# Deep Fluids: A Generative Network for Parameterized Fluid Simulations

Fall 2020 Research Group Presentation Skylar Wurster

## Deep Fluids: A Generative Network for Parameterized Fluid Simulations

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<sup>1</sup>ETH Zürich <sup>2</sup>Technical University of Munich <sup>3</sup>Pixar Animation Studios

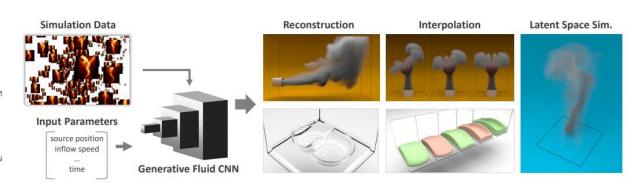


Figure 1: Our generative neural network synthesizes fluid velocities continuously in space and time, using a set of input simulations for training and a few parameters for generation. This enables fast reconstruction of velocities, continuous interpolation and latent space simulations.

- 1. A conditional autoencoder architecture that:
  - a. Reaches up to 1400x compression on flow datasets



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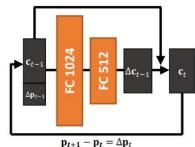


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  - a. Reaches up to 1400x compression on flow datasets
  - b. Generates fluid flow frames (through inference) up to 700x faster than direct numerical simulations (DNS)
  - c. Can approximate frames for unseen parameter settings (conditional generation)
  - d. Works on compressible and incompressible fluids in 2D and 3D



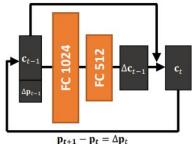
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- 1. A conditional autoencoder architecture...
- 2. A small fully connected network that learns latent space advection to perform simulations completely in the latent space
- 3. A novel *stream function loss* that guarantees the output is physically accurate for incompressible fluids

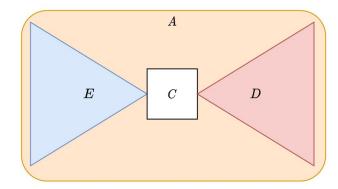




## **Background - Autoencoders**

#### Autoencoders have two parts:

- Encoder (E): "compresses" input into a latent space that captures high level features about the data
- Decoder (D): "decompresses" the latent vector to recover the original ground truth



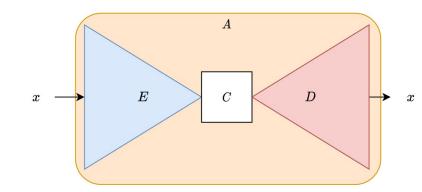
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$$A(x) = D(E(x)) = x$$



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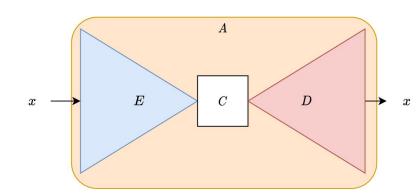
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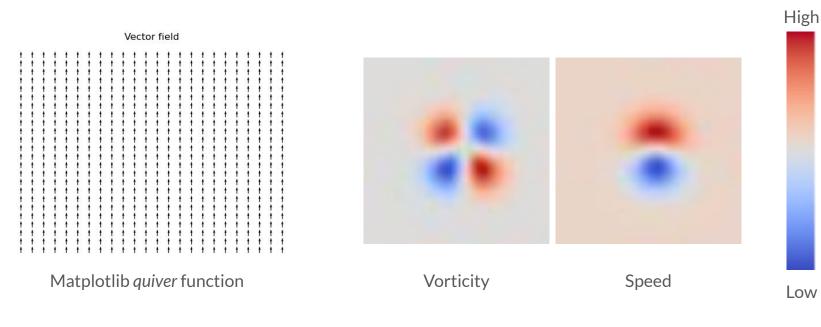
$$A(x) = D(E(x)) = x$$

Therefore, autoencoders are unsupervised.



#### **Background - Fluid representation**

Vector field 2D: [2, x, y]



#### **Background - Fluid representation**

Vector field 2D: [2, x, y] 3D: [3, x, y, z] John Hopkins University Turbulence data (single z-slice of 3D data)

Left: mixing Right: isotropic

Velocity(u,v,w) directly mapped to RGB to visualize

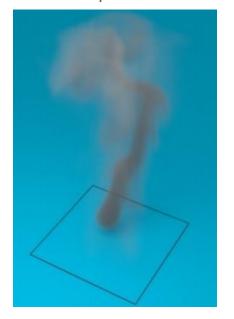




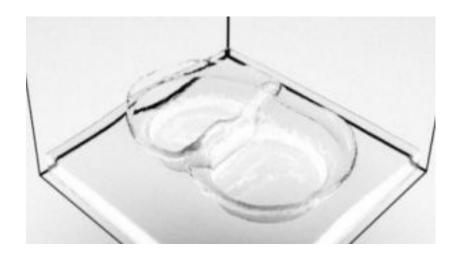
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A property of fluid is *compressibility*.

