

Nanocubes for Real-Time Exploration of Spatiotemporal Datasets

Lauro Lins

James T. Klosowski

Carlos Scheidegger

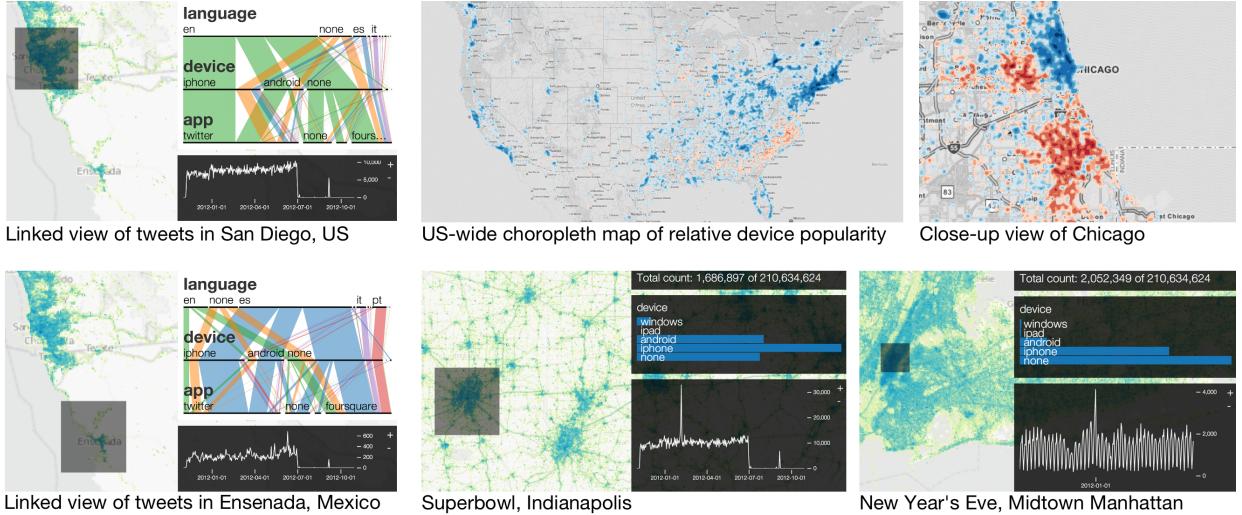


Fig. 1. Example visualizations of 210 million public geolocated Twitter posts over the course of a year. The data structure we propose enables real-time (these images above were rendered faster than the typical screen refresh rate) visual exploration of large, spatiotemporal, multidimensional datasets. The visual encodings built using *nanocubes* are within a controllable difference to ones rendered by a traditional linear scan over the dataset. They naturally support linked navigation and brushing, and include choropleth maps, time series over arbitrary regions and scales of space and time, parallel sets, histograms, and binned scatterplots. The color scale of the choropleth map is a diverging scale in which blue corresponds to iPhones being relatively more popular, and red corresponds to higher relative popularity of Android devices.

Abstract—Consider real-time exploration of large multidimensional spatiotemporal datasets with billions of entries, each defined by a location, a time, and other attributes. Are certain attributes correlated spatially or temporally? Are there trends or outliers in the data? Answering these questions requires aggregation over arbitrary regions of the domain and attributes of the data. Data cubes are a well-known aggregation operation in relational databases. In a sense, they precompute every possible aggregate query over the database. Data cubes are sometimes assumed to take a prohibitively large amount of space, and to consequently require disk storage. In contrast, we show how to construct a data cube that fits in a modern laptop’s main memory, even for billions of entries; we call this data structure a *nanocube*. We present algorithms to compute and query a nanocube, and show how it can be used to generate well-known visual encodings such as heatmaps, histograms, and parallel coordinate plots. When compared to exact visualizations created by scanning an entire dataset, nanocube plots have bounded screen error across a variety of scales, thanks to a hierarchical structure in space and time. We demonstrate the effectiveness of our technique on a variety of real-world datasets, and present memory, timing, and network bandwidth measurements. We find that the timings for the queries in our examples are dominated by network and user-interaction latencies.

Index Terms—Data Cube, Data Structures, Interactive Exploration

1 INTRODUCTION

As datasets get larger, real-time visualization becomes more difficult. Consider a dataset with a billion entries. If we compute a summary of the dataset and visualize it, the natural question becomes “does the summary represent the data well?” and the problem has simply shifted to “how can we visualize one billion residuals”? Even drawing the simplest scatterplot is not straightforward. If we decide to produce the visualization by scanning the rows of a table, we will either need non-trivial parallel rendering algorithms or significant time to produce a drawing. Neither of these solutions scales well with dataset size.

Data cubes are structures that perform aggregations across every possible set of dimensions of a table in a database, to support quick exploration [14, 30]. Many visualization systems are built on top of data cubes, concretely or conceptually. Still, only recently have researchers started to examine data cube creation algorithms in the context of information visualization [32, 17, 20].

Data cubes are often problematic in that they can take prohibitively large amounts of memory as the number of dimensions increases. In Section 4, we show how to construct a data cube that fits in the main memory of a modern laptop computer or workstation, extending the work of Sismanis et al. [30]. In addition, the query times to build the visual encodings in which we are interested will be at most proportional to the size of the output, which is bounded by the number of screen pixels (within a small factor). This is an important observation: the time complexity of a visualization algorithm should ideally be bounded by the number of pixels it touches on the screen. Our technique enables *real-time* exploratory visualization on datasets that are *large, spatiotemporal, and multidimensional*. Because the speed of

• Authors are with AT&T Research, Florham Park, NJ; {llins, jklosow, cscheid}@research.att.com.

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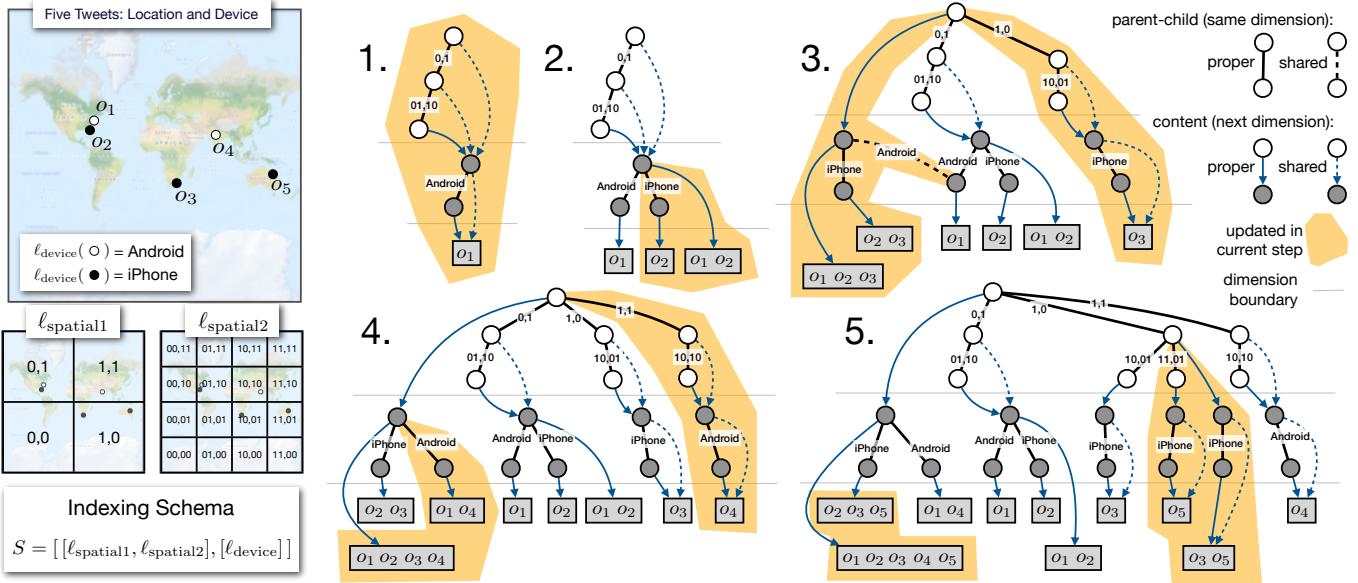


Fig. 2. An illustration of how to build a nanocube for five points $[o_1, \dots, o_5]$ under schema S . The complete process is described in Section 4.

our data cube structure hinges partly on it being small enough to fit in main memory, we call them *nanocubes*.

