



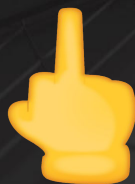
TRAIL
OF
BITS



Fuck RSA

Summercon 2019
Ben Perez

RSA



TRAIL
OF
BITS

Fuck RSA



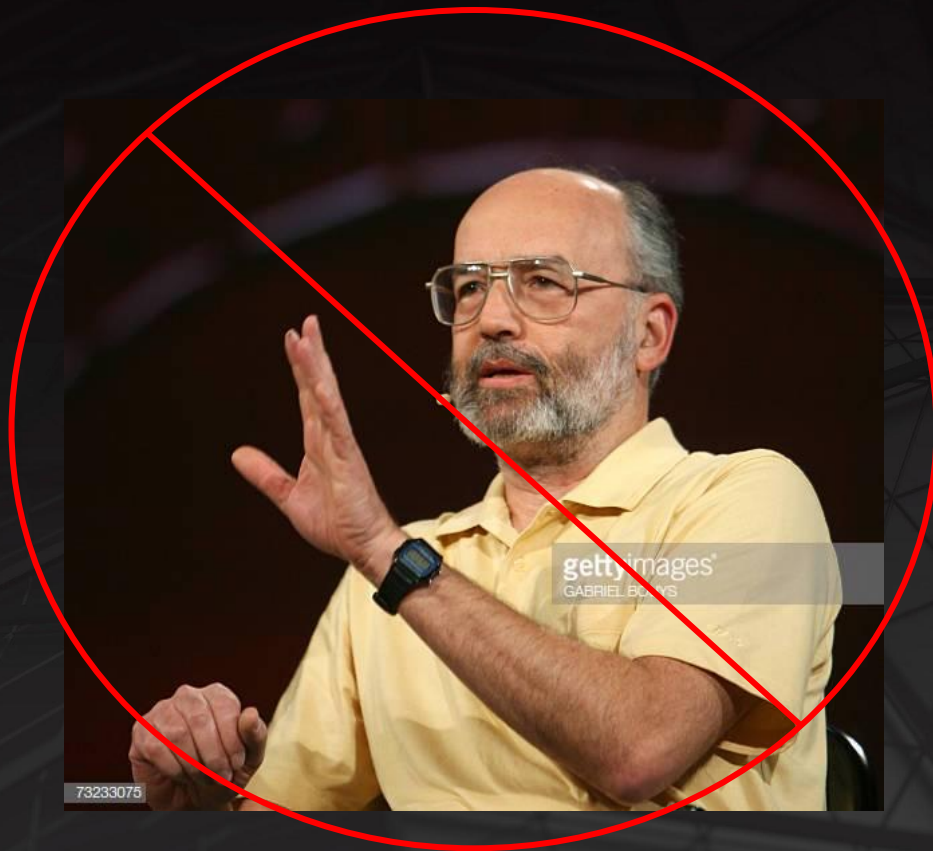


TRAIL
OF
BITS



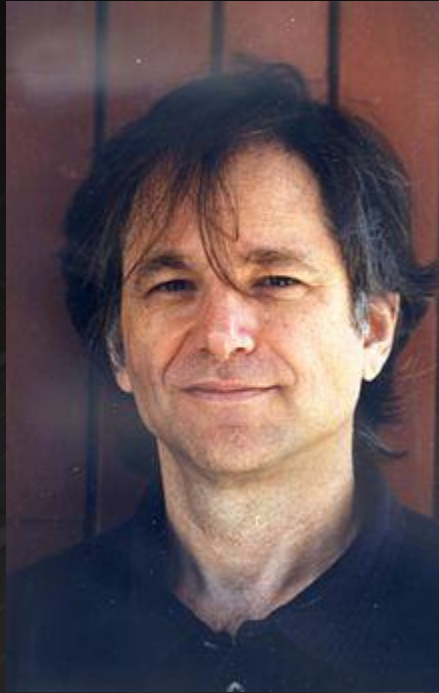
Lizard Person

TRAIL
OF
BITS



Cancelled

Biologist



TRAIL
OF
BITS

RSA INVENTED
1977



TRAIL
OF
BITS

RIVEST

SHAMIR

ADLEMAN

ELVIS

21

16

23

18

$$78 + 4096 - 2920 = 1254$$

RSA KEY
SIZE 2019

TRAIL
OF
BITS



$$1254 / 2 + 39 =$$

6 6 6

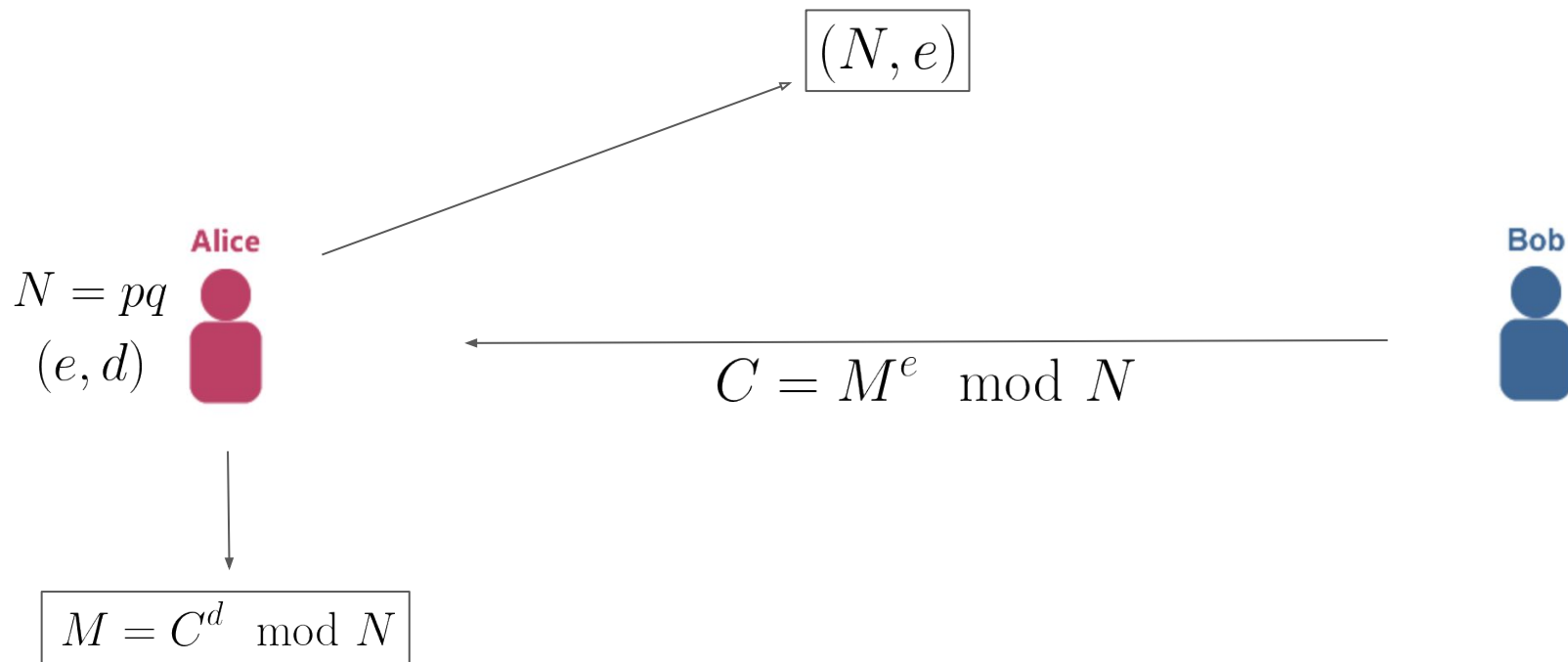


TRAIL
OF
BITS

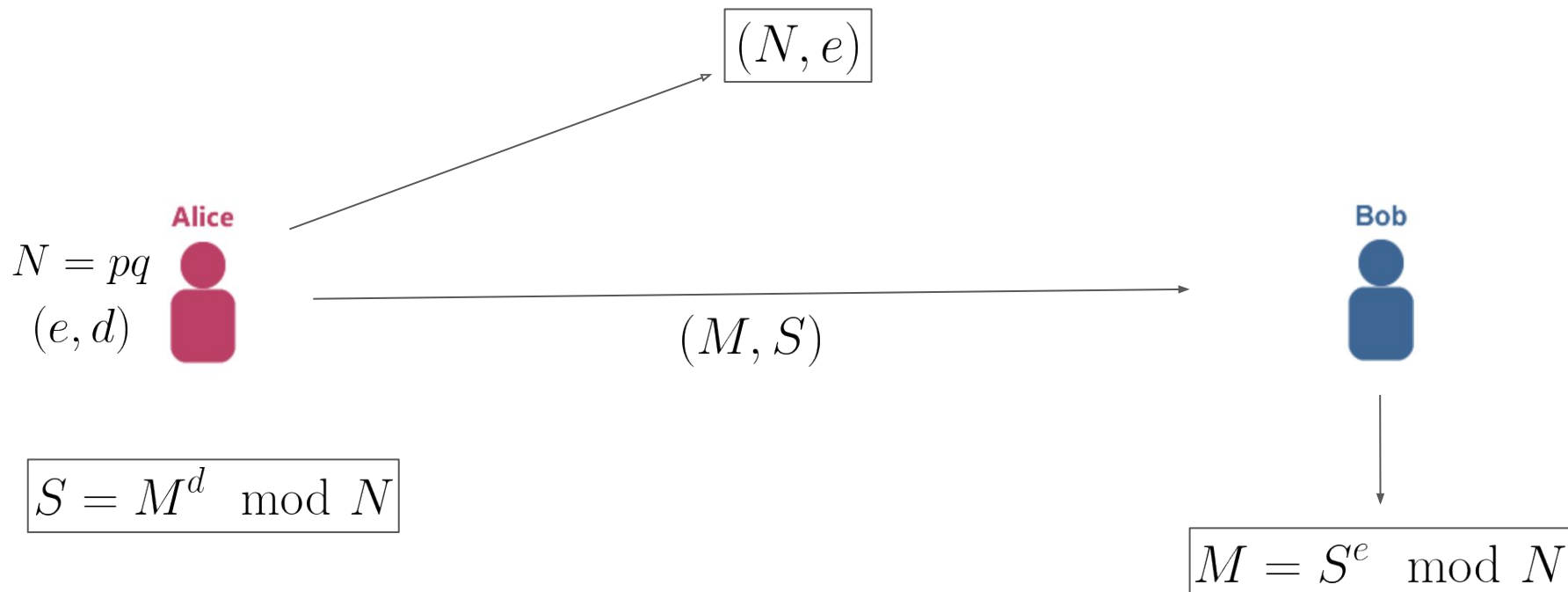
RSA Primer

TRAIL
OF
BITS

What is RSA



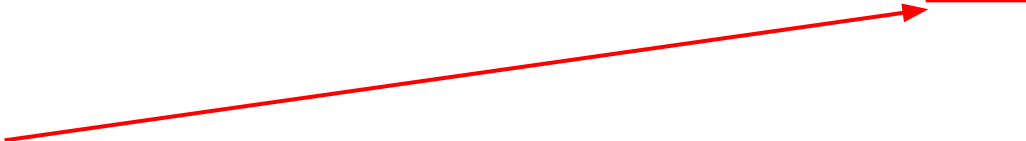
What is RSA



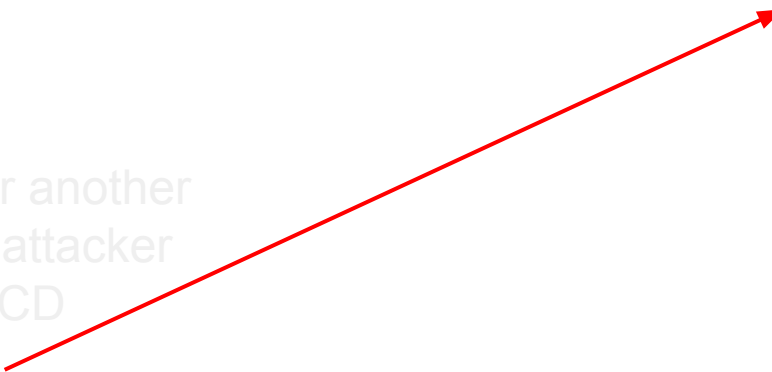
Parameter Selection

TRAIL
OF
BITS

$$M = (M^e)^d \mod pq$$

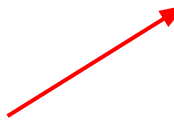
$$M = (M^e)^d \bmod \underline{pq}$$


If Alice reuses p for another
RSA modulus pq' , attacker
can factor using GCD

$$M = (M^e)^d \bmod \underline{pq}$$


If Alice reuses p for another
RSA modulus pq' , attacker
can factor using GCD


If p and q share approximately half
of their upper bits, then pq can be