Compressible



Incompressible

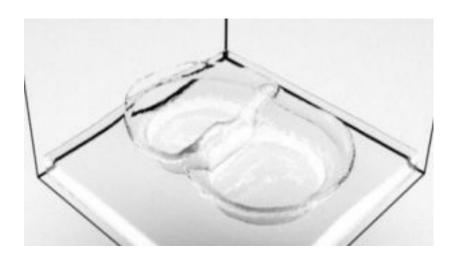


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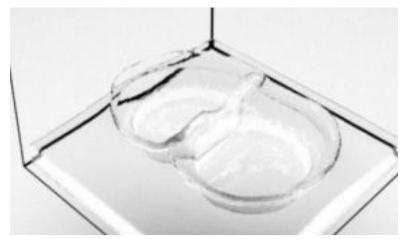


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Incompressibility definition - <u>divergence free</u>

$$divV = \nabla \cdot V = 0$$

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$$abla \cdot V = rac{2 \mathbb{D}}{\partial x} + rac{\partial V_y}{\partial y} \qquad \qquad 
abla \cdot V = rac{3 \mathbb{D}}{\partial x} + rac{\partial V_y}{\partial y} + rac{\partial V_z}{\partial z}$$

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Divergence is a scalar field regardless of dimensionality

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Positive divergence means the vector field is has a net negative flow out of the cell

$$\frac{1}{\partial \lambda} (\mathbf{V}_{x}) > 0$$

$$\frac{\partial}{\partial y} (\mathbf{V}_{y}) > 0$$

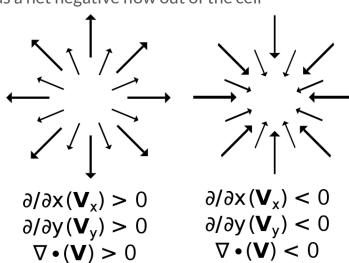
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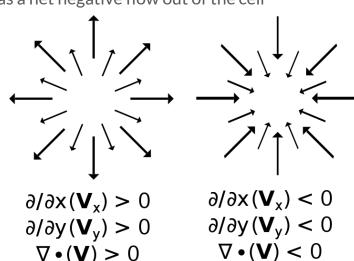
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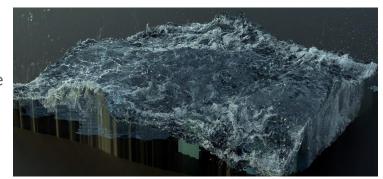
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Negative divergence means the VF has a net positive flow into the cell

Divergence free means no net flow through the cell. Makes sense, means no compression or lost matter for incompressible fluids

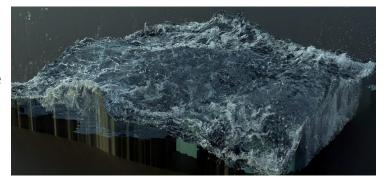


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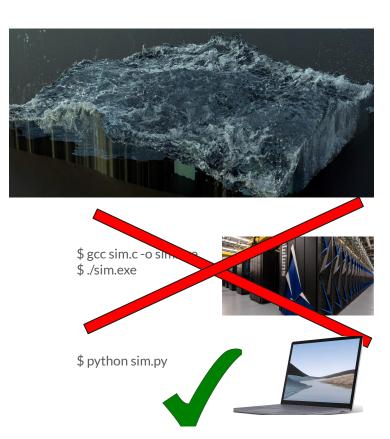
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A drawback of this is that fluid flow (Navier-Stokes equation) is highly non-linear.



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These methods aim to speed up simulations by using simplified representations, which have all been linear this far.

A drawback of this is that fluid flow (Navier-Stokes equation) is highly non-linear.

The authors use a CNN-based approach as a novel non-linear ROM for fluid simulation.



#### Goal

The primary goal for Deep Fluids is to perform fluid flow simulation (approximation) efficiently (low computation/memory requirement). Both 2D and 3D incompressible and compressible fluids are desired.

To do this, they use a CNN-based approach as an ROM for fluid simulations.

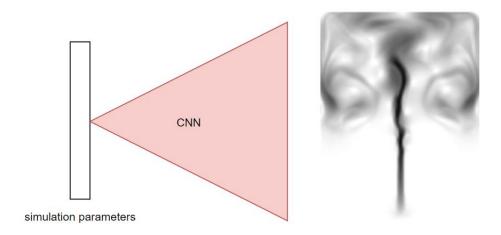
The authors suggest the non-linearities that neural networks have will allow the ROM to do well for the non-linear fluid data.

Primary goal is to train a CNN that approximates the original velocity field data set. The datasets can be parameterized (smoke cloud source, water drop starting position, etc...)

Given some parameters, we want to construct the vector field for the data.