By *real-time*, we mean extremely fast queries: query times average under a millisecond for a single thread running on a computer that ranges from a laptop, to a workstation, to a server-class computing node (Section 6). By *large*, we mean that the datasets we support have millions to billions of entries.

By *spatiotemporal*, we mean that nanocubes support queries typical of spatial databases, such as counting events in a spatial region that can be either a rectangle covering most of the world, or a heatmap of activity in downtown San Francisco (Section 4.3.1). By the same token, nanocubes support temporal queries at multiple scales, such as event counts by hour, day, week, or month over a period of years (Section 4.3.3). Data cubes in general enable the Visual Information-Seeking Mantra [28] of “Overview first, zoom and filter, then details-on-demand” by providing rollup summaries over all projections and letting users drill down by expanding the wanted dimensions. Nanocubes also provide overviews, filters, zooming, and details-on-demand inside the spatiotemporal dimensions themselves.

By *multidimensional*, we mean that besides latitude, longitude, and time, each entry can have additional attributes (see section 6) that can be used in query selections and rollups.

As we will show, nanocubes support queries that lend themselves very well to building visual encodings which are fundamental building blocks of interactive visualization systems, such as scatterplots, histograms, parallel coordinate plots, and choropleth maps. In summary, we contribute:

- a novel data structure that improves on the current state of the art data cube technology to enable real-time exploratory visualization of multidimensional, spatiotemporal datasets;
- algorithms to query the nanocube and build linked and brushable visual encodings commonly found in visualization systems; and
- case studies highlighting the strengths and weaknesses of our technique, together with experiments to measure its utilization of space, time, and network bandwidth.

2 RELATED WORK

Relational databases are so widespread and fundamental to the practice of computing that they were a natural target for information visualization almost since the field’s inception [19]. Mackinlay’s Automatic

Presentation Tool is the breakthrough result that critically connected the relational structure of the data with the graphical primitives available for display [22] and ultimately lead to data cube visualization tools like Polaris [33, 34] and Show Me [23]. Nanocubes are specifically designed to speed up queries for spatiotemporal data cubes, and could eventually be used as a backend for these types of applications.

In contrast, some of the work in large data visualization involves shipping the computation and data to a cluster of processing nodes. While parallelism is an attractive option for increasing throughput, it does not necessarily help achieve *low latency*, which is essential for fluid interactions with a visualization tool. As a result, sophisticated techniques such as query prediction become necessary [5]. Leveraging the enormous power of graphics processing units has also become popular [24, 20], but without algorithmic changes, linear scans through the dataset will still be too slow for fluid interaction, even with GPUs.

Another popular way to cope with large datasets is through sampling. Statistical sampling can be performed on the database backend [25, 1, 9, 13], or on the front-end [10]. Still, the techniques we introduce with nanocubes can produce results quickly and exactly (to within screen precision) without requiring approximations, which we believe is preferable. In addition, as Liu et al. argue, sampling by itself is not sufficient to prevent overplotting, and might actually mask important data outliers [20].

Fekete and Plaisant have proposed modifications of traditional visual encodings which use the computer screen more efficiently, and so scale better with dataset size [12]. Still, the proposal requires a traversal of all input data points, which is not a feasible approach at the scale which we want to approach here. Carr et al. were among the first to propose techniques replacing a scatterplot with an equivalent density plot [4]; nanocubes can be seen as a data structure to enable these visualizations at a variety of dataset sizes and scales.

Careful data aggregation [16], then, appears to be one of the few scalable solutions for low-latency large data graphics. While Elmquist and Fekete propose variations of visualization techniques that include aggregation as a first-class citizen [11], in this paper we show how to issue queries such that at the screen resolution in which the application is operating, the result is indistinguishable (or close to) from a complete scan through the dataset. We note that over-aggressive aggregation itself introduces potential discrepancies between the visualization and the dataset, and there are proposals to understand this [8].

We are interested in bounding the difference between our visual encoding and a visual encoding that would traverse the entirety of the data by the size of the screen, i.e. the number of pixels in it. Related to

```

1: function NANOCUBE( $[o_1, o_2, \dots, o_n]$ ,  $S, \ell_{\text{time}}$ )  $\triangleright n > 0$ 
2:    $nano\_cube \leftarrow \text{NODE}()$   $\triangleright$  New empty node
3:   for  $i = 1$  to  $n$  do
4:      $updated\_nodes \leftarrow \emptyset$ 
5:     ADD( $nano\_cube, o_i, 1, S, \ell_{\text{time}}, updated\_nodes$ )
6:   end for
7:   return  $nano\_cube$ 
8: end function

1: function TRAILPROPERPATH( $root, [v_1, \dots, v_k]$ )
2:    $stack \leftarrow \text{STACK}()$   $\triangleright$  New Empty Stack
3:   PUSH( $stack, root$ )
4:    $node \leftarrow root$ 
5:   for  $i = 1$  to  $k$  do
6:      $child \leftarrow \text{CHILD}(node, v_i)$ 
7:     if  $child = \text{null}$  then
8:        $child \leftarrow \text{NEWPROPERCHILD}(node, v_i, \text{NODE}())$ 
9:     else if ISSHAREDCCHILD( $node, child$ ) then
10:       $child \leftarrow \text{REPLACECHILD}(node,$ 
11:         $child, \text{SHALLOWCOPY}(child))$ 
12:     end if
13:     PUSH( $stack, child$ )
14:      $node \leftarrow child$ 
15:   end for
16:   return  $stack$ 
17: end function

1: function SHALLOWCOPY( $node$ )
2:    $node\_sc \leftarrow \text{NODE}()$ 
3:   SETSHAREDCONTENT( $node\_sc, \text{CONTENT}(node)$ )
4:   for  $v$  in CHILDRENLABELS( $node$ ) do
5:     NEWSHAREDCCHILD( $node\_sc, v, \text{CHILD}(node, v)$ )
6:   end for
7:   return  $node\_sc$ 
8: end function