factored using Fermat's method

$$M = (M^e)^d \bmod \underline{pq}$$


If Alice reuses p for another RSA modulus pq' , attacker can factor using GCD

If either p or q contains too many contiguous zero bits, then pq can be factored using Coppersmith's method

If p and q share approximately half of their upper bits, then pq can be factored using Fermat's method


$$M = (M^e)^d \bmod \underline{pq}$$


If Alice reuses p for another RSA modulus pq' , attacker can factor using GCD

If either p or q contains too many contiguous zero bits, then pq can be factored using Coppersmith's method

If p and q share approximately half of their upper bits, then pq can be factored using Fermat's method

If $p-1$ or $q-1$ has small prime factors, then can use Pollard $p-1$ to factor pq

$$M = (M^e)^d \text{ mod } \underline{pq}$$




ars TECHNICA

BIZ & IT TECH SCIENCE POLICY CARS GAMING & CULTURE

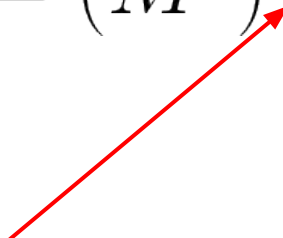
MORE TO COME —

Crippling crypto weakness opens millions of smartcards to cloning

Gemalto IDPrime.NET almost certainly isn't the only smartcard vulnerable to ROCA.

