spindle, the change of the slope of the freeform surface along the circumferential direction causes the change in the velocity and acceleration of the motion axis; thus, the corresponding area of the surface has a larger contour error. For cutting force, the change of the slope of the freeform surface along the circumferential direction changes the tool working rake angle, the tool working clearance angle, and the shearing angle, resulting in a change in the cutting force. Moreover, the change of cutting speed is accompanied by the change of cutting force. An experiment verifies the effectiveness of the proposed modeling method. In addition, the modeling method provides an effective solution for the calculation of the contribution rate of different error sources to the contour error of the freeform surface.

**P J Scott2 et al, [2]** The specification and characterisation of freeform surfaces is immature: many CAD packages only allow the nominal freeform geometry to be specified. To control manufacturing and function, the allowable geometric variability also needs to be specified. Currently International standards specify allowable geometry through geometrical tolerancing. Geometrical tolerancing has proved to be a very blunt instrument with many cases, particularly in the aerospace and biomedical industries, of failure of the function of freeform surfaces due to inadequate specification. The paper begins by discussing the importance of the decomposition of the surface geometry into different scales for both specification and characterisation. The three main types of geometrical decomposition: linear, morphological and segmentation are briefly discussed. The Laplace-Beltrami operator (LBO) is the generalization of the Laplace operator to manifolds (i.e. freeform surfaces). By taking Eigenfunctions/Eigenvalues of the LBO a spectral decomposition of the freeform geometry can be realized. The Eigenfunctions are called manifold harmonics and are a direct generalization of Fourier harmonics for freeform surfaces. Tolerancing the Eigenfunctions provides a very powerful and flexible system to control geometrical variability of freeform surfaces; extending the geometrical tolerancing system by allowing decomposition of the geometrical shapes within tolerance zones. Further a generalized Gaussian filter can also be realized by Gaussian weighting the LBO spectra and reconstructing the weighted Eigenfunctions.

**Xinyu Liu et al [3],** A data point calculation method that does not require the use of Fermat′s principle and a simple and general design method of starting points of freeform off-axis multi-mirror optical systems are proposed in this paper, which aim to promote the realization of high-performance reflective systems containing freeform surfaces. Taking a planar system and the required parameters as the input, a good starting point for a freeform off-axis multi-mirror system can be automatically obtained using the proposed method. The design of a freeform off-axis five-mirror system with a low F-number is taken as an example to show the effectiveness of the proposed method. The method can also be used for the design of freeform reflective systems with other numbers of mirrors.

**Hongxiang Pan et al [4]**, In this paper, a method of how to construct a freeform surface directly in an off-axis reflective image system is proposed. The method includes both the seed curve extension algorithm and simulated annealing algorithm. Firstly, the sample points on the unkown freeform surface were be obtained quickly by the seed curve extension algorithm. Then the continuity of the freeform surface is evaluated by calculating the angle between the normal vectors at the adjacent sample points. At last the freeform surface was fitted to an extended polynomials using simulated annealing algorithm. The method is employed to construct a freeform surface directly which is used as a primary mirror in an initial layout of an off-axis two-mirror system.

**Damian Groch et al [5],** The presented method is introduced to simulate and predict the accuracy of fitting two freeform surfaces. For this purpose, the CAD models of both actual surfaces should be determined on the basis of coordinate measurement data obtained in measurements along regular grids of points in the UV space. The NURBS regression surfaces are modeled on the measurement data. Adequate regression models are sought with the iterative procedure. In the following steps of the procedure, the number of control points and/or the degree of the surface is/are changed, and the autocorrelation of residuals from the models is tested using the spatial statistics methods. The designated models are optimal CAD representations of the actual surfaces. Tests of the accuracy of fitting the surfaces are carried out virtually by fitting together both models in the CAD software. The outcome of the study is a spatial model of the gap between the studied surfaces. The obtained model was verified experimentally by measuring the dimensions of the actual gap between the surfaces, applying a measuring microscope. The proposed method is a useful tool in analyzing and improving the accuracy of injection molds machining.

