

#### Map (SOM) tutorial

## Example

For vector 1100 (We are using the Euclidean distance squared for convenience)

$$D(1) = (1-0.2)^2 + (1-0.6)^2 + (0-0.5)^2 + (0-0.9)^2 = 1.86$$

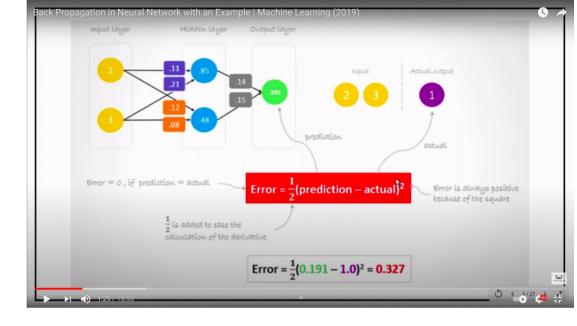
$$D(1) = 1.86, D(2) = 0.98$$

Hence J = 2. Note that R = 0, so we need not update the weights of any neighboring neurons.

Using 
$$w_{ij}(new) = w_{ij}(old) + a(x_i - w_{ij}(old))$$
, the new weight matrix is

$$\begin{bmatrix} w_{11} & w_{12} \\ w_{21} & w_{22} \\ w_{31} & w_{32} \\ w_{41} & w_{42} \end{bmatrix} = \begin{bmatrix} 0.2 & 0.92 \\ 0.6 & 0.76 \\ 0.5 & 0.28 \\ 0.9 & 0.12 \end{bmatrix} \xrightarrow{w_{12}(new) = w_{12}(old) + \alpha(x_1 + w_{12}(old))} = 0.8 + 0.6(1 - 0.8) = 0.92$$

1:00 / 1:45



# Kohonen learning algorithm

## Step 1: Initialization

- Initial synaptic weights are set to small random values  $\in$  [0,1] and the learning rate  $\alpha$  is a small positive value.
- Step 2: Activation and similarity matching
  - Apply the input vector  $\mathbf{X}$  and find the winner-takes-all neuron  $j_{\mathbf{X}}$  at iteration  $\mathbf{p}$ , using the minimum-distance Euclidean criterion

$$j_{X}(p) = \min_{j} ||X - W_{j}(p)|| = \left\{ \sum_{i=1}^{n} [x_{i} - w_{ij}]^{2} \right\}^{1/2}, \quad j = 1, 2, ..., m$$

where n is the number of neurons in the input layer, and m is the number of neurons in the output or Kohonen layer.

## · Step 3: Learning

- Update the synaptic weights:  $w_{ij}(p+1) = w_{ij}(p) + \Delta w_{ij}(p)$  where  $\Delta w_{ij}(p)$  is the weight correction at iteration p
- The competitive learning rule (Haykin, 1999) for weight correction

$$\Delta w_{ij}(p) = \begin{cases} \alpha \big[ x_i(p) - w_{ij}(p) \big] & j \in \Lambda_j(p) \\ 0 & j \notin \Lambda_j(p) \end{cases}$$

where  $\alpha$  is the learning rate  $(0 < \alpha < 1)$ , and  $\Lambda_j(p)$  is the neighborhood function centered around the winner-takes-all neuron  $j_X$  at iteration p

#### • Step 4: Iteration

 Increase iteration p by one, go back to Step 2 and continue until the stopping criterion is satisfied.