Parameters might include:

Time, previous velocity field, viscosity, smoke plume origin, gravity, smoke speed, etc...

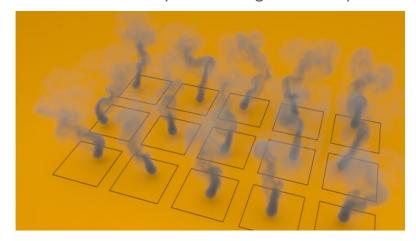


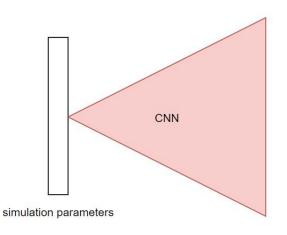
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Parameters might include:

Time, previous velocity field, viscosity, smoke plume origin, gravity, smoke speed, etc...

<u>Problem:</u> what if these change over time? For instance, if the smoke plume source moves around. Then the number of parameters grow linearly with the time, creating intractably large parameter space.

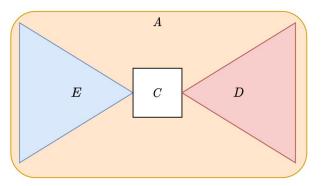






This is where the autoencoder is introduced - represent the parameters with a latent space

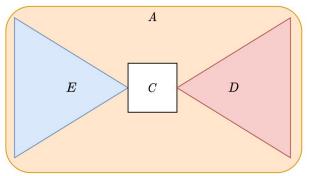
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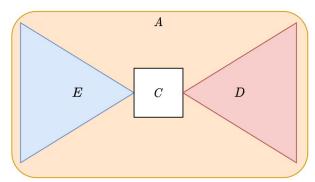
But, they still want manual control over some parameters, so they supervise some parameters in the latent space



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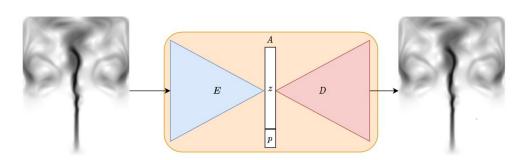
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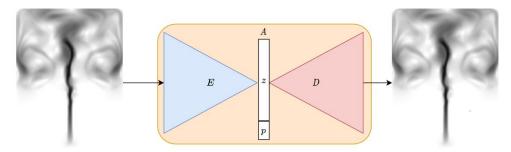
Solution:

$$C = [z, p]$$

z represents arbitrary features (unsupervised) p is supervised and represents the smoke plume source (0.5)

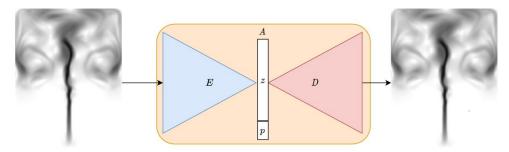


Now, each frame can be reduced to a latent space encoding parameters about the frame



This allows us to do our frame generation from the latent space, which is a compressed representation

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But what about the next timesteps? How do we simulate the evolution of a fluid over time?

### A generative fluid model

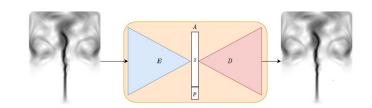
#### Time integration network

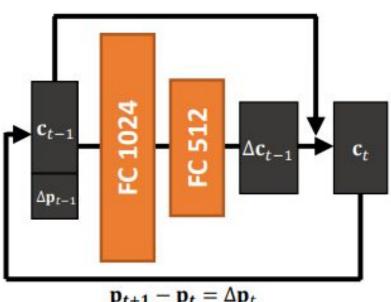
They create a second network that tries to replicate a simulation, but in the latent space.

Learns the change in the latent vector given the current latent vector

Note: p is our controlled parameters that we must choose ourselves. That is why it is not a part of the output of the network. We append it ourselves.

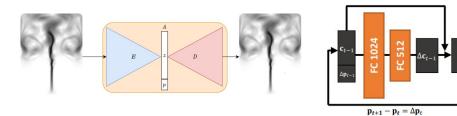
This allows us to change some parameter over time to see different output.



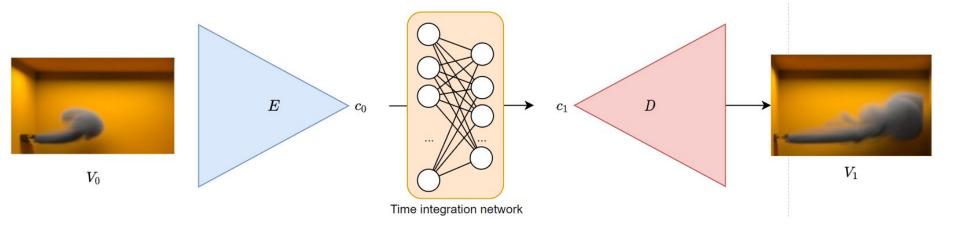


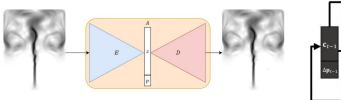
$$\mathbf{p}_{t+1} - \mathbf{p}_t = \Delta \mathbf{p}_t$$