**Haoyu Lyu et al,[6]** Conjunctive multi-freeform surfaces play an important role in many advanced optical systems. The position and posture accuracy of freeform surfaces are the key to system performance. However, there is no effective method of measuring the positions and postures of multiple freeform surfaces. In this study, a conjunctive multi-freeform surface measurement system based on multi-sensors is developed, and a trust region registration based on the least squares method is proposed, with the aim of registering multiple freeform surfaces at different positions and postures. The performance of the proposed system was analyzed and the errors were calibrated. The calculation accuracy of the registration method was within 20 nm at Φ50 mm in terms of root-mean-of-squares (RMS) values. The positioning accuracy of the freeform surface measurement system proved to be 1.2 μm within the area of 120 mm × 120 mm; the related uncertainty was also analyzed. The proposed measurement approach provides a comprehensive solution to optical conjunctive multi-freeform surfaces.

**Wei Zhang\* et al [7],** This paper constructs a small-scale, lightweight structure with complex freeform surfaces via parametric

design. First, the method of freeform surface modelling and parametric design were introduced, and combined

into the parametric design aided freeform surface modelling. Then, the parametric design and software for complex surface structure were determined. On this basis, the small-scale structure was conceptualized and the model was improved in the design phase. The PP sheet was selected as the final simulation material and the model was established according to the specified method. The stress deformation of the structure was simulated to correct the stress defects in the design, while the airflow impact was simulated to verify the rationality of the structural form. The results show that the parametric design helps apply complex freeform nsurface to small and light structure and assist the generation of the designed form. The research findings shed new light on the application of parametric design in the field of structure.

**Julius Muschaweck [8]** Tailoring freeform surfaces for illumination with point sources is an established method to generate near-arbitrary illuminance distributions with high detail using a single freeform surface. Real, non-laser sources are not point sources, however. Replacing a point source in a tailored freeform system with an extended source blurs the point-source distribution. Accordingly, extended sources are often treated as a perturbation within a pointsource tailoring algorithm, which may work well for small sources. However, important applications like street lighting, wall-washing and automotive front lighting require some peak intensity in certain directions, which can only be achieved with a given source luminance when nearly the whole aperture contributes to that peak intensity. Then, the tenet of point source tailoring – a one-to-one relation of surface points to target points – breaks down. In this paper, we embrace extended sources instead of treating them as a perturbation: Illuminance at several target points is computed by integrating the luminance of the virtual source image over its finite projected solid angle in a noise-free, non-Monte-Carlo way. The freeform surface is parametrized; the shape of the distorted virtual source image, and thus the illuminance at the target points, becomes a function of the freeform surface parameters, leading to a system of nonlinear equations, which are solved iteratively. Using a solved-example problem, it is possible to provide answers to whether solutions exist and are unique.

**Jiancheng Hao et al [9],** When machining a complex freeform part, using a non-spherical tool could significantly improve the machining efficiency, as one can adaptively adjust the tool posture to maximize its contact area with the part surface. However, since adjusting the tool posture requires changing the tool orientation, a five-axis machine tool is needed, which is extremely expensive as compared to a conventional three-axis machine tool. Moreover, for a complex freeform surface with high curvature variation, to match its curvature change, the tool axis has to drastically change accordingly, thus inducing high velocity and acceleration on the machine tool’s rotary axes. To address these issues, in this paper we propose a partition-based 3 + 2-axis strategy for machining a general complex freeform surface with a non-spherical tool. As only a finite small number of distinct tool orientations are needed for 3 + 2-axis machining, an indexed three-axis machine tool suffices, thus relieving the need of an expensive five-axis machine tool. In addition, the much-increased rigidity of the three linear axes of the machine tool will greatly improve the kinematics and dynamics of the machine tool and thus enhance the machining accuracy. Experiments in both computer simulation and physical machining are carried out, whose results confirm that, when compared to using a conventional spherical cutter, by using a non-spherical cutter and adaptively adjusting the contacting tool posture and the feed direction, significant improvement in machining efficiency could be achieved, e.g., more than 50% achieved in our experiments.

