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CS 1555

Homework 8

1. Consider the following set of functional dependencies:

FD1: $\text{ItemId} \rightarrow \text{ItemDescription}, \text{ItemPrice}, \text{StockQuantity}$

FD2: $\text{PurchaseId} \rightarrow \text{PurchaseDate}, \text{VendorCode}$

FD3: $\text{VendorCode} \rightarrow \text{VendorName}, \text{VendorAddress}$

FD4: $\text{ItemId}, \text{PurchaseId} \rightarrow \text{OrderQuantity}$

- a. Using universal relational approach (top-down process), construct a set of 3NF/BCNF relations from the above functional dependencies. Indicate the primary keys for the result relations. Please show all steps clearly as mentioned in the lecture slides.

Key = {ItemId, PurchaseId}

R = (ItemId, ItemDescription, ItemPrice, StockQuantity, PurchaseId, PurchaseDate, VendorCode, VendorName, VendorAddress, OrderQuantity)

R Decomposition \rightarrow

R₁ = (VendorCode, VendorName, VendorAddress) \rightarrow FD3

R₂ = (ItemId, ItemDescription, ItemPrice, StockQuantity, PurchaseId, PurchaseDate, VendorCode, OrderQuantity)

R₂ \rightarrow Decomposition

R₃ = (ItemId, ItemDescription, ItemPrice, StockQuantity) \rightarrow FD1

R₄ = (ItemId, PurchaseId, PurchaseDate, VendorCode, OrderQuantity)

R₄ Decomposition \rightarrow

R₅ = (PurchaseId, PurchaseDate, VendorCode) \rightarrow FD2

R₆ = (ItemId, PurchaseId, OrderQuantity) \rightarrow FD4

Final Decomposition:**R₁ = (VendorCode, VendorName, VendorAddress)****R₃ = (ItemId, ItemDescription, ItemPrice, StockQuantity)****R₅ = (PurchaseId, PurchaseDate, VendorCode)****R₆ = (ItemId, PurchaseId, OrderQuantity)**

- b. Using the table method, check whether the constructed set of relations is lossless or not. Also, state if your decomposition is good, bad or ugly. You must show all steps. Hint: Bad decomposition is a lossy one, while ugly decomposition is lossless but does not preserve some dependencies.

	ItemId	ItemDescription	ItemPrice	StockQuantity	PurchaseId	PurchaseDate	VendorCode	VendorName	VendorAddress	OrderQuantity
R ₁	U	U	U	U	U	U	<u>K</u>	K	K	U
R ₃	<u>K</u>	K	K	K	U	U	U	U	U	U
R ₅	U	U	U	U	<u>K</u>	K	<u>K</u>	U → K	U → K	U
R ₆	<u>K</u>	U → K	U → K	U → K	<u>K</u>	U → K	U → K	U	U	K

	ItemId	ItemDescription	ItemPrice	StockQuantity	PurchaseId	PurchaseDate	VendorCode	VendorName	VendorAddress	OrderQuantity
R ₁	U	U	U	U	U	U	K	K	K	U
R ₃	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	U	U	U	U	U	U
R ₅	U	U	U	U	<u>K</u>	<u>K</u>	<u>K</u>	K	K	U
R ₆	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	U → K	U → K	K

	ItemId	ItemDescription	ItemPrice	StockQuantity	PurchaseId	PurchaseDate	VendorCode	VendorName	VendorAddress	OrderQuantity
R ₁	U	U	U	U	U	U	K	K	K	U
R ₃	K	K	K	K	U	U	U	U	U	U
R ₅	U	U	U	U	K	K	K	K	K	U
R ₆	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>	<u>K</u>

Good Decomposition

2. Consider the following set of functional dependencies:

$A \rightarrow B$,
 $B \rightarrow CD$,
 $A \rightarrow D$,
 $B \rightarrow C$,
 $AB \rightarrow CD$,
 $A \rightarrow C$,
 $E \rightarrow F$

- a. Using synthesis approach (bottom-up process), construct a set of 3NF/BCNF relations from the above functional dependencies. Indicate the primary keys for the result relations and whether or not they are in 3NF or BCNF. Please show all steps clearly as mentioned in the lecture slides.

$A \rightarrow D$, - inferred from ($A \rightarrow B$, $B \rightarrow CD$) then $A \rightarrow CD$ then $A \rightarrow C$ and $A \rightarrow D$ [Transitive and Decomposition]

$A \rightarrow C$, - inferred from ($A \rightarrow B$, $B \rightarrow CD$) then $A \rightarrow CD$ then $A \rightarrow C$ and $A \rightarrow D$ [Transitive and Decomposition]

$B \rightarrow C$, - inferred from $B \rightarrow CD$ then $B \rightarrow C$ and $B \rightarrow D$ [Decomposition]

$AB \rightarrow CD$, - inferred from ($A \rightarrow B$, $B \rightarrow CD$) [Composition]

Canonical Cover:

$A \rightarrow B$,
 $B \rightarrow CD$,
 $E \rightarrow F$

Key: {A, E}

R_1 : (A, B)

R_2 : (B, C, D)

R_3 : (E, F)

R_4 : (A, E) \rightarrow added because no other relation contains the key

- b. Using the table method, check whether the constructed set of relations is lossless or not. If not, correct them.

	A	B	C	D	E	F
R ₁	<u>K</u>	<u>K</u>	U → K	U → K	U → K	U
R ₂	U	<u>K</u>	K	K	U	U
R ₃	U	U	U	U	<u>K</u>	K
R ₄	<u>K</u>	U	U	U	<u>K</u>	U → K

	A	B	C	D	E	F
R ₁	K	K	K	K	<u>K</u>	U → K
R ₂	U	K	K	K	U	U
R ₃	U	U	U	U	<u>K</u>	K
R ₄	K	U	U	U	<u>K</u>	K

	A	B	C	D	E	F
R ₁	K	K	K	K	K	K
R ₂	U	K	K	K	U	U
R ₃	U	U	U	U	K	K
R ₄	K	U	U	U	K	K

Lossless