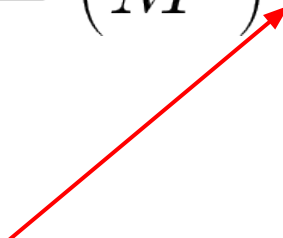
DAN GOODIN - 10/23/2017, 4:30 PM

Private Exponent

$$M = (M^e)^{\underline{d}} \bmod pq$$


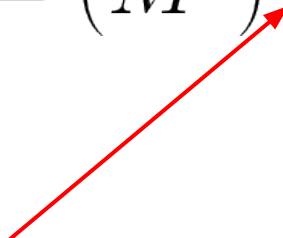
- Small private exponent speeds up decryption

Private Exponent

$$M = (M^e)^{\underline{d}} \mod pq$$


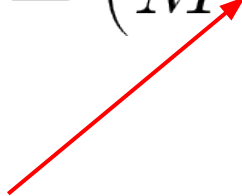
- Small private exponent speeds up decryption
- If $d < \sqrt[4]{pq}$, then Eve can recover private key using continued fractions

Private Exponent

$$M = (M^e)^{\underline{d}} \bmod pq$$


- Small private exponent speeds up decryption
- If $d < \sqrt[4]{pq}$, then Eve can recover private key using continued fractions
- Can use Chinese remainder theorem to speed up decryption instead of picking small d - vulnerable to fault attacks.

Public Exponent

$$M = (M^{\underline{e}})^d \mod pq$$


- Common to use $e = 3, 17, 65537$
- $e = 3$ is very bad
- Related messages can be decrypted
- Partial key exposure attack
- Signature forgery

How Bad is This IRL?



How Bad is This IRL?



saltstack / salt

Watch 616 Star 9,973 Fork 4,576

Code Issues 2,332 Pull requests 271 Projects 2 Wiki Security Insights

Change key generation seq

0.15 [Browse files](#)

thatch45 authored and basepi committed on May 8, 2013 1 parent 43d8c16 commit 5dd304276ba5745ec21fc1e6686a0b28da29e6fc

Showing 1 changed file with 1 addition and 1 deletion. [Unified](#) [Split](#)

2 salt/crypt.py

<pre>@@ -47,7 +47,7 @@ def gen_keys(keydir, keyname, keysize, user=None): 47 priv = '{0}.pem'.format(base) 48 pub = '{0}.pub'.format(base) 49 50 - gen = RSA.gen_key(keysize, 1, callback=lambda x, y, z: None) 51 cumask = os.umask(191) 52 gen.save_key(priv, None) 53 os.umask(cumask)</pre>	<pre>47 priv = '{0}.pem'.format(base) 48 pub = '{0}.pub'.format(base) 49 50 + gen = RSA.gen_key(keysize, 65537, callback=lambda x, y, z: None) 51 cumask = os.umask(191) 52 gen.save_key(priv, None) 53 os.umask(cumask)</pre>
--	---

How Bad is This IRL?



Developers should not need to understand algebraic number theory to build secure software

