

Section 4.2

Part #2

Review: Find the derivative of $xy^2 + y = 16$

$$\frac{d}{dx} xy^2 + \frac{d}{dx} y = \frac{d}{dx} 16$$

$$x \frac{d}{dx} y^2 + y^2 \frac{d}{dx} x + y' = 0$$

$$x 2y \cdot y' + y^2 (1) + y' = 0$$

$$2xyy' + y' = -y^2$$

$$y'(2xy + 1) = -y^2$$

$$y' = \frac{-y^2}{2xy + 1}$$

Find the derivative of $3x^2 = \cos(y)$

$$\frac{d}{dx} 3x^2 = \frac{d}{dx} \cos y$$

$$6x = -\sin y \cdot y'$$

$$\frac{-\sin y}{-\sin y}$$

$$y' = -\frac{6x}{\sin y}$$

Find the derivative of $x^2y^2 + x\sin(y) = 4$

$$\frac{d}{dx} x^2y^2 + \frac{d}{dx} x\sin y = \frac{d}{dx} 4$$

$$x^2(2yy') + y^2(2x) + x(\cos y \cdot y') + \sin y(1) = 0$$

$$2x^2yy' + 2xy^2 + x\cos y \cdot y' + \sin y = 0$$

$$2x^2yy' + x\cos y \cdot y' = -2xy^2 - \sin y$$

$$y'(2x^2y + x\cos y) = -2xy^2 - \sin y$$

$$y' = \frac{-2xy^2 - \sin y}{2x^2y + x\cos y} \quad \text{OR} \quad = -\frac{2xy^2 + \sin y}{2x^2y + x\cos y}$$

Find the equations of the tangent and normal lines for the equation below at the point $(\frac{\pi}{4}, \frac{\pi}{2})$

$$x \sin 2y = y \cos 2x$$

$$x \frac{d}{dx} \sin 2y + \sin 2y \frac{d}{dx} x = y \frac{d}{dx} \cos 2x + \cos 2x \frac{d}{dx} y$$

$$x \cos 2y (2y') + \sin 2y (1) = y (-2 \sin 2x) + \cos 2x y'$$

$$y' = \frac{-\sin 2y - 2y \sin 2x}{2x \cos 2y - \cos 2x}$$

$$\begin{aligned} m &= \frac{-\sin 2(\frac{\pi}{2}) - 2(\frac{\pi}{2}) \sin 2(\frac{\pi}{4})}{2(\frac{\pi}{4}) \cos 2(\frac{\pi}{2}) - \cos 2\frac{\pi}{4}} \\ &= \frac{-\sin \pi - \pi \sin \pi/2}{\frac{\pi}{2} (\cos \pi - \cos \pi/2)} \\ &= \frac{-0 - \pi(1)}{\frac{\pi}{2} (-1) - 0} = \frac{-\pi}{-\frac{\pi}{2}} = 2 \end{aligned}$$

Homework

p. 167 #5-8, 23, 25, 26

Typo the point should
be $(1, \frac{\pi}{2})$

Answers:

6. $\sec y$

8. $y' = \frac{1-y}{x - \cos y}$

26. a. $y = \pi$

b. $x = 0$