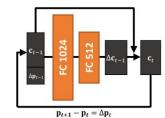
## A generative fluid model



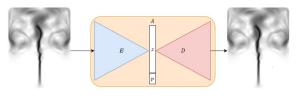
Big picture

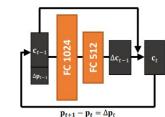






$$A(x) = D(E(x)) = x$$

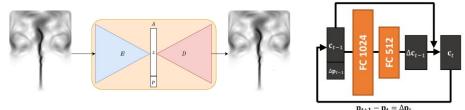




# A(x) = D(E(x)) = x

#### Compressible fluid loss:

$$L(A(x)) = ||x - A(x)||_1$$



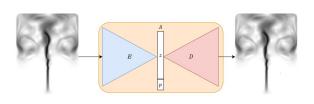
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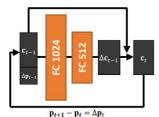
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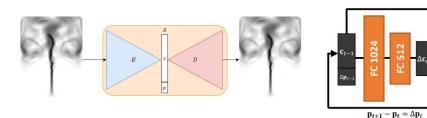
<u>Incompressible fluid loss:</u>

$$L(A(x)) = ||x - \nabla \times A(x)||_1$$

The curl of A(x)

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Curl in  $\mathbb{R}^2$ 

$$curl(ec{R}) = 
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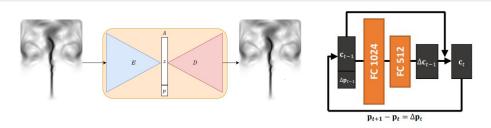
Curl in R<sup>2</sup> is the rotation around the z-axis (scalar field)

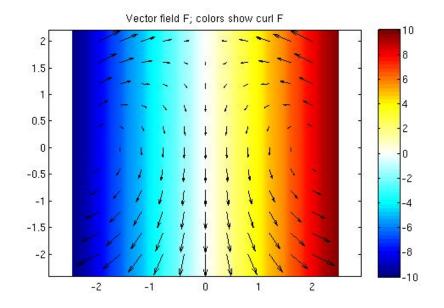
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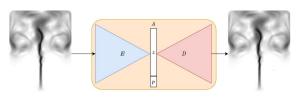
Positive curl is counter-clockwise rotation Negative curl is clockwise rotation

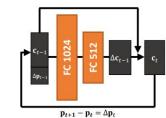




#### <u>Incompressible fluid loss:</u>

$$L(A(x)) = ||x - 
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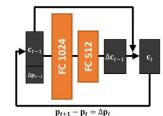




Curl in  $\mathbb{R}^3$ 

$$curl(ec{R}) = 
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 is the rotation

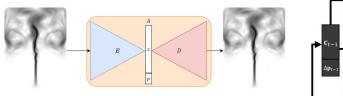
Curl in R<sup>3</sup> is similar with each term identifying the rotation around some axis

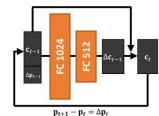


#### Incompressible fluid loss:

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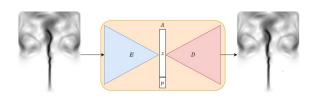
So why use the curl of the output of the network?

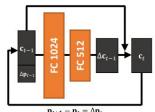




Identity:

$$\nabla \cdot (\nabla \times F) = 0$$



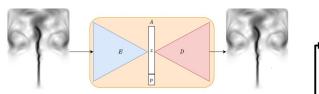


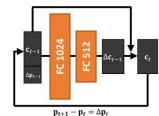
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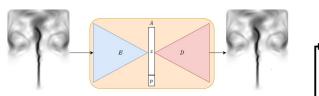


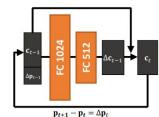


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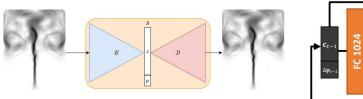
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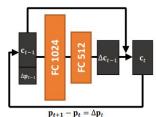




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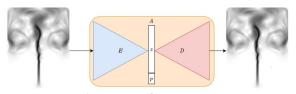
$$\begin{split} & \nabla \cdot \left( \nabla \times \boldsymbol{F} \right) = \boldsymbol{0} \\ & \nabla \times \vec{V} = [\frac{\partial \vec{V}_z}{\partial y} - \frac{\partial \vec{V}_y}{\partial z}, \frac{\partial \vec{V}_x}{\partial z} - \frac{\partial \vec{V}_z}{\partial x}, \frac{\partial \vec{V}_y}{\partial x} - \frac{\partial \vec{V}_x}{\partial y}] \\ & \nabla \cdot (\nabla \times V) = \nabla \cdot ([\frac{\partial \vec{V}_z}{\partial y} - \frac{\partial \vec{V}_y}{\partial z}, \frac{\partial \vec{V}_x}{\partial z} - \frac{\partial \vec{V}_z}{\partial x}, \frac{\partial \vec{V}_y}{\partial x} - \frac{\partial \vec{V}_x}{\partial y}]) \end{split}$$