```

```

1: procedure ADD( $root, o, d, S, \ell_{\text{time}}, updated\_nodes$ )
2:    $[\ell_1, \dots, \ell_k] \leftarrow \text{CHAIN}(S, d)$ 
3:    $stack \leftarrow \text{TRAILPROPERPATH}(root, [\ell_1(o), \dots, \ell_k(o)])$ 
4:    $child \leftarrow \text{null}$ 
5:   while  $stack$  is not empty do
6:      $node \leftarrow \text{POP}(stack)$ 
7:      $update \leftarrow \text{false}$ 
8:     if  $node$  has a single child then
9:       SETSHAREDCONTENT( $node, \text{CONTENT}(child)$ )
10:      else if CONTENT( $node$ ) is null then
11:        SETPROPERCONTENT( $node,$ 
12:          ( $d = \text{dim}(S)$ ) ?
13:            SUMMEDTABLETIMESERIES() : NODE())
14:          update  $\leftarrow \text{true}$ 
15:        else if CONTENTISSHARED( $node$ ) and
16:          CONTENT( $node$ ) not in  $updated\_nodes$  then
17:            SETPROPERCONTENT( $node,$ 
18:              SHALLOWCOPY(CONTENT( $node$ )))
19:            update  $\leftarrow \text{true}$ 
20:        else if CONTENTISPROPER( $node$ ) then
21:          update  $\leftarrow \text{true}$ 
22:        end if
23:        if update then
24:          if  $d = \text{dim}(S)$  then
25:            INSERT(CONTENT( $node$ ),  $\ell_{\text{time}}(o)$ )
26:          else
27:            ADD(CONTENT( $node$ ),  $o, d+1, updated\_nodes$ )
28:          end if
29:        end if
30:        child  $\leftarrow node$ 
31:      end while
32:    end procedure

```

Fig. 3. Pseudo-code of an algorithm to build nanocubes.

this, pixel-oriented techniques [18] have been investigated. However, these tend to focus on the development of new visual encodings, while in this paper we show how to create the already well-known and established encodings with low error, high performance and interactivity.

Our technique is most closely related to the work of Sismanis et al. [29, 30, 31]. Nanocubes improve upon their work in two fundamental directions. First, we develop a model for spatiotemporal data cubes that exploits unique characteristics of space and time to get a good compromise between space usage and efficiency of queries (Sections 4.2.1 and 6). Second, we show how these structures enable the visualizations which are common in interactive tools (Section 4.3).

There have been recent efforts to build data cube structures specifically suited for visualization. Crossfilter [32] is based on the clever observation that many queries in interactive visualization are incremental: assuming that previous results are available, the results needed for the next query can be quickly computed. Unfortunately, we do not see how this would work for the multiscale queries necessary in a spatiotemporal setting. Just as recently, Kandel et al. proposed Datavore, a column-oriented database that supports fast data cube queries [17], and Liu et al. leverage graphics hardware in imMens, achieving extremely fast queries over large data [20]. We defer direct comparison of nanocubes to Datavore and imMens until Section 7.

3 DATA CUBES

Following common practice, we will call the table in Figure 4 a *relation*, its columns *attributes*, its lines *records*, and its entries *values*. An *aggregation* represents the idea of selecting a certain group of records from a relation and summarizing this group using an *aggregation function* (e.g. count, sum, max, min). For example, a possible aggregation for the relation A could be to select all its records and summarize those using count, yielding five as the *aggregation result*. If we allow

a special value *All* to be a valid attribute value, we could represent this aggregation as relation B in Figure 4. A record that contains the special value *All* is an *aggregation record*. Using this notation, it is easy to understand some conventional ways of describing aggregations for a given relation: GROUP_BY, CUBE, and ROLL_UP.

A GROUP_BY operation is one in which a relation is derived from a base relation given a list of attributes and an aggregation function. For example, GROUP_BY on attributes *Device* and *Language* with the count aggregation function results in the relation C in Figure 4. Note that for every different combination of values present in the attributes of a base relation, an aggregation record is added to the resulting relation. In our running example, these combinations are (Android, en), (iPhone, en), and (iPhone, ru).

Relation A			Cube on Device, Language D		
Country	Device	Language	Country	Device	Language
US	Android	en	All	All	All
US	iPhone	ru	All	Android	All
South Africa	iPhone	en	All	iPhone	All
India	Android	en	All	All	en
Australia	iPhone	en	All	All	ru

Aggregation B			
Country	Device	Language	Count
All	All	All	5

Group By on Device, Language C			
Country	Device	Language	Count
All	Android	en	2
All	iPhone	en	2
All	iPhone	ru	1

Equivalent to Group By on all possible subsets of {Device, Language}
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Fig. 4. A sample relation and its associated aggregation operators.

Natural language query	s	c	t	URL
count of all Delta flights	R	U	R	/where/carrier=Delta
count of all Delta flights in the Midwest	R	Midwest	R	/region/Midwest/where/carrier=Delta
count of all flights in 2010	R	U	R	/field/carrier/when/2010
time-series of all United flights in 2009	R	U	D	/tseries/when/2009/where/carrier=United
heatmap of Delta flights in 2010	D	tile0	R	/tile/tile0/when/2010/where/carrier=Delta

Fig. 5. A simplified set of queries supported by nanocubes. The column s represents space; t , time; c , category. R means “rollup”, D means “drilldown”. The value next to R or D contains the subset of that dimension’s domain being selected. U represents the entire domain (“universe”).

The CUBE operation is the result of collecting all possible GROUP_BY aggregations into a single relation for a given list of attributes (i.e. 2^n GROUP_BYS for n input attributes). In our running example, the CUBE for count on *Device* and *Language* is the union of four GROUP_BYS: on (1) no attributes; on (2) *Device* only; on (3) *Language* only; and (4) on *Device* and *Language*, shown in relation D in Figure 4. Finally, a ROLL_UP is a constrained version of the CUBE operation where the order of the input attributes is important. A ROLL_UP on *Device* and *Language* (in this order) means the union of GROUP_BYS on: (1) no attributes; (2) *Device*; and (3) *Device* and *Language*, but does not include the GROUP_BY on *Language* only. As the results of GROUP_BYS, CUBEs and ROLL_UPs can be seen as relations, we can naturally compose such operators (e.g. a ROLL_UP_CUBE).

4 NANOCUBE: A COMPACT, SPATIOTEMPORAL DATA CUBE

Data visualizations in a computer are necessarily bounded by display size, and so we would like to be able to quickly collect subsets of the dataset that would end up in the same pixel on the screen. However, spatiotemporal navigation is inherently multiscale. The same data structure should support quick indexing for a visualization over multiple years of time series and for drilling down into one particular hour or day. Similarly, the data cube should support aggregation queries over vast spatial regions covering entire continents, as well as very narrow queries covering only a few city blocks.

The database notion of ROLL_UP, in a sense, aligns nicely with the notion of *Level of Detail*. For example, if the records of a table (relation) contain a location attribute, one can design a ROLL_UP query whose resulting relation encodes the same information as the one encoded in a level of detail data structure. More concretely, suppose ℓ_1, \dots, ℓ_k are attributes computed from the original location attribute and yield “quadtree addresses” of increasingly higher levels of detail (from 1 to k). A ROLL_UP query on these (computed) attributes results in, essentially, the same information as the one contained in a quadtree (given that we are keeping the same summary in both, e.g. count).

The second important notion in the design of nanocubes is the idea that we want to combine aggregations of independent dimensions at independent levels of detail. For example we might want to know for a whole country, what is the spatial distribution of tweets generated by an iPhone: coarse on the spatial dimension, but specific on the device dimension. Conversely, we might want to know the distribution of tweets (coarse on device) in a small city block (fine in space). In relational database terminology, this model has a name: it is a CUBE of ROLL_UP, or a ROLL_UP_CUBE. With the terminology set, we can state: a *nanocube* is a data structure to efficiently store and query spatiotemporal ROLL_UP_CUBE. Besides implementation tricks, the main difference between nanocubes and previously published sparse coalesced data cubes such as Dwarf cubes [29] is in the design of aggregations across spatiotemporal dimensions (see Sections 4.3.1 and 4.3.3). Next, we present a formal description of the components that make up our nanocube index, pseudo-code for building nanocubes, an illustrated example, and how queries are made against our index.