Padding Attacks

TRAIL
OF
BITS

RSA Requires Padding

Nuclear launch site



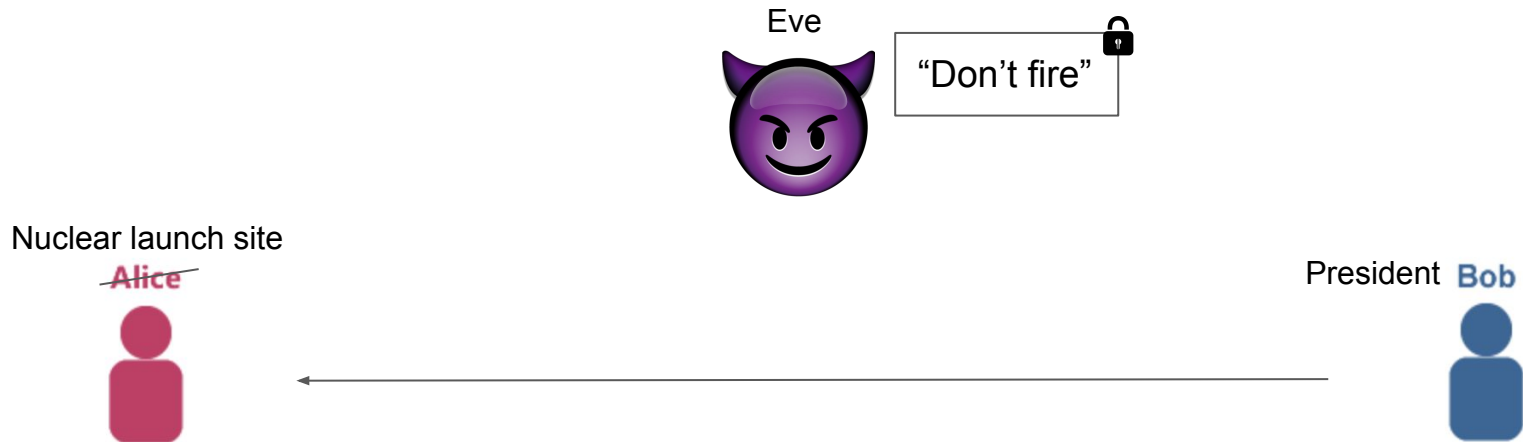
President Bob



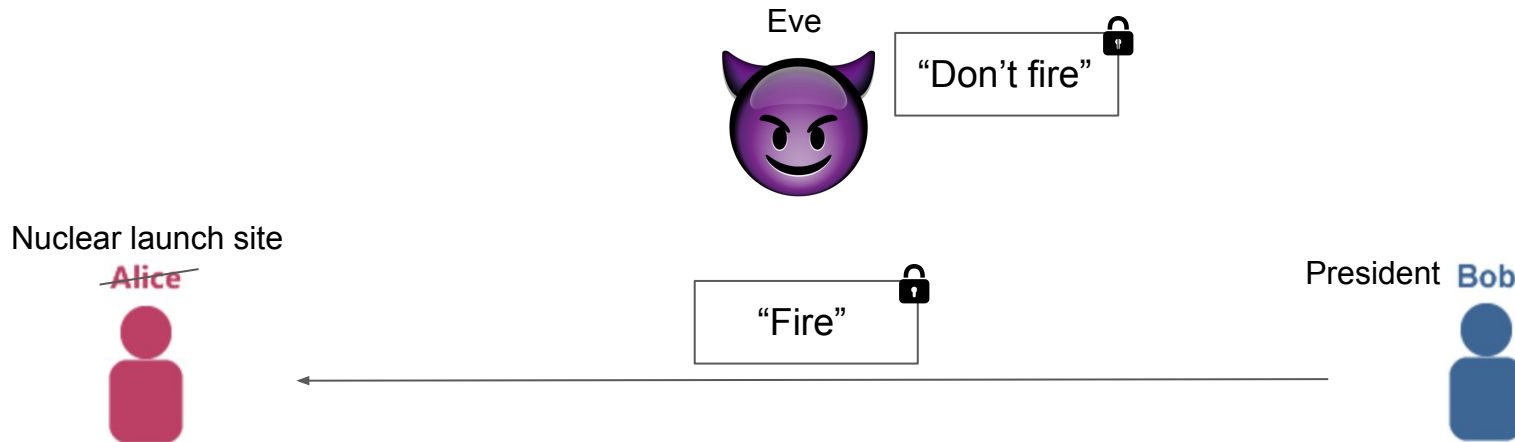
RSA Requires Padding



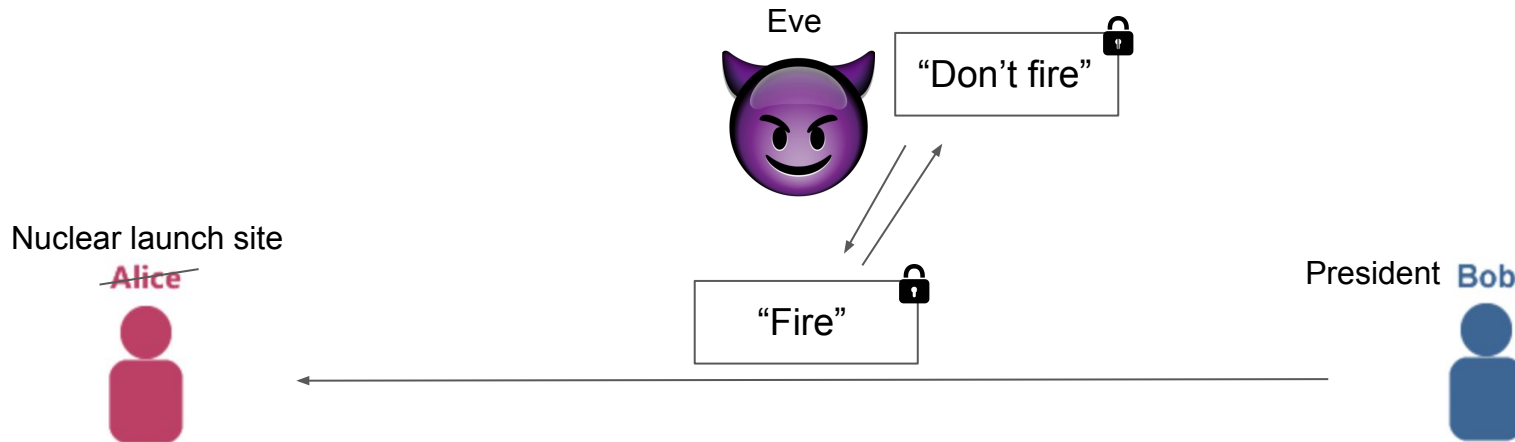
RSA Requires Padding



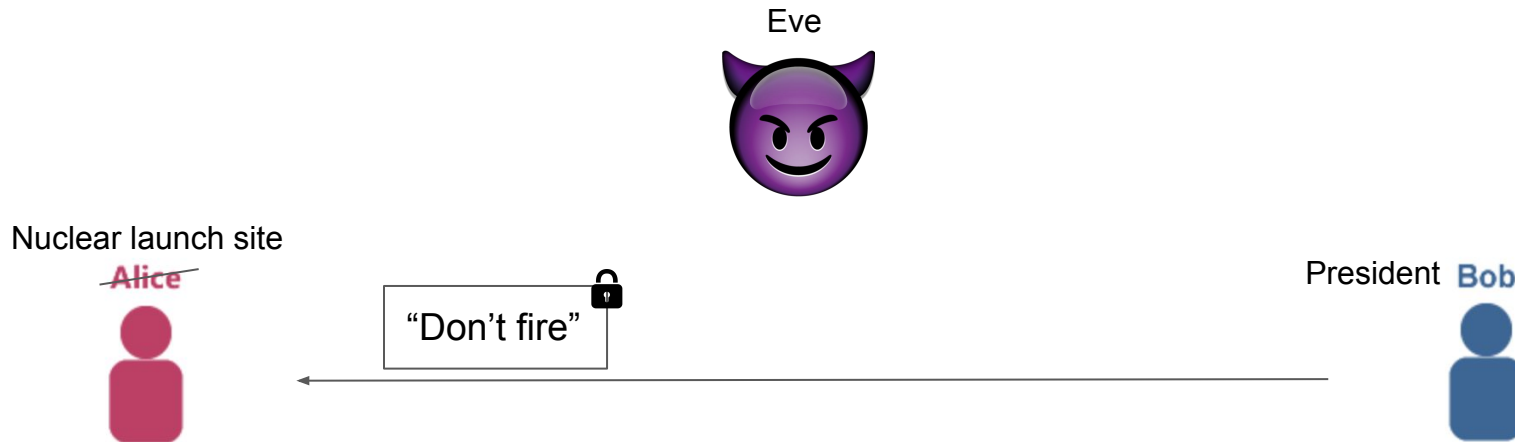
RSA Requires Padding



RSA Requires Padding



RSA Requires Padding



Forgery Attack

```
00 01 FF FF ... FF FF 00 ASN.1 HASH
```

Forgery Attack



```
00 01 FF 00 ASN.1 HASH GARBAGE
```

Forgery Attack

If $e = 3$, can forge signatures



```
00 01 FF 00 ASN.1 HASH GARBAGE
```

Forgery Attack

If $e = 3$, can forge signatures



```
00 01 FF 00 ASN.1 HASH GARBAGE
```



OpenSSL



Padding Oracle Attacks

```
0x00 0x02 [some non-zero bytes] 0x00 [here goes M]
```