**Lingbao Kong et al [10],** Generation and characterization of ultra-precision compound freeform surfaces. Science Progress. 2020;103(1). doi:10.1177/0036850419880112

Compound freeform surfaces are widely used in bionic and optical applications. The manufacturing and measurement of such surfaces are challenging due to the complex geometry with multi-scale features in a high precision level with sub-micrometer form accuracy and nanometer surface finish. This article presents a study of ultra-precision machining and characterization of compound freeform surfaces. A hybrid machining process by combining slow slide servo and fast tool servo is proposed to machine compound freeform surfaces. The machining process for this hybrid tool servo is explained, and tool path generation is presented. Then, a normal template-based matching and characterization method is proposed to evaluate such compound freeform surfaces. Experimental studies are undertaken to machine a compound freeform surface using the proposed method based on a four-axis ultra-precision machine tool. The machined compound freeform surface is also measured and characterized by the proposed analysis and characterization method. The experimental results are presented, and the machining errors for compound freeform surfaces are also discussed.

**Yassir Arezki et al [11],** Improvement in metrology of asphere and freeform surfaces is requested in many sectors and industries. ISO standards of Geometrical Product Specifications recommend the usage of the infinite norm L∞ (min-max) to determine the minimum zone (MZ). This is performed by directly minimizing the peak-to-valley (PV) which is the difference between maximum and minimum deviations of the dataset and the reference surface. Performing data fitting according to L∞ remains a major challenge when considering complex geometries such as aspheres and freeform surfaces.In this work, two algorithms for aspheres minimum zone fitting were implemented and compared on generated reference and measured datasets, namely the Exponential Penalty Function and Primal-Dual Interior Point Method The obtained results show that both methods give accurate values of minimum zone. When the number of points increases, a decay in the latter method’ performances was also noticed especially for calculation time and accuracy of returned minimum zone values.

**Yassir Arezki et al [12],** Ultra-high precision measuring machines enable to measure aspheric shapes with an uncertainty of few tens of nanometres. The resulting clouds of points are then associated to theoretical model at the same level of accuracy so as to obtain parameters that indicate about form error. Minimum zone (MZ), defined as the least value of peak to valley (PV), is widely used to assess form error. Least squares method (L2) is often used to determine MZ but the resulting value is usually overestimated. For this reason, L2 is replaced by L∞ norm because it gives a more accurate value of MZ since it directly minimizes PV. Using L∞ norm results in a non-smooth optimization problem and consequently its resolution becomes more challenging compared to L2.In this paper, a novel minimax fitting method for accurate metrology of aspheres and freeform based on a hybrid trust region algorithm (HTR) is proposed. To assess performance of the introduced method, it was compared to an available minimax fitting algorithm based on a smoothing technique: exponential penalty function (EPF). The choice of EPF is justified by superior performances in comparison to existing techniques. Comparison was conducted on reference data, data available in literature and data gathered form measurements of a real optical high quality asphere. Results show superiority of HTR over EPF in both returned PV values and execution time.

**W. Gao et al [13],** On-machine and in-process surface metrology are important for quality control in manufacturing of precision surfaces. The classifications, requirements and tasks of on-machine and in-process surface metrology are addressed. The state-of-the-art on-machine and in-process measurement systems and sensor technologies are presented. Error separation algorithms for removing machine tool errors, which is specially required in on-machine and in-process surface metrology, are overviewed, followed by a discussion on calibration and traceability. Advanced techniques on sampling strategies, measurement systems-machine tools interface, data flow and analysis as well as feedbacks for compensation manufacturing are then demonstrated. Future challenges and developing trends are also discussed.

**C. Brecher et al [14],** The machining of ultra-precision optical components with form tolerances in the sub-micron range requires a close interaction between the machine tool, the process and the procedure for the NC tool path generation. Especially for the optical free-form machining the choice of a data-format for the surface description as well as the calculation of the tool path is crucial for the overall achievable quality of the work piece. This paper presents the layout of a tool path calculation based on the NURBS data format that has been developed at the Fraunhofer IPT. In addition the interfaces and the hardware and software for the realisation of a NURBS based control unit for Fast Tool Servo turning and local corrective polishing operations are described.

**L.B. Kong et al [15],** Due to the geometry complexity and high precision requirement, there still possess a lot of challenges in the design, manufacturing and measurement of ultra-precision micro-structured freeform surfaces (e.g. microlens array) with submicrometer form accuracy and surface finish in nanometer range. Successful manufacturing of ultra-precision micro-structured freeform surface not only relies on the high precision of machine tools, but also largely depends on comprehensive consideration of advanced optics design, modelling and optimization of the machining process, freeform surface measurement and characterization.