4.1 Definitions

Let O be a set of objects. A *labeling function* $\ell : O \rightarrow L$ associates a *label value* to the objects of O . We can think of ℓ as an attribute in a relational database. In connection with the level of detail discussion above, if ℓ_1 and ℓ_2 are two labeling functions for O , we say ℓ_1 is *coarser than* ℓ_2 or that ℓ_2 is *finer than* ℓ_1 if for any two objects $o, o' \in O$

the implication $\ell_2(o) = \ell_2(o') \Rightarrow \ell_1(o) = \ell_1(o')$ holds. We denote this fact by $\ell_1 \succcurlyeq \ell_2$.

A sequence of labeling functions $c = [\ell_1, \ell_2, \dots, \ell_k]$ for objects O is a *chain for O* if every labeling function is coarser than the next labeling function in the sequence: $\ell_i \succcurlyeq \ell_{i+1}$. The *number of levels* of a chain is defined by $levels(c) = |c| + 1$. An *indexing schema* for objects O consists of a sequence of chains $S = [c_1, c_2, \dots, c_n]$. The *dimension* of an indexing schema S is the length of its sequence of chains and is denoted by $dim(S)$. The *multiplicity* of a schema S is the product of its chains’ number of levels: $\mu(S) = \prod_{i=1}^n levels(c_i)$.

A *full assignment* for a sequence of labeling functions $[\ell_1, \ell_2, \dots, \ell_k]$ is a sequence of label values $[v_1, v_2, \dots, v_k]$ where v_i is a label value under ℓ_i . Any prefix of a full assignment for a sequence of labeling functions, including the empty one, is referred to as a *partial assignment*. Note that a *full assignment* is also a *partial assignment* since a sequence is also a prefix of itself. An *address* on a schema is a sequence of partial assignments for its chains, more formally, if $S = [c_1, c_2, \dots, c_n]$ is an indexing schema, then $a = [p_1, p_2, \dots, p_n]$ is an *address of S* if p_i is a partial assignment for chain c_i . The set of possible addresses of S is denoted by $addr(S)$.

The addresses of an object o under indexing schema S , denoted by $addr(o, S)$ are all the addresses in $addr(S)$ whose partial assignments are consistent with the label values associated to o and it is easy to see that the size of $addr(o, S)$ is always $\mu(S)$. Besides a schema S , the definition of a *nanocube* requires a separate labeling function, $\ell_{\text{time}} : O \rightarrow T$, which we refer to as the *time labeling function* since we use it to encode the temporal aspect of our datasets. Thus, a nanocube for objects o_1, \dots, o_n is denoted by:

$$\text{NANOcube}([o_1, \dots, o_n], S, \ell_{\text{time}})$$

A *key* in a nanocube is any pair (a, t) where $a \in addr(S)$ and corresponds to a full assignment (see definition above) and $t \in T$ is a possible time label. If we remove the requirement of a being a full assignment, we say that pair (a, t) is an *aggregate key*. Note that every key is also an aggregate key. The set of all possible keys and the set of all possible *aggregate keys* of a nanocube are respectively referred to as its *key space*, or K^* , and its *aggregate key space*, or K_a^* . The size of the key space, $|K^*|$, is referred to as its *cardinality*.

4.2 Building the Index

To ease the remaining exposition, we assume that a nanocube maps an aggregate key to a *count*. However, nanocubes support any kind of summary that is an algebra with weighted sums and subtractions, and thus works for any linear statistics, including means and variances.

The pseudo-code for building a nanocube is presented in Figure 3. The main idea of the algorithm is for every object o_i to first find the finest address of the schema S hit by this object, update the time series associated with this address and from there on update in a deepest first fashion, all coarser addresses also hit by o_i . Note that the content of the last dimension of schema S is always a time series and that is why, in line 21 of ADD, we insert the time label of the current object. The important trick used is to, when possible, allow for shared links across dimensions (dashed blue lines in Figure 2) and in the same dimension (dashed black connections). In real use cases this sharing is responsible for significant memory savings and enables exploring even larger datasets on small laptops. The functions not defined in the pseudo-code should have its semantics easy to understand from its name.

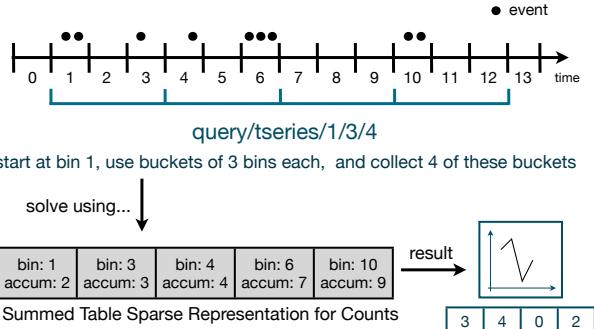


Fig. 6. An illustration of the summed-area table variant we use for our time series indexing scheme. Every node in Figure 2 stores an array of timestamped counts like the one in this figure.

4.2.1 Nanocube Example

Consider the scenario where an analyst is interested in understanding the spatiotemporal distribution of Twitter data (i.e. tweets), including which devices (e.g. iPhone, Android) people are using. Natural questions to ask include: Which device is more popular for tweeting? Is one device more popular in certain areas than in others? How has this popularity changed over time? We illustrate the construction of a nanocube built using Twitter data in Figure 2. For clarity, this example contains only five tweets o_1, \dots, o_5 , all ordered in time.

As shown on the top-left map of Figure 2, the first two tweets (o_1 and o_2) were sent from the east coast of the United States; the third tweet (o_3), from South Africa; the fourth tweet (o_4) was sent from Asia, and the fifth tweet (o_5) from Australia. Tweets o_1 and o_4 were sent from an Android device while o_2 , o_3 , and o_5 were sent from an iPhone device. The labeling functions ℓ_{device} , $\ell_{spatial1}$, and $\ell_{spatial2}$ as well as the schema of this nanocube, S , are all defined on the left part of this figure. The labeling ℓ_{device} assigns a device to each tweet and $\ell_{spatial1}$ and $\ell_{spatial2}$ assign a spatial label to each tweet. The tweet labels given by $\ell_{spatial1}$ and $\ell_{spatial2}$ are essentially addresses in a quadtree partition of a square. Note that $\ell_{spatial1}$ is coarser than $\ell_{spatial2}$. The right part of Figure 2 presents intermediate nanocubes generated by NANOCUBE (Figure 3) after each tweet is inserted.

4.3 Querying the Cube

Nanocubes support three distinct dimension types, which are always traversed in a fixed order: spatial, categorical, and finally temporal. Before describing queries for each of these specific dimension types, we first illustrate how simple queries are conducted on nanocubes using an example. Recall that the end result of the query will be to return precomputed aggregates across one or more dimensions.

In Figure 2(5), assume we are interested in the count of all tweets that occurred in the northwest quadrant of the world, regardless of the device type and time. The aggregate key $k_a = ((p_1, p_2), t)$ for this query consists of: (1) the partial assignment for the northwest quadrant in the spatial dimension: $p_1 = [0, 1]$; (2) the empty partial path for the device dimension $p_2 = []$ indicating any device; and (3) a time label t indicating any time. Finding the precomputed aggregate for a given aggregate key is called a *simple query*. In this example, we start at the top-most node and traverse all black parent-child links described in the partial assignment p_1 : in this case only the black $[0, 1]$ link. We next cross the dimension boundary line by traversing the (blue) content link of the current node. The traversal process is repeated for the device dimension using the partial assignment p_2 . In this specific case, no restrictions are made on the device, and we can jump to the next dimension by traversing the content link. At this point, we reach a leaf node containing $\{o_1, o_2\}$. Since no time constraint is imposed, the count of elements inside the leaf (2) is the answer for the query.