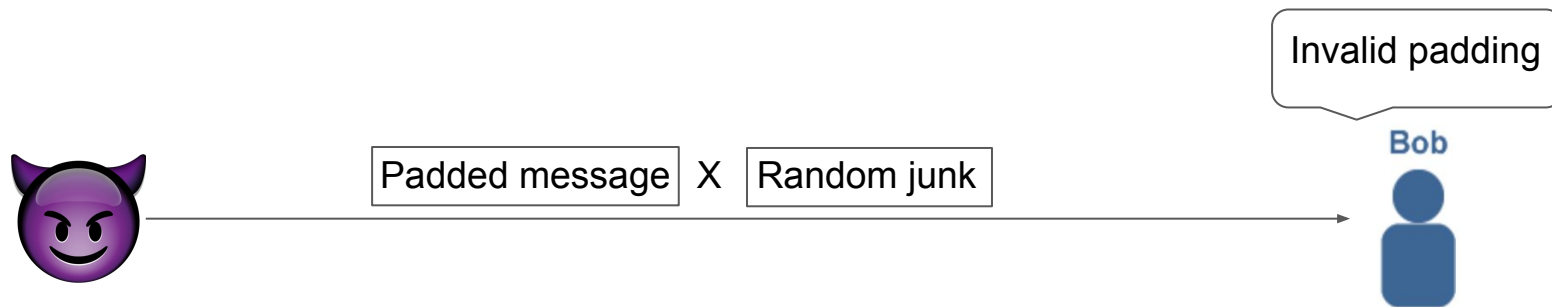
Padding Oracle Attacks



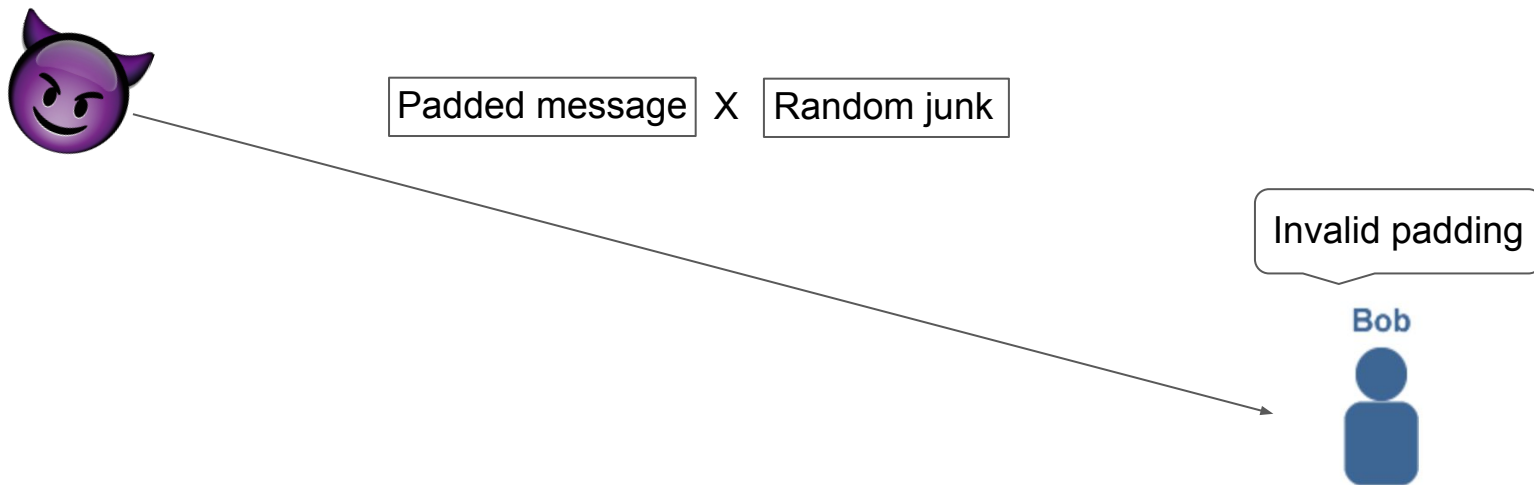
Padding Oracle Attacks



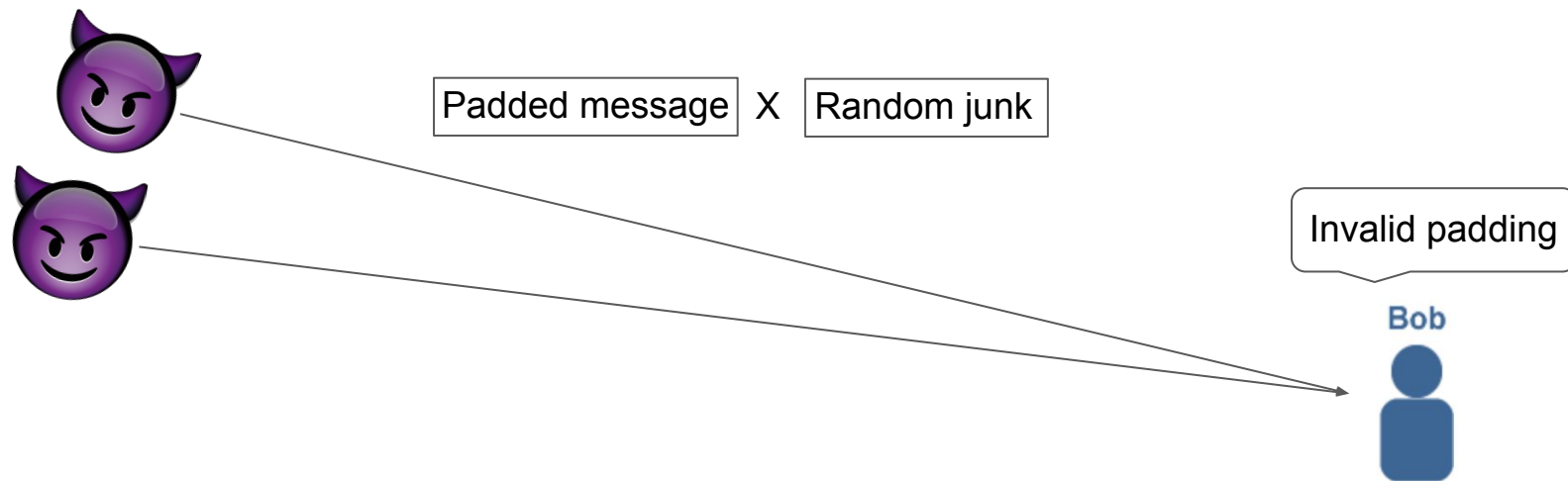
Padding Oracle Attacks



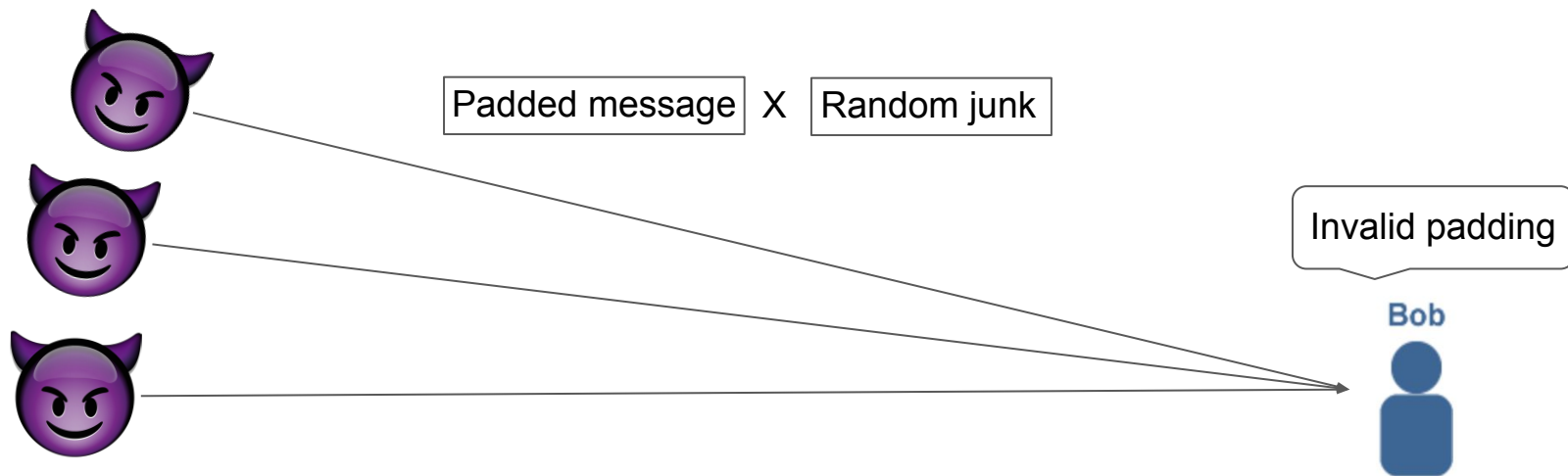
Padding Oracle Attacks



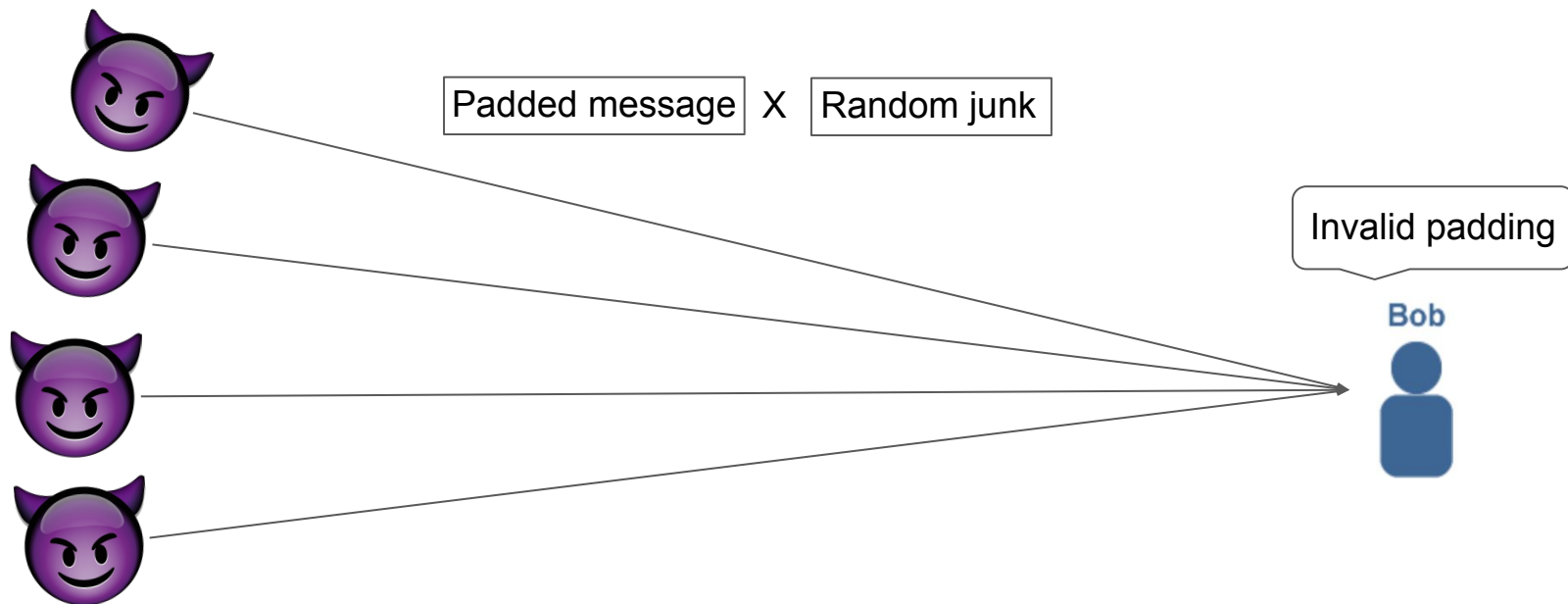
Padding Oracle Attacks



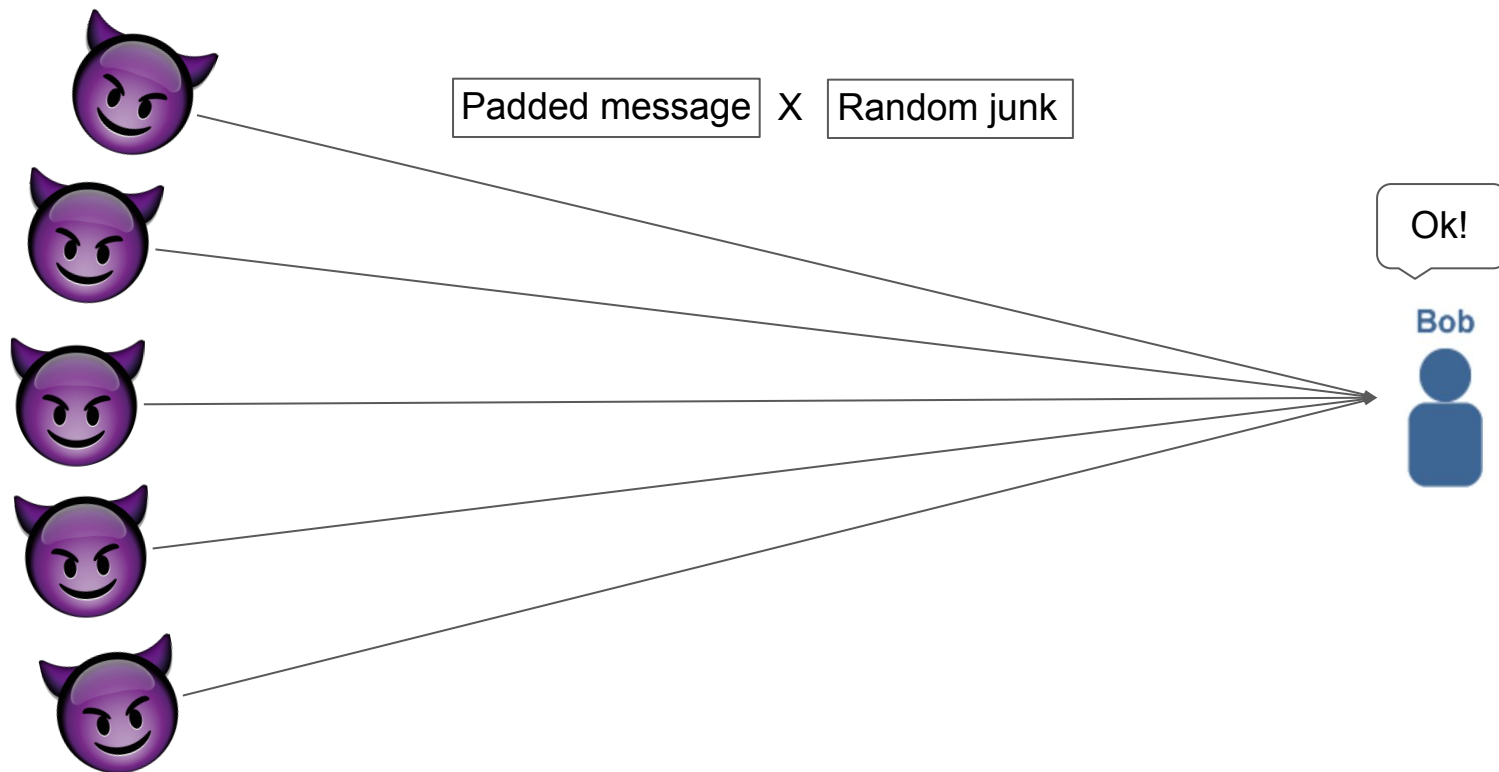
Padding Oracle Attacks



Padding Oracle Attacks



Padding Oracle Attacks



The ROBOT Attack

Return Of Bleichenbacher's Oracle Threat

[Hanno Böck](#), [Juraj Somorovsky](#) ([Hackmanit GmbH](#), Ruhr-Universität Bochum), [Craig Young](#) (Tripwire VERT)

Full paper [published at the Usenix Security conference](#).

An earlier version was [published at the Cryptology ePrint Archive](#)



How Bad is This IRL?

The



Return (

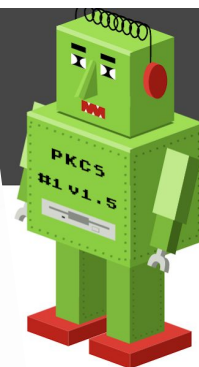
[Hanno Böck,](#)
[Young \(Tripw](#)

[Full paper](#) [pu.](#)