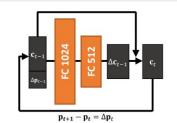




#### Identity:

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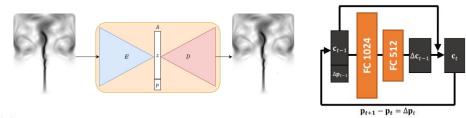




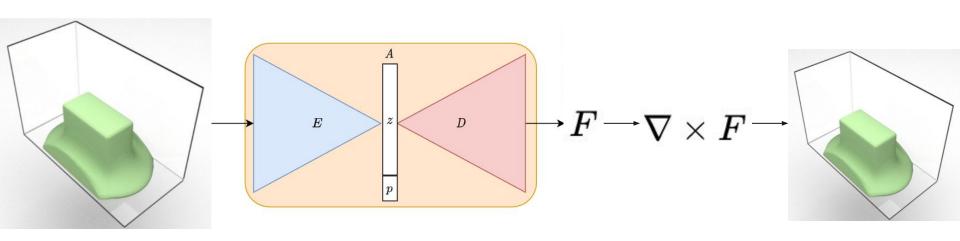
If we teach the network to generate this *stream function*, and then take the curl, the output is guaranteed to be divergence free

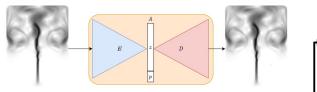
Thus, they call this a stream function loss.

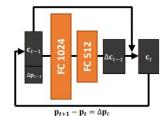
$$\nabla \cdot (\nabla \times F) = 0$$



$$L(A(x)) = ||x - \nabla \times A(x)||_1$$



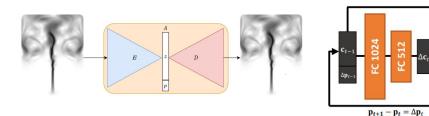




#### **Gradient loss:**

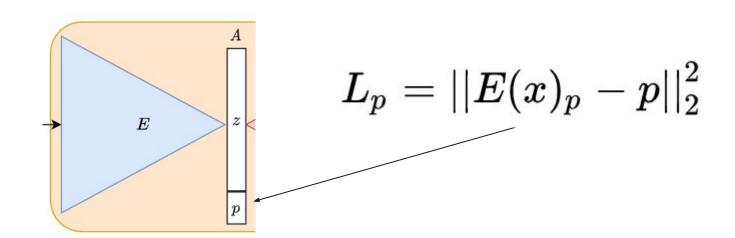
Velocity gradient encodes vorticity, shearing, and divergence.

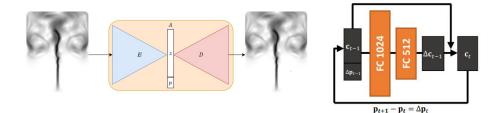
$$L_
abla = ||
abla x - 
abla A(x)||_1$$



#### Controlled parameter loss:

Force some parameters in the AE latent space to be controlled



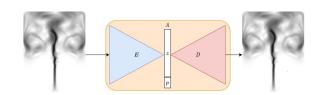


Full autoencoder loss

$$L=L_{L1}+L_{
abla}+L_{p}$$

$$L_{L1} = ||x-A(x)||_1 \qquad L_
abla = ||
abla x - 
abla A(x)||_1 \qquad L_p = ||E(x)_p - p||_2^2$$

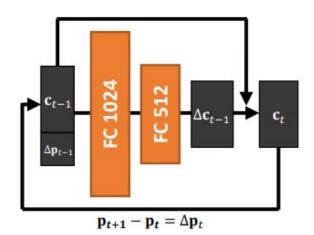
When training on incompressible fluids, define A(x) as the curl of the autoencoder output.



Temporal inference network

w=30 is used

$$L_T(\mathbf{x}_t,...,\mathbf{x}_{t+w-1}) = \frac{1}{w} \sum_{i=t}^{t+w-1} ||\Delta \mathbf{z}_i - T_i||_2^2,$$



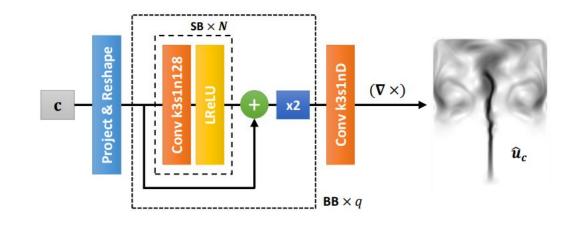
#### **Architecture - Encoder/Decoder**

Decoder architecture (encoder is symmetric)