Note that, for each dimension, a simple query only traverses a single path of its tree before jumping to the root node of a tree in the next dimension (or to a leaf node which encodes time and is treated differ-

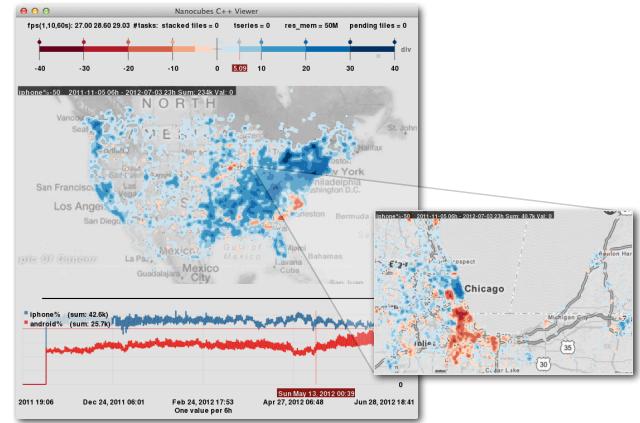


Fig. 7. Which device is more popular for tweeting: iPhone (blue) or Android (orange)? This choropleth map highlights areas in which devices are more popular based on a sample of 210M tweets. When we zoom in to Chicago we can observe something not seen from the overview display: south and west of the city, Android is more popular than iPhone.

ently). In general, higher level queries might traverse multiple paths of a single tree, and may also report single aggregates, multiple aggregates, or even combine aggregates from multiple branches. To abstract and classify how a general nanocube query processes a dimension, we use the terminology of *rollups* and *drilldowns* (the ROLL_UP relational operation is related but has a different meaning than the one we intend here). The dimension that is the basis of a *rollup* should report a single aggregate value as a result. This aggregate might be a single existing aggregate in the nanocube or a combination of multiple aggregates from different branches of that dimension. A *drilldown* reports aggregate values for multiple branches in that dimension. In a single nanocube query, each dimension is independently set to be used as the basis for either a rollup or a drilldown. In Figure 5, we provide a set of example queries and their mapping to the server query URL.

It is worth noting that the order of the d dimensions does not impact the worst-case query run-time. For example, a marginal barchart of a categorical dimension (with k bars), requires $O(kd)$ time, regardless of the category chosen or the ordering of the dimensions.

4.3.1 Spatial Queries

In our current implementation, the first dimension to be traversed in a nanocube is always the spatial dimension. It is helpful to think of this dimension as being represented by a traditional quadtree [27], where each quadtree node is enriched by an extra pointer (content pointer) that jumps to the next dimension of the nanocube. If a query matches exactly the region represented by a quadtree node, then the content pointer of that node is the gateway for all aggregates that refers precisely to that region. If the query includes categorical restrictions (or drilldowns), then these can be found by traversing down the following categorical dimensions, as described below. However, spatial regions will very rarely match exactly one node in the quadtree; therefore, we use the traditional region quadtree intersecting algorithms to compute the minimal disjoint set of quadtree nodes that exactly cover the query region [27], and sum the resulting rollups across the nodes.

Arbitrarily shaped regions are not currently supported for spatial queries because of the additional complexity that is introduced, but there is no major intrinsic barrier in the nanocubes framework which prevents them from working. Instead, we support regions defined by the tiling scheme of most mapping services on the WWW. For example, the widest tile in the world in OpenStreetMap [15] has coordinates $(0, 0, 0)$, while a tile for block-level maps of downtown Los Angeles might have coordinates $(22485, 52342, 17)$. The first two coordinates are integer addresses, and the third coordinate corresponds to the *zoom level*: going down a zoom level doubles the resolution in both x and y . Our spatial drilldowns are then specified by a tile (x, y, z) address and an additional integer resolution, which denotes how many levels

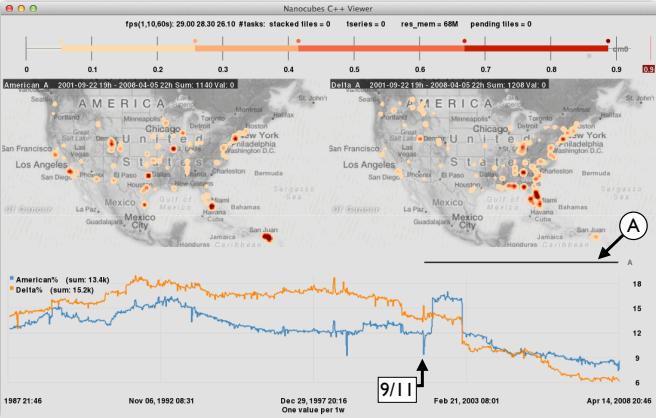


Fig. 8. A history of American Airlines and Delta. The time series show the weekly percentage of the number of commercial flights in the United States. After 9/11 Delta (orange) saw a positive spike where American (blue) saw a negative one. The big bump on American was the merger with TWA. The heatmap shows the spatial hotspots of the two companies counting all flights after 9/11 (the *time bar A* can be dragged and resized to change the considered time window for the heatmap).

to break down space inside the tile. Traditionally, tiles from mapping services are squares with 256 pixels on the side, which corresponds in our case to a resolution of 8. Since our spatial drilldowns return an array of counts broken down by latitude and longitude, they are the basis for spatial density plots and choropleth maps.

4.3.2 Categorical Queries

Categorical dimensions in a nanocube are represented by *flat trees*, which always contain a root node with potentially as many children as there are different values in that category. To restrict the domain to a certain value of the category, the query engine simply follows the path down the child of the corresponding value. Categorical rollups are performed by simply returning the count corresponding to either the top-level node (in case of no restriction) or the child node (in case of a restriction). Categorical drilldowns are also similarly simple: they are a sparse array of all children with non-zero counts.

We note that since categorical dimensions appear under spatial dimensions, answering spatial region rollups with either categorical restrictions or drilldowns requires combining the categorical rollups across all quadtree nodes that are reached by the region. An analogous phenomenon happens for nested drilldowns across multiple categories. For example, the binned scatterplot in Figure 11 can be built directly from the result of drilling down in both day of week and hour of day. The recombinable parallel set visualization of Figure 1 requires a triple breakdown of language, device and application. Single category drilldowns also trivially enable histogram plots.

4.3.3 Temporal Queries

To represent the temporal dimension, we use a sparse variant of summed-area tables [7] (Figure 6). Each time series in a node is stored as a dense, sorted array of *cumulative counts*, tagged by timestamp. With this data structure, we can compute a temporal rollup of event counts along *any* contiguous period, using only two binary searches: one to find the array element with the least upper bound of the period's beginning, and another to find the greatest lower bound of the period's end. The difference between these numbers is the total number of events in the period. A temporal drilldown happens similarly, and we can compute a time series with t entries by performing $t + 1$ binary searches. Each determines the breaking points in the cumulative array, and the final value is computed by stepwise differences.

This scheme for storing time entries is attractive for several reasons. First, it ensures that we can store time series of any granularity without requiring a nested tree structure like our spatial indexing scheme. Second, the running time is essentially optimal (up to a $\log n$ factor), and the algorithm is extremely fast in practice.

