

Transforming Exponential Functions (7.2) p354 day 2

Thomas Malthus

We're all going to die

Growth of resources

Growth of population

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12. Statistics indicate that the world population since 1995 has been growing at a rate of about 1.27% per year. United Nations records estimate that the world population in 2011 was approximately 7 billion. Assuming the same exponential growth rate, when will the population of the world be 9 billion?

1.27%

2011 7

2012 $7(1.0127)$

$7(1.0127)^n = 9$

$1.0127^n = 1.2$

10. The CANDU (CANA Uranium) reactor is pressurized heavy-water (D₂O) moderator. The CANDU reactor is approximately 70% efficient. What exponential decay of 1 kg of variables you use?

a) Graph the function. Explain why the function is exponential.

b) How many people have the virus at each time?

c) How long will it take to decay to 0.125 kg?

d) Will the sample decay to 0 kg? Explain.

7. A flu virus is spreading through the student population of a school according to the function $N = 2^t$, where N is the number of people infected and t is the time, in days.

a) Graph the function. Explain why the function is exponential.

b) How many people have the virus at each time?

c) How long will it take to decay to 0.125 kg?

d) Will the sample decay to 0 kg? Explain.

8. Scale's down below that the deeper they dive, the more light is absorbed by the water above them. On a dive, Peta's light meter shows that the amount of light available decreases by 10% for every 10 m that she descends.

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don't write this down!

A cup of water is heated to 100 °C and then allowed to cool in a room with an air temperature of 20 °C. It is found that the temperature of the water decreases exponentially at a rate of 25% every 5 min.

Develop a function that models this situation.

answer later

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How does changing the value of k change the graph?

ex1: Sketch $y = 4^x$

$y = 4^x + 2$

$y = 4^x - 3$

$y = a(c)^{b(x-h)} + k$

horiz asym

moves y-intercept and horiz asymptote

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How does changing the value of h change the graph?

ex2: Sketch $y = 6^x$

$y = 6^{x+2}$

2 left

$y = 6^{x-3}$

3 right

moves the y-intercept

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How does changing the value of a change the graph?

ex3: Sketch $y = 3^x$

$y = 4(3)^x$

$y = -2(3)^x$

$y = a(c)^{b(x-h)} + k$

a is distance between asymptote and y-intercept

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How does changing the value of b change the graph?

ex4: Sketch $y = 2^x$

$(2^3)^x$
horiz comp

$y = 2^{3x}$

$y = 2^{-0.5x}$

$y = a(c)^{b(x-h)} + k$

b is usually a fraction that slows down the function

$-b$ means decay

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ex5: Sketch and describe $y = 2(3)^{x-4}$

vert str 2
horiz trans 4 right

3ab, 4

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ex6: A cup of water is heated to 100 °C and then allowed to cool in a room with an air temperature of 20 °C. It is found that the temperature of the water decreases exponentially at a rate of 25% every 5 min.

a) Develop a function that models this situation.

$T(t) = 80(0.75)^{\frac{t}{5}} + 20$

b) Find the temp after 20 minutes.

$T(20) = 80(0.75)^{\frac{20}{5}} + 20$
 $= 45.3^\circ\text{C}$

c) What do each of the numbers in this function mean?

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hw: p354 #3cde, 7ab