SB = Small Blocks BB = Big Blocks

$$c = 16$$
  
 $N = 4 \text{ or } 5$   
 $q = \log_2(d_{max}) - 3$ 

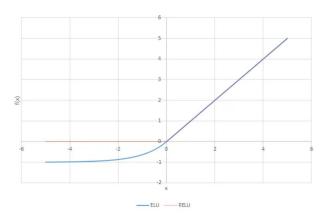
Ex. 
$$d_{max} = 128 \rightarrow q = 7-3 = 4$$

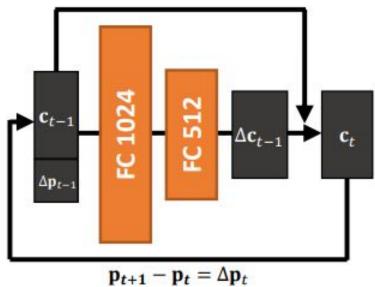


### **Architecture - Temporal inference network**

3 fully connected

**ELU** activation function Batchnorm and dropout layers (p=0.1) to avoid overfitting

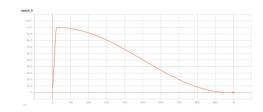




#### Results

#### Specifics:

300,000 iterations per AE network, 30,000 for time network Learning rate scheduled with cosine annealing decay Batch size: 1 for 3D, 8 for 2D



Sims performed in Mantaflow

Data is all normalized to [-1, 1] via maximum absolute value

#### Results - 2D smoke

Parameters: source width(5 samples) and source x

position(21 samples)

Simulation length: 200 frames

Resolution: 96x128

Training data: 21000 unique frames

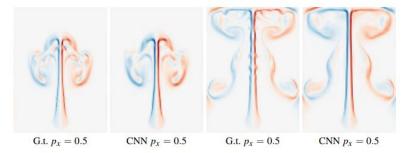
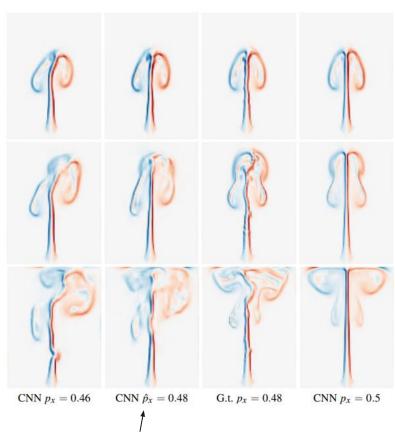


Figure 6: Vorticity plot of a 2-D smoke simulation with direct correspondences to the training data set for two different times. The RdBu colormap is used to show both the magnitude and the rotation direction of the vorticity (red: clockwise). Our CNN is able to closely approximate ground truth samples (G.t.).



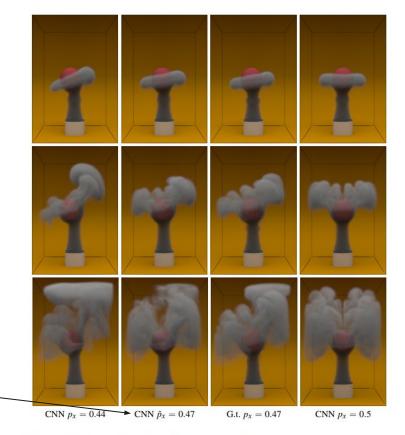
Not in training data

#### Results - 3D smoke sphere obstacle

Parameters: sphere position(10 samples)

Resolution: 64x96x64

Simulation length: 660 frames



Not in training data

#### Results - 3D smoke inflow and buoyancy

Parameters: inflow velocities (5), buoyancy values (3)

Simulation length: 250 frames

Resolution: 112x64x32

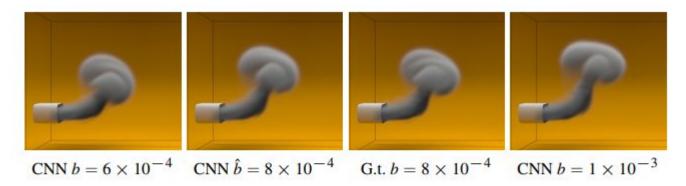


Figure 9: Reconstructions of the rising plume scene (left and right), reconstruction for an interpolated buoyancy value ( $\hat{b} = 8 \times 10^{-4}$ ) (second image) and the corresponding ground truth (third image).

#### Results - 3D smoke rotating

Parameters: inflow velocities (5), buoyancy values (3)

Simulation length: 500 frames

Resolution: 48x72x48

Smoke rotates periodically

every 100 frames

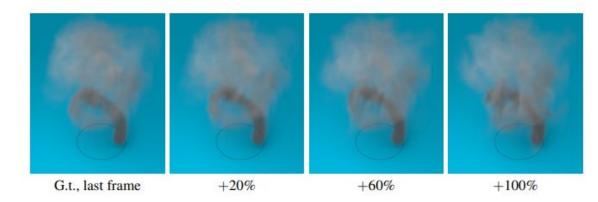


Figure 10: Time extrapolation results using our latent space integration network. The left image shows the last frame of the ground truth simulation. The subsequent images show results with time extrapolation of +20%, +60% and +100% of the original frames.