An earlier vers

The Dangers of Key Reuse: Practical Attacks on IPsec IKE

Dennis Felsch, Martin Grothe, and Jörg Schwenk, *Ruhr-University Bochum*;
Adam Czubak and Marcin Szymanek, *University of Opole*
<https://www.usenix.org/conference/usenixsecurity18/presentation/felsch>



How Bad is This IRL?

The

The DROWN Attack



Return

[Hanno F. Young](#) (

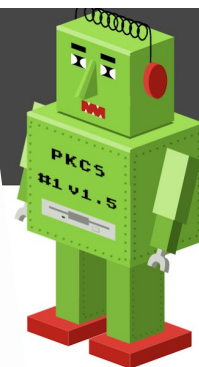
Full pa

An ear

Paper

Q&A

DROWN is a serious vulnerability that affects HTTPS and other services that rely on SSL and TLS, some of the essential cryptographic protocols for Internet security. These protocols allow everyone on the Internet to browse the web, use email, shop online, and send instant messages without third-parties being able to read the communication.



How Bad is This IRL?

The



Retur

[Hanno F](#)
[Young](#) (

Full pa

An ear

DROWN
SSL and
These pr
online, ar
communi

Revisiting SSL/TLS Implementations: New Bleichenbacher Side Channels and Attacks

Christopher Meyer, Juraj Somorovsky, Eugen Weiss, and Jörg Schwenk, *Ruhr-University Bochum*; Sebastian Schinzel, *Münster University of Applied Sciences*; Erik Tews, *Technische Universität Darmstadt*

<https://www.usenix.org/conference/usenixsecurity14/technical-sessions/presentation/meyer>



How Bad is This IRL?

The

The 9 Lives of Bleichenbacher's CAT: New Cache Attacks on TLS Implementations

Eyal Ronen*, Robert Gillham†, Daniel Genkin‡, Adi Shamir§, David Wong§, and Yuval Yarom†**
*Tel Aviv University, †University of Adelaide, ‡University of Michigan, §Weizmann Institute, §NCC Group, **Data61

Review
Bleichenbacher

Christopher Meyer, Juraj Somorovsky,
Bochum; Sebastian Schinzel, Münster.
Technische Universität

<https://www.usenix.org/conference/usenixsecurity14/technical-sessions/presentation/meyer>