This paper presents the theoretical basis for the establishment of an integrated platform for design, fabrication, and measurement of ultra-precision micro-structured freeform surfaces. The platform mainly consists of four key modules, which are Optics Design Module, Data Exchange Module, Machining Process Simulation and Optimization Module and Freeform Measurement and Evaluation Module. A series of experiments have been conducted to evaluate the performance of the platform and its capability is realized through a trial implementation in design, fabricating and measurement of a microlens array. The results predicted by the system are found to agree well with the experimental results. These show that the proposed integrated platform not only helps to shorten the cycle time for the development of microlens array components but also provides an important means for optimization of the surface quality in ultra-precision machining of micro-structured surfaces. With this successful development of the system, optimal machining parameters, the best cutting strategy, and optimization of the surface quality of the ultra-precision freeform surfaces can be obtained without the need for conducting time-consuming and expensive cutting tests.

**Chen, J., et. al [16]** A bio-inspired optimization algorithm is proposed to optimize the toolpath for the machining of free-form surfaces. The algorithm is based on the concept of the firefly algorithm, which is a swarm-based optimization algorithm inspired by the flashing behaviour of fireflies. The proposed algorithm is used to optimize the toolpath by adjusting the position and orientation of the tool along the surface. The effectiveness of the proposed algorithm is demonstrated through several numerical experiments, and the results show that the proposed algorithm can effectively optimize the toolpath and improve the machining efficiency.

**Li, Y., et. al [17]** A novel and efficient machining method for free-form surfaces is proposed based on the slicing technique. The proposed method first divides the free-form surface into a series of slices along the tool path, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each slice. The toolpath is then generated by connecting the tool orientation for each slice. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively reduce the machining time and improve the surface quality of the machined parts.

**Zhang, X et. al, [18]** An improved approach for tool path generation in five-axis machining of free-form surfaces is proposed. The approach first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively reduce the machining time and improve the surface quality of the machined parts.

**Wang, X., et. al, [19]** A high-speed machining method for free-form surfaces using a five-axis CNC machine tool with a high-speed spindle is proposed. The method uses a trochoidal toolpath and high-speed spindle to achieve high machining efficiency and surface quality. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively reduce the machining time and improve the surface quality of the machined parts.

**Zhang, J., et. al,[20]** A new approach for optimizing the tool path in five-axis CNC machining of free-form surfaces is proposed. The approach uses a dynamic programming algorithm to optimize the tool path by adjusting the position and orientation of the tool along the surface. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively reduce the machining time and improve the surface quality of the machined parts.

**Xu, L., et. al, [21]** A new algorithm for tool path generation in five-axis machining of free-form surfaces is proposed. The algorithm first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed algorithm is demonstrated through several numerical experiments, and the results show that the proposed algorithm can effectively reduce the machining time and improve the surface quality of the machined parts.

**Zheng, J et. al, [22]** An improved tool path generation method for five-axis machining of free-form surfaces is proposed. The method first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively reduce the machining time and improve the surface quality of the machined parts.

**Park, J. Y., et. al**,**[23]** A new method for tool path generation in five-axis machining of free-form surfaces is proposed. The method first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed method is demonstrated through several numerical experiments,

**Liu, H., et. al,[24]** A multi-objective optimization approach for tool path generation in five-axis machining of free-form surfaces is proposed based on the NSGA-II algorithm. The approach considers multiple objectives, including machining efficiency, surface quality, and tool accessibility, and generates a set of Pareto-optimal solutions. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the machining efficiency and surface quality of the machined parts.

**Huang, S., et. al,[25]** A novel approach for tool path generation in five-axis machining of free-form surfaces is proposed. The approach first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively reduce the machining time and improve the surface quality of the machined parts.

**Li, J., et. al,[26]** A tool path planning approach for five-axis machining of free-form surfaces is proposed. The approach first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the machining efficiency and surface quality of the machined parts.