#### Results - 3D smoke moving

Simulation length: 400 frames

Resolution: 48x72x48 Number of sims: 200

Each sim moves the smoke source around randomly using Perlin noise. Evaluated by using time network to generate plausible flow.

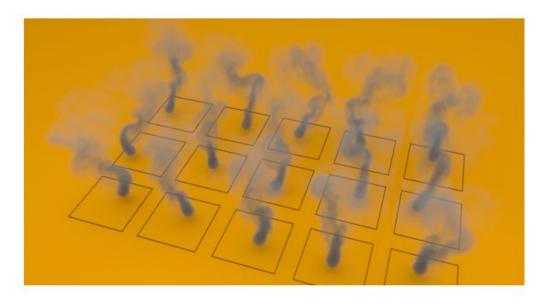


Figure 11: Example simulations of the moving smoke scene used for training the extended parameterization networks.

### Results - 3D liquid spheres

Parameters: initial distance of the spheres (5), drop angles (10)

Simulation length: 150 frames

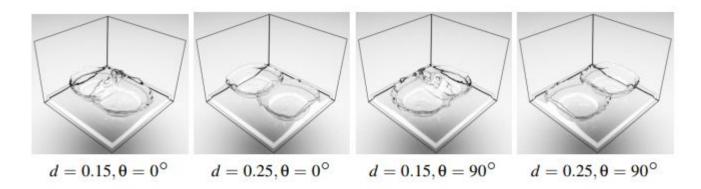


Figure 13: Training samples for the liquid spheres scene. In total we used 50 simulation examples with varying distances and angles.

#### Results - 3D liquid spheres

Parameters: initial distance of the spheres (5), drop angles (10)

Simulation length: 150 frames

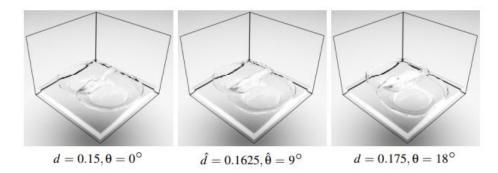


Figure 14: CNN-generated results with parameter interpolation for the liquid spheres example. While the far left and right simulations employ parameter settings that were part of the training data, the middle example represents a new in-between parameter point which is successfully reconstructed by our method.

#### Results - 3D liquid viscous dam break

Parameters: viscosity strength (4)

Simulation length: 150 frames

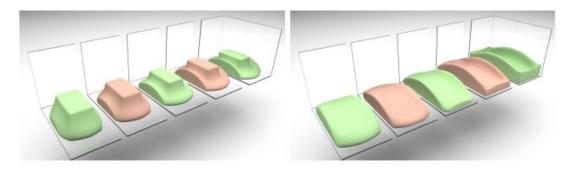


Figure 15: Snapshots of a CNN reconstructed dam break with different viscosity strengths for two different frames. Green liquids denote correspondences with ground truth ( $\mu = 2 \times [10^{-4}, 10^{-3}, 10^{-2}]$ , back to front) while pink ones are interpolated ( $\hat{\mu} = 2 \times [5^{-3}, 5^{-2}]$ , back to front).

### Results - 3D liquid viscous dam break

Parameters: viscosity strength (4)

Simulation length: 150 frames

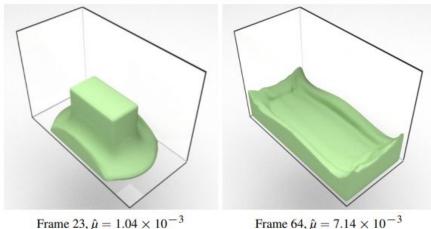


Figure 16: Reconstruction result using a time varying viscosity strength. In the first few frames the liquid quickly breaks into the container. As the simulation advances, the viscosity increases and the liquid sticks to a deformed configuration.

#### **Results - training**

- Batch normalization didn't help
- Other rescaling techniques might do better
  - Standardization, histogram equalization
- Training was stable for all trials
- Training took longer with liquid to have high quality surfaces than it took with the gases

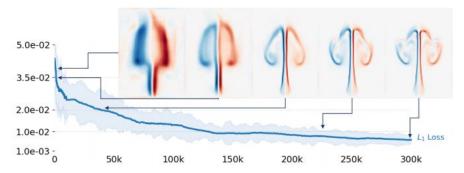


Figure 17: Convergence plot of the  $L_1$  loss for the 2-D smoke sequence from Figure 7.