...being able to read the



Return

Hanno F
Young (

Full pa

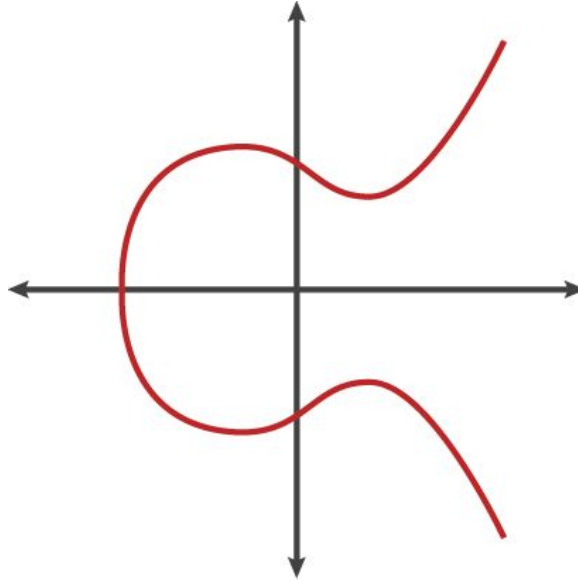
An ear

DROWN
SSL and
These pr
online, ar
communi

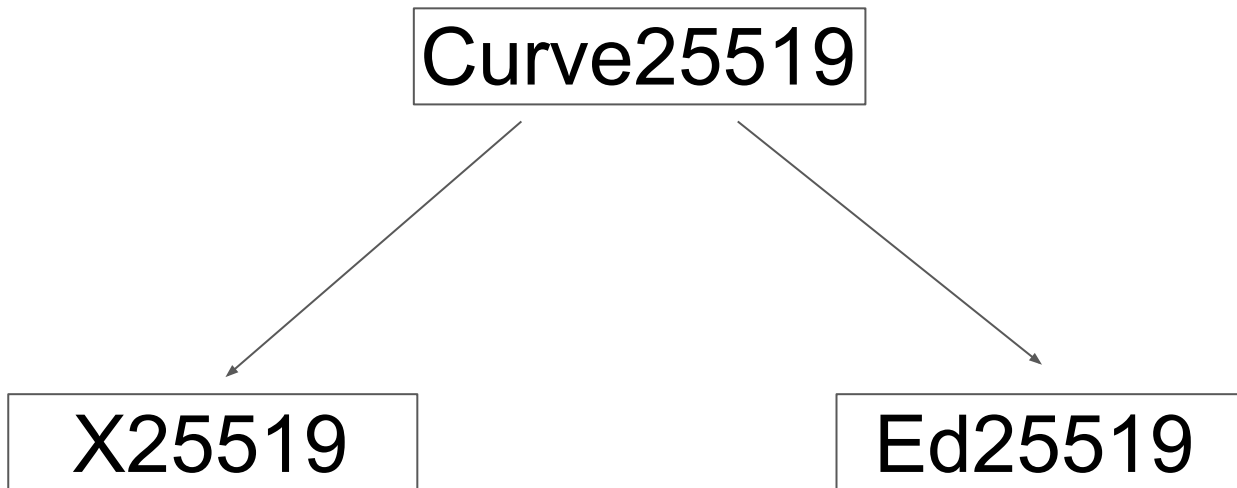
What Should I Use Instead?

TRAIL
OF
BITS

What Should I Use Instead



What Should I Use Instead?



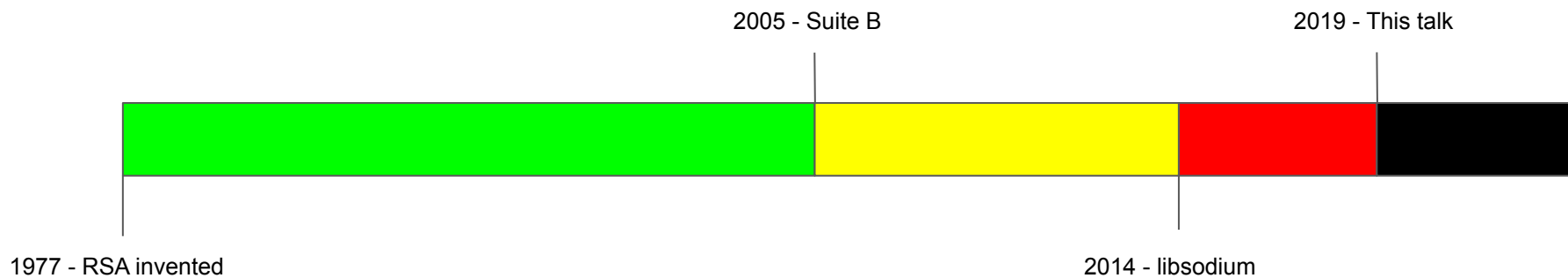
What Should I Use Instead?

 libsodium

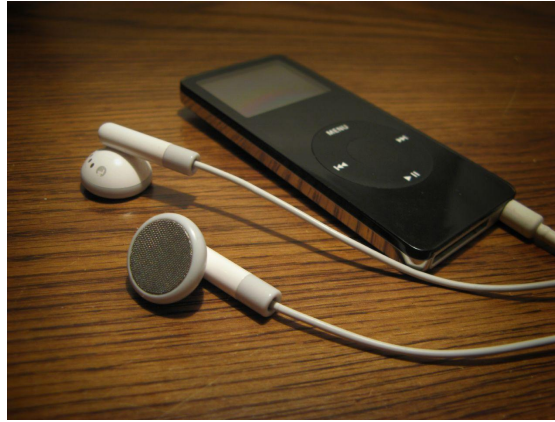
Final Thoughts

TRAIL
OF
BITS

RSA Timeline



RSA Timeline

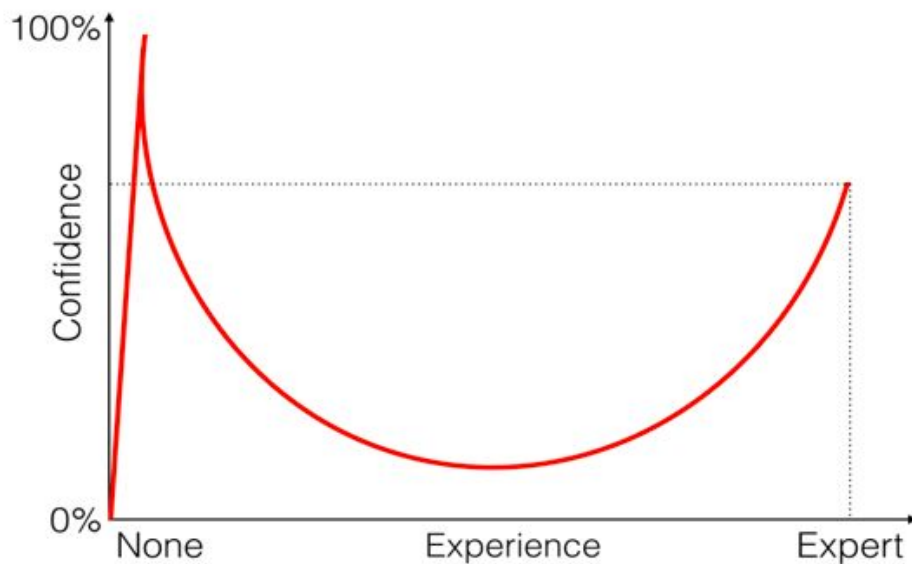


Wrapping Up



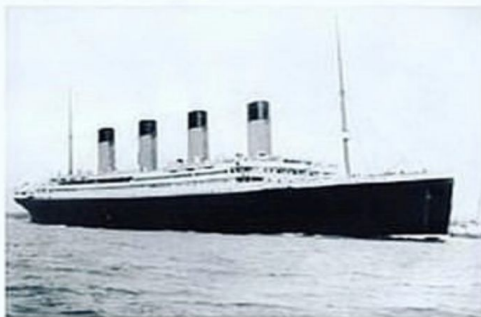
Wrapping Up

Dunning-Kruger Effect



Wrapping Up

What you see VS what ^{cryptographers} see



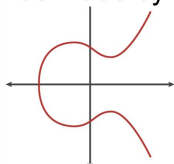
Wrapping Up



Wrapping Up

Imagine trying to use digital signatures

this meme
was made by



ecc gang



but anyone can sign things as you because
you used pkcs#1v1.5 padding wrong

“Using crypto in your application shouldn't have to feel like juggling chainsaws in the dark.” - Tink Documentation

Thanks!

TRAIL
OF
BITS

Contact



Ben Perez

Security Engineer

benjamin.perez@trailofbits.com

[@blperez_](#)