

Solving Exponential Equations II (7.3) p364 day 5

take up quiz 10

Quiz 10C

1. Solve on  $[0, 2\pi)$   
 $\sin 2x + \cos x = 0$   
 $\sin 2x = -\cos x$   
 $2\sin x \cos x = -\cos x$   
 $2\sin x \cos x + \cos x = 0$   
 $\cos x (2\sin x + 1) = 0$   
 $\cos x = 0$  or  $2\sin x + 1 = 0$   
 $\cos x = 0 \Rightarrow x = \frac{\pi}{2}, \frac{3\pi}{2}$   
 $2\sin x + 1 = 0 \Rightarrow \sin x = -\frac{1}{2}$   
 $\sin x = -\frac{1}{2} \Rightarrow x = \frac{7\pi}{6}, \frac{11\pi}{6}$

2. Solve on  $x \in \mathbb{R}$   
 $2\cos^2 x + 3\sin x = 3$   
 $2(1 - \sin^2 x) + 3\sin x = 3$   
 $2 - 2\sin^2 x + 3\sin x = 3$   
 $-2\sin^2 x + 3\sin x - 1 = 0$   
 $2\sin^2 x - 3\sin x + 1 = 0$   
 $(2\sin x - 1)(\sin x - 1) = 0$   
 $2\sin x - 1 = 0$  or  $\sin x - 1 = 0$   
 $2\sin x = 1 \Rightarrow \sin x = \frac{1}{2} \Rightarrow x = \frac{\pi}{6}, \frac{5\pi}{6}$   
 $\sin x = 1 \Rightarrow x = \frac{\pi}{2}$

3. Ac-225 has a half-life of 10 days. How much of a 100g sample remains after 30 days?  
 $A(t) = 100 \left(\frac{1}{2}\right)^{\frac{t}{10}}$   
 $A(30) = 100 \left(\frac{1}{2}\right)^3$   
 $A(30) = 100 \left(\frac{1}{8}\right)$   
 $A(30) = 12.5 \text{ g}$

4. Graph:  $y = 3(2)^{x-1} - 2$

5. If  $\tan \theta = \frac{5}{12}$ , find the value of  $A$  on  $[0, 2\pi)$   
 $A = \frac{1}{2} \cos^{-1} \left( \frac{5}{13} \right)$   
 $A = \frac{1}{2} \cos^{-1} \left( \frac{5}{13} \right)$   
 $A = 0.39 \text{ rad}$   
 $A = 0.39 \text{ rad}$

6. Evaluate:  
 $\cos \frac{\pi}{6} \cos \frac{\pi}{3} - \sin \frac{\pi}{6} \sin \frac{\pi}{3}$   
 $= \cos \left( \frac{\pi}{6} + \frac{\pi}{3} \right)$   
 $= \cos \left( \frac{\pi}{2} \right)$   
 $= 0$

Applications II (7.3) p364 day 5

8. If seafood is not kept frozen (below  $0^\circ\text{C}$ ), it will spoil due to bacterial growth. The relative rate of spoilage increases with temperature according to the model  $R = 100(2.7)^{\frac{T}{8}}$ , where  $T$  is the temperature, in degrees Celsius, and  $R$  is the relative spoilage rate.

a) Sketch a graph of the relative spoilage rate  $R$  versus the temperature  $T$  from  $0^\circ\text{C}$  to  $25^\circ\text{C}$ .

b) Use your graph to predict the temperature at which the relative spoilage rate doubles to 200.

c) What is the relative spoilage rate at  $15^\circ\text{C}$ ?

d) If the maximum acceptable relative spoilage rate is 500, what is the maximum storage temperature?

10. Simionie needs \$70,000 to buy a snowmobile, but on offers a GIC that pays interest at a rate of 3.93% compounded annually. How long would Simionie need to wait to have the money to buy the snowmobile?

$4\text{cd}, 5\text{cd}, 8, 10$   
 $200 = 100(2.7)^{\frac{T}{8}}$

Christmas music quiz

Project 5

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ex1: A culture of E-coli has 2000 bacteria. Two and a half hours later there are 2 048 000 bacteria. What is the doubling period?

$P(t) = P_0(2)^{\frac{t}{d}}$  ← doubling period

$2048000 = 2000 \cdot 2^{\frac{2.5}{d}}$

$1024 = 2^{\frac{2.5}{d}}$

$2^{10} = 2^{\frac{2.5}{d}}$

$\therefore 10 = \frac{2.5}{d}$

$d = 0.25$

$\therefore 15 \text{ minutes}$

always 2 for bacteria

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ex2: You borrow \$10,000 to get through first year. If the interest is 7% compounded semi-annually, how much will you owe in 4 years time?

$A = 10000(1.07)^4$

$A = 10000(1.035)^8$

$A = 13168$

Amount  
Principal  
interest rate  
compounds / year  
number of years

$A = P \left( 1 + \frac{i}{c} \right)^{nc}$

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ex3: How much will you have if you invest \$3000 for 9 years at 5% compounded quarterly?

$A = P \left( 1 + \frac{i}{c} \right)^{nc}$

$A = 3000 \left( 1 + \frac{0.05}{4} \right)^{9 \cdot 4}$

$A = 4692$

try: \$6200 at 3% for 10 years compounded monthly

$A = 6200 \left( 1 + \frac{0.03}{12} \right)^{12 \cdot 10}$

$A = 8366$

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ex4: You bought a new car that cost \$24,000. It depreciates at 16% per year. What will the car be worth in 5 years?

$A = 24000(1 - 0.16)^5$

$A = 24000(0.84)^5$

$A = 10,037$

Compare after 10 years

$\$4197$

Solving Exponential Equations II (7.3)

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hw: p364 #9, 11, 13