#### **Results - compression and ROM**

#### Efficiency:

- Up to 700x faster than simulating via CPU
- Can efficiently create many timesteps at once (batching) while a sim has to do one step at a time

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#### Efficiency:

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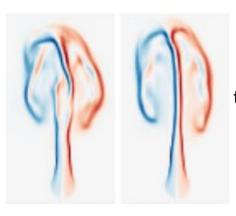
#### Compression:

- Compression rates of up to 1300x, based on the network taking a static 30MB.
  - Previous ROMs only achieved 14x.
- Outperforms FZIP (compression algorithm), which only achieves 4x with a mean absolute error comparable to Deep Fluids

### Results - quality of reconstruction

Highly dependent on training data and proximity to a nearby parameter setting.

Less training data



More training data

 Training with incompressible loss gives better results.

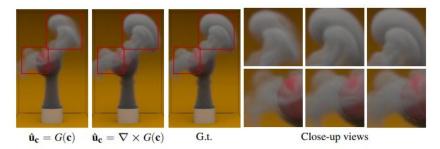


Figure 18: Comparisons of the results from networks trained on our compressible loss, incompressible loss and the ground truth, respectively. On the right sequence we show the highlighted images from the simulations on the left. We notice that the smoke patterns from the incompressible loss are closer to ground truth simulations.

#### Results - quality of reconstruction

Attempts to not penetrate boundaries

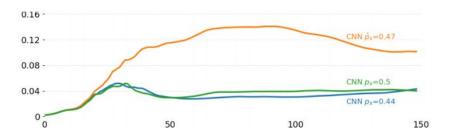


Figure 20: Mean absolute error plot of velocity penetration for the smoke obstacle example. Though errors in interpolated samples are a bit higher than those of reconstructed samples, they do not exceed 1% of the maximum absolute value of the data set.

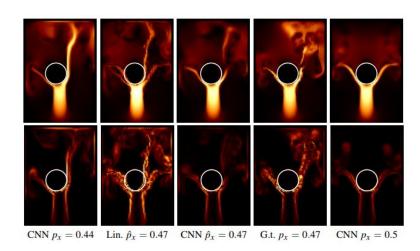


Figure 19: Slice views of the last row of Fig. 8. The color code represents the velocity (top) and vorticity (bottom) magnitudes. The second column shows a linear interpolation of the input. Despite the absence of any constraints on boundary conditions, our method (third column) preserves the shape of the original sphere obstacle, and yields significantly better results than the linear interpolation.

#### Results - summary

	Grid		Simulation	Eval. Time	Speed Up	Data Set	Network	Compression	Training
Scene	Resolution	# Frames	Time (s)	(ms) [Batch]	(×)	Size (MB)	Size (MB)	Ratio	Time (h)
Smoke Plume	96 × 128	21,000	0.033	0.052 [100]	635	2064	12	172	5
Smoke Obstacle	$64 \times 96 \times 64$	6,600	0.491	0.999 [5]	513	31143	30	1038	74
Smoke Inflow	$112 \times 64 \times 32$	3,750	0.128	0.958 [5]	128	10322	29	356	40
Liquid Drops	$96 \times 48 \times 96$	7,500	0.172	1.372 [3]	125	39813	30	1327	134
Viscous Dam	$96 \times 72 \times 48$	600	0.984	1.374 [3]	716	2389	29	82	100
Rotating Smoke	$48 \times 72 \times 48$	500	0.08	0.52 [10]	308	995	38	26	49
Moving Smoke	$48 \times 72 \times 48$	80,000	0.08	0.52 [10]	308	159252	38	4191*	49

Table 1: Statistics for training data sets and our CNN. Note that simulation excludes advection and is done on the CPU, while network evaluation is executed on the GPU with batch sizes noted in brackets. In case of liquids, the conjugate gradient residual threshold is set to  $1e^{-3}$ , while for smoke it is  $1e^{-4}$ . For the Rotating and Moving Smoke scenes, the numbers for training time and network size include both the autoencoder and latent space integration networks.

<sup>\*</sup> We optimize the network for subspace simulations rather than the quality of reconstruction, so we do not take this number into account when evaluating the maximal compression ratio.

#### Limitations

- Extrapolation is limited with the time network
- Cannot recreate arbitrary velocity fields that aren't similar to the training dataset
- No physical constraints on boundaries
- Temporal jittering due to no gradient loss
- Number of control parameters is limited
- No quantitative metrics shown
- Artifacts appear when not near trained parameter settings

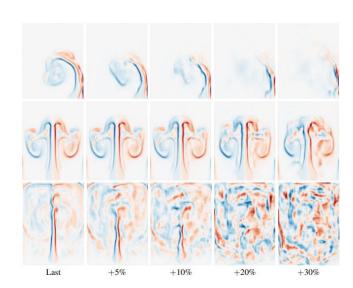


Figure 21: 2-D smoke plume extrapolation results (from t. to b.: position, inflow width, time) where only the generative network is used. Plausible results can be observed for up to 10% extrapolation.

# The End