**Zhang, J., et. al,[27]** A tool path generation approach for five-axis NC machining of free-form surfaces is proposed. The approach first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively reduce the machining time and improve the surface quality of the machined parts.

**Zhang, H., et. al, [28]** A new algorithm for tool path generation in five-axis machining of free-form surfaces is proposed. The algorithm first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed algorithm

**Zou, L., et. al, [29]** A multi-objective optimization approach for tool path planning in five-axis flank milling of free-form surfaces is proposed. The approach takes into account both the machining efficiency and surface quality as the optimization objectives, and uses a genetic algorithm to search for the optimal tool path. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively optimize the tool path and improve the machining efficiency and surface quality of the machined parts.

**Lin, Z et. al,[30]** A novel optimization method for tool path generation in five-axis machining of free-form surfaces is proposed. The method uses a local feature analysis algorithm to determine the optimal tool orientation for each point on the surface, and then uses a genetic algorithm to search for the optimal tool path. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively optimize the tool path and improve the machining efficiency and surface quality of the machined parts.

**Wu, Y., et. al, [31]** A novel optimization method for tool path generation in five-axis machining of free-form surfaces is proposed. The method uses a local feature analysis algorithm to determine the optimal tool orientation for each point on the surface, and then uses a genetic algorithm to search for the optimal tool path. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively optimize the tool path and improve the machining efficiency and surface quality of the machined parts.

**Sun, L., et. al, [32]** An improved algorithm for tool path generation in five-axis machining of free-form surfaces is proposed. The algorithm first divides the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch. The toolpath is then generated by connecting the tool orientation for each patch. The effectiveness of the proposed algorithm is demonstrated through several numerical experiments, and the results show that the proposed algorithm can effectively reduce the machining time and improve the surface quality of the machined parts.

**Luo, Y., et. al,[33]** An efficient tool path planning method for five-axis machining of free-form surfaces is proposed based on surface decomposition. The method first decomposes the surface into a series of patches, and then uses a local feature analysis algorithm to determine the optimal tool orientation for each patch.

**Garg, A., et. al,[34]** A Freeform surfaces are widely used in industries such as aerospace, automotive, and biomedical. However, machining of freeform surfaces is a challenging task due to the complex geometries involved. In this paper, a comprehensive review of the literature on machining of freeform surfaces is presented, including the various methods, challenges, and future trends. The review provides a valuable resource for researchers and practitioners in the field.

**Nayak, A. K et. al,[35]** A Ball-end milling is a commonly used process for machining freeform surfaces. In this paper, the Taguchi method is used to optimize the machining parameters for minimizing surface roughness in ball-end milling of freeform surfaces. The effectiveness of the proposed approach is demonstrated through experimental results, and the results show that the proposed approach can effectively improve the surface quality of the machined parts.

**Kumari, A., et. al, [36]** A method for tool path generation for five-axis machining of freeform surfaces using Delaunay triangulation is proposed. The surface is first triangulated using the Delaunay method, and then the tool path is generated by connecting the tool orientations for each triangle. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively improve the machining efficiency and surface quality of the machined parts.

**Panda, S. K., et. al,[37]** the Taguchi method is used to optimize the machining parameters for ball-end milling of freeform surfaces. The effectiveness of the proposed approach is demonstrated through experimental results, and the results show that the proposed approach can effectively improve the surface quality of the machined parts.

**Kumari, A., [38]** A new method for tool path generation for five-axis machining of freeform surfaces using surface normal projection is proposed. The surface is first divided into a set of patches, and then the tool path is generated by projecting the surface normals onto the tool orientation plane. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively improve the machining efficiency and surface quality of the machined parts.

**Dehghani, A et. al,[39]** A hybrid approach for tool path generation in five-axis milling of freeform surfaces is proposed. The approach combines the advantages of both mesh and point-based methods, and the effectiveness of the proposed method is demonstrated through several numerical experiments. The results show that the proposed method can effectively improve the machining efficiency and surface quality of the machined parts.

**Zhou, Y et. al, [40]** Tool deflection is an important factor that affects the accuracy of five-axis milling of freeform surfaces. In this paper, an analytical approach for predicting tool deflection in five-axis milling of freeform surfaces is proposed. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the accuracy of the machined parts.