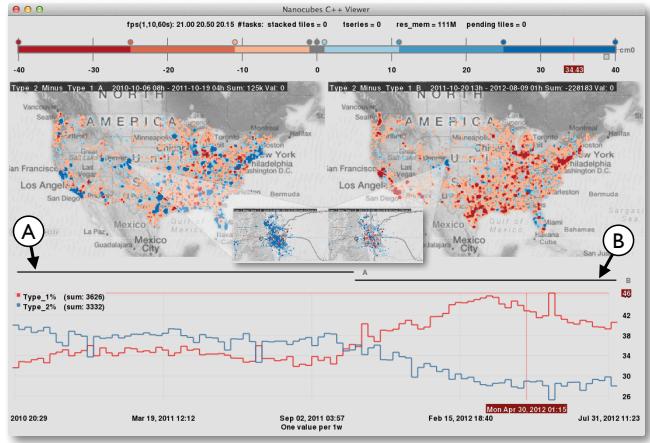


Fig. 9. Two kinds of Customer Tickets: Type 1 (Red) and Type 2 (Blue). The heatmap on the left map corresponds to *time bar A*, and the one on the right to *time bar B*: both encode the difference between number of reports of Type 2 and Type 1 in each point of the map. Reports of Type 1 exceed reports of Type 2, but not everywhere: notice that the region of Denver is still blue. Zooming into Denver we see that the number of Type 1 reports has increased over time, but Type 2 still dominates.

5 IMPLEMENTATION

We use a client-server architecture for the current implementation of nanocubes. The server reads the multidimensional data, builds a nanocube, and then processes queries on the nanocube from client applications. The server is a C++11 template-based implementation which makes it easy to plug in different data structures for each dimension of the nanocube. For example, for the Twitter data, we use a 2d quadtree for the spatial dimensions (latitude and longitude), and flat trees for each categorical dimension (e.g. language, device, application), and our summed-area variant for the time dimension.

The nanocube construction algorithm has not been optimized for speed (results are included in section 6) but there are several possible improvements that we could make: using multiple threads, or using memory pools to avoid the overhead of repeated memory allocations and deallocations. Due to the scale of the input data, most of our effort has been spent on optimizing memory usage, including optimized libraries for memory allocation (libtcmalloc) and tagged pointers, which allow us to use the 16 most significant bits in a 64-bit pointer to quickly identify different types of nodes in our data structure.

The nanocube server exposes its API for queries via HTTP. More specifically, it provides a web service by which queries can be issued [26]. After the data cube is built, the data structures are no longer mutated, and so the server is easily parallelizable (it also means that nanocubes are *add-only*: they cannot be updated if a record is removed from the base relation). Our implementation uses the Mongoose library for handling multiple HTTP requests in separate threads concurrently [21]. We have built two front-end visualization clients to query the nanocube server. One client is written in C++ and uses OpenGL for efficient rendering. The other client is browser-based and is written in Javascript, HTML5, SVG, WebGL, and D3 [3].

6 EXPERIMENTS

To study the behavior of nanocubes, we collected six datasets that ranged in size from four million records up to over one billion records. Each dataset includes geospatial, temporal, and domain-specific categorical dimensions with up to 30 distinct values. For all but the synthetic dataset experiments, we included the geospatial time-series dimensions, and varied the other dimensions based on the datasets.

In the following sections, we provide a brief overview of each of the datasets, followed by an overall summary of our experimental results in section 6.8. For each of the experiments, we paid particular attention to how much memory was required to build and store the nanocube index, as well as the overall complexity of the dataset itself,

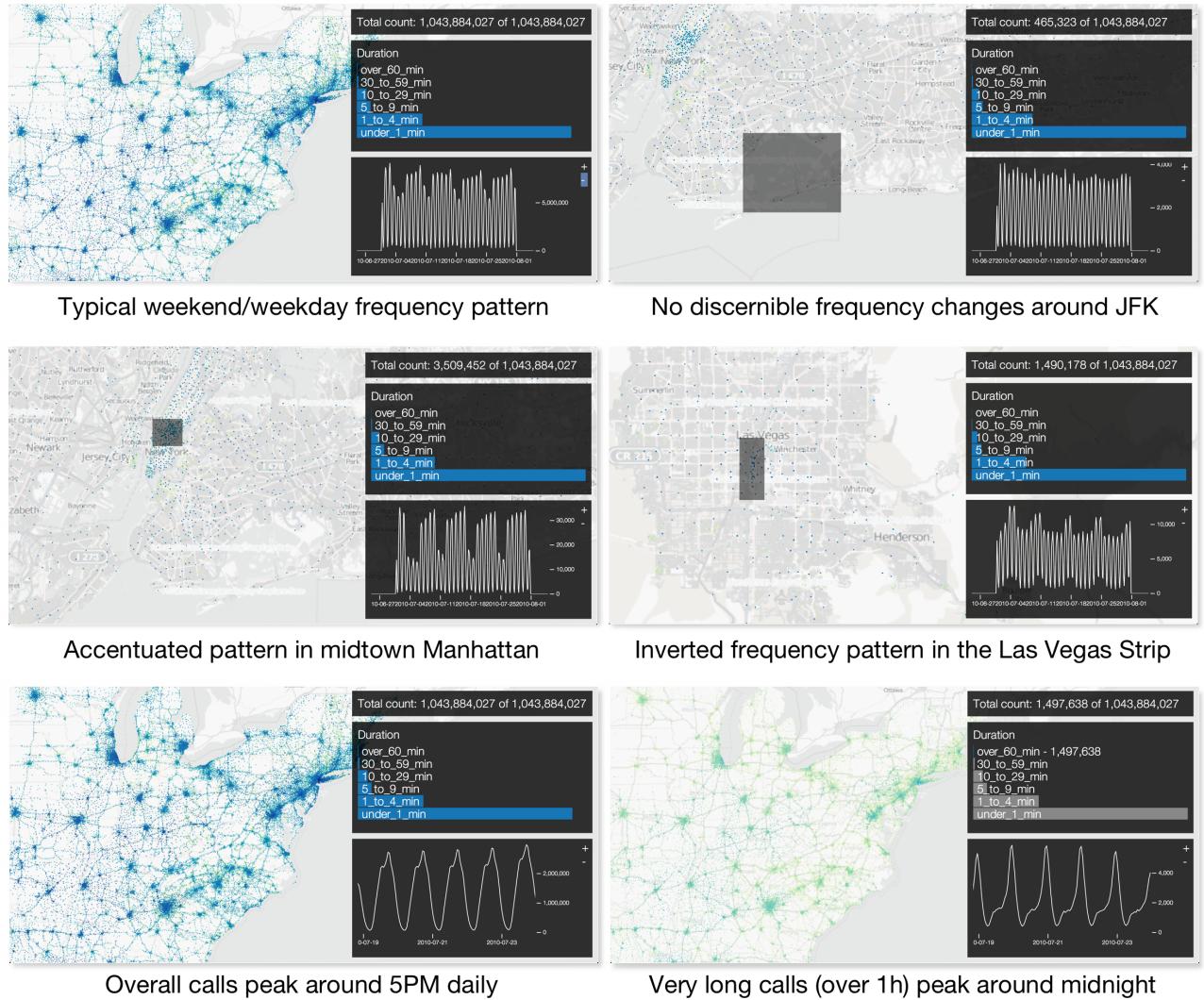


Fig. 10. Highlights of a visual analysis session of the CDR dataset, with 1,043,884,027 records. We noticed the different patterns in call volume by interacting with the dataset and trying different regions and category selections. Notice the patterns occur at different spatial and temporal scales.

which varied greatly from one to the next. Once the nanocubes were constructed, we queried them using one or both of our front-end clients to highlight the ease with which analysts could explore the data.