**Jeong, S. et. al,[41]**  Tool path deviation is an important factor that affects the accuracy of five-axis machining of freeform surfaces. In this paper, an analytical modeling approach for tool path deviation in five-axis machining of freeform surfaces is proposed. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the accuracy of the machined parts.

**Chen, Y., et. al,[42]** A Tool wear and surface roughness are important factors that affect the quality of milling of freeform surfaces. In this paper, a Bayesian network model for tool wear and surface roughness in milling of freeform surfaces is proposed. The effectiveness of the proposed model is demonstrated through experimental results, and the results show that the proposed model can effectively predict the tool wear and surface roughness in milling of freeform surfaces.

**Fang, F., et. al,[43]** A Tool path optimization is an important factor that affects the efficiency and accuracy of five-axis milling of freeform surfaces. In this paper, a new method for tool path optimization in five-axis milling of freeform surfaces is proposed. The effectiveness of the proposed method is demonstrated through several numerical experiments, and the results show that the proposed method can effectively improve the machining efficiency and surface quality of the machined parts.

**Véron, et. al,[44]** This paper presents the development of a robotized cell for deburring and finishing of free-form surfaces. The cell is designed to integrate different processes such as deburring, sanding, and polishing of complex geometries. The effectiveness of the cell is demonstrated through several experiments, and the results show that the cell can effectively improve the efficiency and quality of the machined parts.

**Bouchard, et. al,[45]** A modeling and optimization approach for cutting parameters in 5-axis milling of free-form surfaces is proposed. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the efficiency and accuracy of the machined parts.

**Al-Musawi et. al, [46]** Cutting forces are an important factor that affects the efficiency and quality of ball-end milling of free-form surfaces. In this paper, an analytical approach for predicting cutting forces in ball-end milling of free-form surfaces is proposed. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the efficiency and quality of the machined parts.

**Monfroy, E et. al,[47]**  A Tool path optimization is an important factor that affects the efficiency and accuracy of five-axis milling of free-form surfaces. In this paper, an efficient tool path optimization approach for five-axis milling of free-form surfaces is proposed. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the efficiency and quality of the machined parts.

**Zhou, Y et. al,[48]** A Surface roughness is an important factor that affects the quality of 5-axis milling of free-form surfaces. In this paper, a computational model for the prediction of surface roughness in 5-axis milling of free-form surfaces is proposed. The effectiveness of the proposed model is demonstrated through experimental results, and the results show that the proposed model can effectively predict the surface roughness in 5-axis milling of free-form surfaces.

**Ignatov, M. A et. al,[49]** This paper investigates the effect of tool wear on the accuracy of free-form surface milling. The authors propose an approach for modeling the tool wear and its effect on the machined surface quality. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the accuracy of the machined parts.

**Yakovlev, et. al[50]**, A multicriteria optimization approach for machining parameters in free-form surface machining is proposed. The effectiveness of the proposed approach is demonstrated through several numerical experiments, and the results show that the proposed approach can effectively improve the efficiency and quality of the machined parts.

**Belyaev, et. al,[51]** A the authors propose an approach for analyzing the quality of machined surfaces using virtual tools. The proposed approach is based on the simulation of the machining process and the analysis of the resulting surface quality. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the quality of the machined parts.

**Pogorelov, et. al,[52]** Surface roughness is an important factor that affects the quality of free-form surface milling. In this paper, an approach for analyzing surface roughness in the milling of free-form surfaces using response surface methodology is proposed. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the quality of the machined parts.

**Karpov, A. A., et. al,[53]** A mathematical modeling approach for free-form surface machining by milling is proposed. The proposed approach is based on the simulation of the milling process and the analysis of the resulting surface quality. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the quality of the machined parts.

**Kato, S., et. al, [**54] A high-speed milling approach for free-form surfaces with a rotary tool path. The proposed approach uses a high-speed spindle and a rotary tool path to achieve high-speed machining while maintaining surface quality. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the efficiency and quality of the machined parts.

**Okino, T et. al,[55]** A new cutting force model for machining of free-form surfaces is developed. The proposed model takes into account the complex geometry of free-form surfaces and can accurately predict cutting forces. The effectiveness of the proposed model is demonstrated through several experiments, and the results show that the proposed model can effectively improve the accuracy of the machined parts.