The query times and bandwidth usage across all experiments are consistent, so we report them in aggregate here. The mean query time was $800\mu s$ (less than 1 millisecond) with a maximum of 12 milliseconds. The output size per query averaged 5KB, with a maximum size of 50KB (geographical tiles dominated bandwidth usage). Our server currently uses no compression, although we plan to support transparent gzip stream encoding. The mean number of queries for the C++ client was 100 requests per second. The HTML5 client is much quieter, at around 1 query per second, since linked views are only updated when a brush is released. The C++ client was designed for LANs, and its bandwidth usage is around 5Mbps, well within current capacities.

6.1 Twitter

Between November 2011 and June 2012, we collected about 210 million tweets that originated in the United States using Twitter's public feed which provides a representative sampling of all tweets. The rate of tweets obtained averaged about one million per day. The data was streamed in the form of JSON objects, from which we extracted the following attributes: latitude and longitude of the device, the time the tweet occurred, the client application used, the type of device, and the language of the tweet. The categorical dimensions in our data (application, device, language) had respectively 4, 5, and 15 distinct values. With a nanocube built using this data, we could quickly explore the

data to better understand the areas in which one device is more popular than another, where each of the languages is most prevalent, and how that information changes over time (see Figure 7).

6.2 Airline Commercial Flights History

This publicly available dataset contains data for every commercial flight in the United States over a 20 year period (1987–2008) [2, 35]. For over 120 million flights, the records include the scheduled departure and arrival times, the actual departure and arrival times, the origin and destination airports, the airline, and other fields. For this experiment, we built our index using the origin airport (for latitude and longitude), scheduled departure time, the departure delay, and the airline. This allows us to answer queries related to overall departure delays for any airports, airlines, time of day, or combinations thereof. In Figure 8 we present an overview on the weekly percentages of total commercial flights in the U.S. for a 20 year period of Delta and American Airlines.

6.3 Call Detail Records

For each cellular phone call, telecommunications companies collect information about the call including time, duration, and the sequence of cell towers that carried the call. This information is organized into what are known as Call Detail Records (CDRs). A large U.S. service provider (privately) shared with us over one billion CDRs generated from a one month period in July 2010. Due to the sensitivity of CDR data, our data has been completely anonymized. No personally identifiable information was gathered or used in conducting this study. To



U.S. West Coast



UK



Japan

Fig. 11. Selecting different geographical regions highlights how different populations interacted with the Brightkite social network. While in the US and UK there is no substantial difference between weekday and weekend traffic, in Japan weekday usage is markedly lower.

the extent that any data was used, it was anonymous and aggregated data. The nanocube was built using the geospatial temporal data (of first cell tower), as well as the duration (transformed to a categorical dimension) of each call (see Figure 10).

6.4 Location-Based Social Networks

The next dataset is also publicly available, and consists of location-based checkins in the Brightkite social network collected by Cho et al. [6]. The dataset comprises all data checkins from the (now-defunct) website between April 2008 and October 2010. In addition to latitude, longitude, and the time of each checkin, we redundantly encoded hour of day and day of week as extra categorical dimensions, since we expected there to be interesting periodic day-to-day and weekday vs. weekend patterns (see Figures 11 and 12).

6.5 Customer tickets

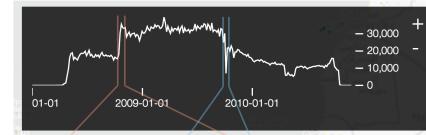
This dataset contains a record of about 8 million records of customer interactions of a large U.S. service provider over a period of 2.5 years. The dataset contains latitude, longitude, time and report type (one of eight categories). The same measures taken to anonymize CDR data in Section 6.3 were used here. In Figure 9, we highlight the use of nanocubes to detect relative changes in category in the time series plot, and how choropleth maps restricted to different time regions show the change in geographical distribution of the report types.

6.6 SPLOM

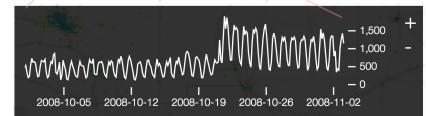
This is a collection of synthetic datasets (each with five dimensions) designed by Kandel et al. [17] to exercise data cube technology (SPLOM stands for ScatterPLOT Matrix, the visual encoding used to explore the dataset in that work), also used by Liu et al. [20]. To compare resource usage to that of these other proposals, we built nanocubes using five different bin sizes per dimension, from 10 to 50.

6.7 Memory Usage

To understand the memory requirements to build a nanocube, it is important to remember that objects are not inserted directly into the nanocube, but rather through their corresponding keys (see Figure 3). An object's key identifies the most specific bin in the nanocube that contains that object. Thus, depending upon the resolutions defined for the dimensions of a nanocube, two different objects may or may not be distinguishable. For example, if the time resolution of a nanocube is one hour, two objects with timestamps at 20h10m and 20h50m will both have have keys with the same time label rounded to 20h. As a result, new occurrences of keys that were already inserted into a nanocube do not require additional storage space.



Overall time series



Upward spike: iOS App Store Release



Downward spike: service outage

Fig. 12. By supporting multiscale time series queries, we can explore the Brightkite checkin frequency to investigate global trends as well as short-lived events. The iOS client for Brightkite was released exactly when the upward spike happened. The downward spike was caused by a global outage that lasted a few days.

Figure 14(A) shows the memory usage growth for the SPLOM dataset as we insert from zero to one billion objects into the five nanocubes of increasing bin size. In all cases there is an initial rapid growth that quickly flattens out. In the case of SPLOM 50, the index grew from 0 to 300MB with the first 200 million object insertions, but grew less than 100MB larger as a result of the next 800 million object insertions. The explanation for this behavior is that, by a characteristic of the synthetic object generator (samples from a normal distribution for each dimension) a key set of high probability was quickly generated making it harder and harder for a new object with an unseen key to be generated. Thus, later in the process, most inserted objects will not require more memory since their keys were already inserted into the nanocube. We refer to this phenomena as *key saturation*.

In Figure 14(B), we present curves for memory usage and number of keys for the CDR dataset, both relative to the final nanocube numbers. To test for a key saturation effect, we excluded the time dimension present in the original data. Once again, we observe an initial rapid growth on memory usage explained by the large number of combinations of cell locations and call durations not yet inserted. Once the bulk of the keys corresponding to these combinations are inserted, a relatively small but steady rate of new keys are inserted reflecting a small but steady growth in the cell tower infrastructure. Similarly defined curves for the Flights dataset are shown in Figure 14(C). The first part of this experiment follows the same trend as before: rapid initial growth, followed by a saturation of keys and a steady but much slower growth reflecting the small rate of new airport locations and carriers. At about 80M inserted flights (circa 1995), we again observe a regime of rapid growth, which corresponds to a burst of new carriers.

6.8 Performance Summary

In Figure 13, we summarize the relevant information for building our nanocubes on the previously described datasets. The number of input objects N , the memory requirements, and the build times are reported in the first three columns, while the exact schema used for each dataset is included in the last column. Column “size” indicates the number of nodes in our data structure (in the nanocube of Figure 2(5) this number would be 41: 22 circles + 19 entries in the leaves). The “sharing” column indicates how much larger the nanocube would be without the sharing mechanism (dashed lines in Figure 2). For example, the twitter dataset nanocube would use at least $4 \times 46.4GB = 185.6GB$ without sharing. Column “keys” is the number of distinct keys induced by the N objects (note here that the time dimension is included). Finally, column $|K^*|$ reports the cardinality of the key space of each nanocube.

dataset	objects (N)	memory	time	size	sharing	keys ($ K $)	$ K^* $	schema
brightkite	4.5 M	1.6 GB	3.50 m	149.0 M	3.00x	3.5 M	2^{74}	lat(25), lon(25), time(16), weekday(3), hour(5)
customer tix	7.8 M	2.5 GB	8.47 m	213.0 M	2.93x	7.8 M	2^{69}	lat(25), lon(25), time(16), type(3)
flights	121.0 M	2.3 GB	31.13 m	274.0 M	16.50x	43.3 M	2^{75}	lat(25), lon(25), time(16), carrier(5), delay(4)
twitter-small	210.0 M	10.2 GB	1.23 h	1.2 B	3.72x	116.0 M	2^{53}	lat(17), lon(17), time(16), device(3)
twitter	210.0 M	46.4 GB	5.87 h	5.2 B	4.00x	136.0 M	2^{60}	lat(17), lon(17), time(16), lang(5), device(3), app(2)
spлом-10	1.0 B	4.3 MB	4.13 h	51.2 K	5.67x	7.4 K	2^{20}	d1(4), d2(4), d3(4), d4(4), d5(4)
spлом-50	1.0 B	166.0 MB	4.72 h	8.8 M	16.00x	1.9 M	2^{30}	d1(6), d2(6), d3(6), d4(6), d5(6)
cdrs	1.0 B	3.6 GB	3.08 h	271.0 M	18.60x	96.3 M	2^{69}	lat(25), lon(25), time(16), duration(3)

Fig. 13. Summary of resource usage for our reported experimental results ($K=10^3$, $M=10^6$, $B=10^9$). The numbers in parentheses on the schema column denote the number of bits necessary to refer to a value of that dimension, and their sum is the exponent of 2 in the $|K^*|$ column.

All but two of the datasets fit in 4GB of RAM, and only one of them would not fit in 16GB, the amount of memory in a high-end laptop. The multiscale nature of spatiotemporal datasets make the cardinality of the key space impractically large for any dense storage scheme.

7 DISCUSSION

As a sparse scheme to store aggregates, nanocubes suffer from the same drawbacks of any sparse data structure. Namely, when the occupancy (i.e. key space covered by the inserted objects) is large, the extra logic and memory needed to handle pointers is wasteful. A dense mechanism, on the other hand, using implicit addressing on arrays has simpler logic, faster access, and uses less memory. When considering multidimensional datasets, the memory requirements of a dense mechanism quickly become impractical (see cardinality of Figure 13). Except for the SPЛОМ experiments, every other dataset would require at least 2^{53} memory locations to represent only the finest bin summaries (e.g. counts), without even considering the memory needed to represent aggregates. This requirement is simply overwhelming. A smart sparse scheme like nanocubes can handle well those datasets with present day technology. Obviously, we cannot expect nanocubes to solve the combinatorial explosion that happens when an arbitrary number of dimensions is considered, but it pushes the size limits of the multidimensional datasets for which we can have a smooth interactive visualization experience.

It is enlightening to compare nanocubes to recent data cube visualization proposals: Datavore [17] and imMens [20] (see Figure 15). For this discussion, we assume input objects inducing keys K and aggregate keys K_a . Datavore’s algorithms behave well in the sparse regime, but cannot handle very large datasets, because its querying time appears to be proportional to $|K|$. imMens, on the other hand, has extremely fast query times (below 1ms per query, and apparently $O(1)$), but is designed for the dense regime, and uses memory proportional to the cardinality of its key space, $O(|K^*|)$. This limits the size of the key space and we observe that although imMens reports experiments varying N from 10^6 to 10^9 , the value of $|K^*|$ in all experiments were within a factor of 5 of one another [20]. The hierarchical nature of a nanocube’s spatiotemporal index provides advantages in the fidelity of resulting visualizations for a much larger set of scales than imMens (Datavore supports exact visual encodings across any dimensions, but cannot cope with large-scale datasets). This same hierarchical nature provides nanocubes with natural *offscreen culling*: the region visible onscreen can be interpreted as a spatiotemporal selection, reducing the total processing necessary.

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	Space	Query Time	Constraints
Datavore [17]	$O(K \log_2 K^*)$	$O(K)$	$ K \leq \text{Main Mem.}$
imMens [20]	$O(K^*)$	$O(1)$	$ K^* \leq \text{GPU Mem.}$
Nanocubes	$O(f(K_a))$	$O(1)$	$ f(K_a) \leq \text{Main Mem.}$

Fig. 15. Comparison of observed asymptotic resource usage of recent methods. Set K corresponds to the input keys and set K_a to the aggregate keys induced by K . Key space, K^* , is a set that grows quickly with resolution and number of dimensions. Function f reflects nanocube’s sharing mechanism and has an important compression effect on the already sparse set K_a (see sharing col. in Figure 13): $|f(K_a)| \leq |K_a|$.

8 LIMITATIONS AND FUTURE WORK

Nanocubes offer efficient storage and querying of large, multidimensional, spatiotemporal datasets, but are not without limits. Nanocubes do not allow queries down to any individual record, like a traditional database. Our index was designed specifically to answer queries from interactive visualization systems that explore massive datasets

Our current server API encourages much chattier communication than is necessary, peaking at hundreds of HTTP requests a second. This happens when brushes are being moved in the C++ client, but could be avoided by techniques like query queueing and prediction [5].

The current nanocube implementation allows for only one spatial dimension and one temporal dimension. It would be clearly useful to allow schemata that included multiple spatial dimensions so that one could visualize, for example, the distribution of geographical locations of flights leaving a certain different geographical area. Similarly, phone calls have two natural geographical dimensions.

Nanocubes still take more memory than we would like. We picked one example to clearly demonstrate this: when indexing all six dimensions, the 210 million points from Twitter take around 45GB of memory. This is enough memory for a present-day server, but above that of typical laptops and workstations. We envision dynamic control over the cardinality of dimensions, but leave that for future work. We would also like to explore hybrid solutions that utilize both on-disk and in-memory data structures to enable more complex nanocubes.

Acknowledgments We would like to thank Stephen North for support throughout this project, Luciano Barbosa for processing the Twitter dataset, and Jeff Heer for bringing imMens to our attention.

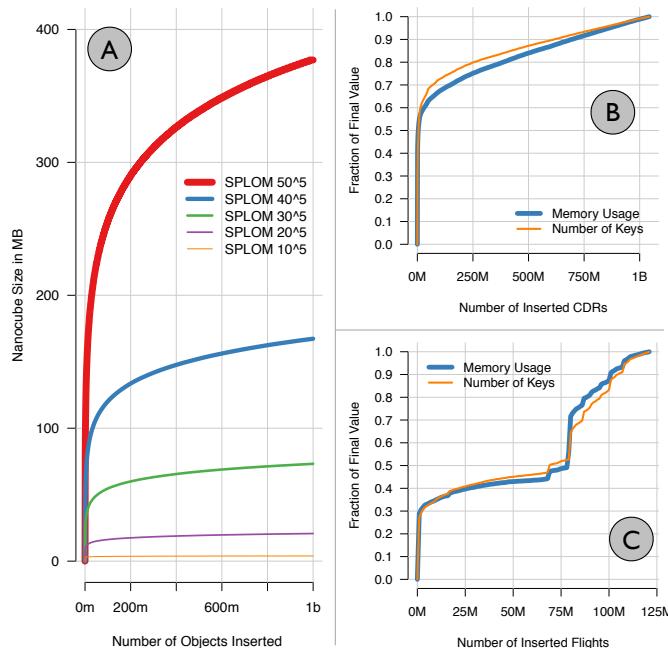


Fig. 14. (A) Nanocube memory usage growth with number of elements, using the SPЛОМ benchmark by Kandel et al [17]. Notice the plateauing in memory usage due to *key saturation*. On the right, the growth of memory usage and number of keys when inserting objects into nanocubes for the Call Detail Records (B) and Flights (C) datasets.

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