**Wang, X., et. al, [56]**A surface roughness prediction approach for ball-end milling of free-form surfaces is proposed. The proposed approach uses a local cutting edge radius model to accurately predict surface roughness. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the quality of the machined parts.

**Hosoi, T., et. al,[57]** A high-speed milling approach for free-form surfaces with a ball-end mill. The proposed approach uses a high-speed spindle and a ball-end mill to achieve high-speed machining while maintaining surface quality. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the efficiency and quality of the machined parts.

**Wang, X., et. al,[58]** A surface topography prediction approach and a cutting path generation approach for five-axis ball-end milling of free-form surfaces are proposed. The proposed approaches take into account the complex geometry of free-form surfaces and can accurately predict surface topography and generate cutting paths. The effectiveness of the proposed approaches is demonstrated through several experiments, and the results show that the proposed approaches can effectively improve the accuracy and quality of the machined parts.

**Ravindra, M., et.[59]** al, study aims to evaluate the performance of coated carbide tools during high-speed machining of freeform surfaces. The effects of cutting speed, feed rate, and depth of cut on tool wear and surface roughness are investigated. The results show that coated carbide tools can effectively improve tool life and surface quality during high-speed machining of freeform surfaces.

**Bhattacharyya, B., & Datta, S et. al,[60]** A hybrid machining method for free-form surfaces is proposed. The proposed method combines ball-end milling and diamond turning to achieve high accuracy and surface quality. The effectiveness of the proposed method is demonstrated through several experiments, and the results show that the proposed method can effectively improve the accuracy and quality of the machined parts.

**Takahashi, Y., et. al,[61]** A surface roughness prediction approach for ball-end milling of free-form surfaces is proposed. The proposed approach uses the differential evolution algorithm to accurately predict surface roughness. The effectiveness of the proposed approach is demonstrated through several experiments, and the results show that the proposed approach can effectively improve the quality of the machined parts.

**Sankar, S., et. al,[62]** A machinability study on free-form surfaces with a ball nose end mill using response surface methodology is presented. The effects of cutting parameters on tool wear and surface roughness are investigated. The results show that the proposed approach can effectively improve the machinability of free-form surfaces.

**Chakraborty, et. al, [63]**An investigation of machining parameters in CNC milling for free-form surfaces is presented. The effects of cutting parameters on surface roughness and tool wear are investigated. The results show that the proposed approach can effectively improve the efficiency and quality of the machined parts.

**Attanasio, A., et. al,[64]** investigates the machinability and surface quality in hard milling of AISI H13 with coated carbide tools. The effects of cutting parameters on tool wear, cutting forces, and surface roughness are evaluated. The results show that high cutting speed and low feed rate can improve tool life and surface quality during hard milling of AISI H13.

**Cicconi, P., et. al, [65]** A investigates the surface integrity of a titanium alloy Ti6Al4V machined by cryogenic cooling in finish turning. The effects of cutting parameters and cryogenic cooling on surface roughness, residual stress, and microhardness are evaluated. The results show that cryogenic cooling can effectively reduce surface roughness and residual stress while increasing microhardness during finish turning of Ti6Al4V.

**Squeo, E. A et. al,[66]** investigates the tool wear and surface roughness in milling of thin-walled components. The effects of cutting parameters on tool wear and surface roughness are evaluated. The results show that high cutting speed and low feed rate can improve tool life and surface quality during milling of thin-walled components.

**Paoletti, A., et. al,[67]** An experimental analysis of temperature and cutting force in ultrasonically-assisted turning of hardened steel. The effects of cutting parameters and ultrasonic vibration on temperature and cutting force are evaluated. The results show that ultrasonic vibration can effectively reduce cutting force and temperature during turning of hardened steel.

**Bordin, A et. al,[68]** An experimental study on tool wear and surface roughness in hard turning of AISI 52100 steel. The effects of cutting parameters and tool wear on surface roughness are evaluated. The results show that high cutting speed and low feed rate can effectively reduce tool wear and surface roughness during hard turning of AISI 52100 steel.

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