

Inverse of a Relation (1.4)

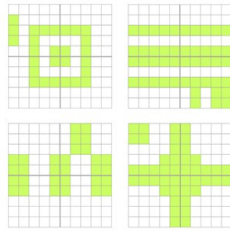
p51

day 7

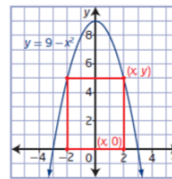
bias toward adding

when is it better to subtract?

training wheels
artwork



16. A rectangle is inscribed between the x-axis and the parabola $y = 9 - x^2$ with one side along the x-axis, as shown.



a) Write the equation for the area of the rectangle as a function of x .

$$A = bh$$

$$= (2x)(y)$$

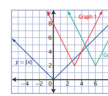
$$A(x) = (2x)(9 - x^2)$$

p51
14, 16a*

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14. Two parabolic arches of first arch can be modeled $y = -x^2 + 9$, with a radius of 3 units. The second arch must be translated left and 3 units down. a) Sketch the graph of b) Determine the equation of the arch.

According to the equation $y = -x^2 + 9$, the vertex is at (0, 9). The arch is 3 units wide at the base. To sketch the graph, we decide to apply the horizontal stretch of 3 units to the vertex to a base of 3. Then, we decide to apply the horizontal stretch of 3 units to the right and the vertical translation of 3 units up. This results in Graph 2. We explain why the two graphs are so different.



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Which of the following are invertible?

closing a door

putting on your shoes

ripping paper

turning on a light

saying something mean

burning down the school

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Many things in life are invertible - you can undo them by doing the opposite action.

In math, we have seen many inverse operations

eg. multiply by 3, divide by 3

adding 10, subtracting 10

Functions can also be inverted.

An inverse function can be used to undo the original.

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ex1: Find the inverse of the following:

a) $y = x^2$

b) $y = 4x$

c) $y = x + 5$

$$y = \sqrt{x}$$

$$y = \frac{1}{4}x$$

$$y = x - 5$$

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ex2: Find the inverse:

$$y = x^2 - 4$$

$$y = 2x + 3$$

$$y = -5x + 2$$

$$x = y^2 - 4$$

$$x = 2y + 3$$

$$x = -5y + 2$$

$$x + 4 = y^2$$

$$x - 3 = 2y$$

$$x - 2 = -5y$$

$$\sqrt{x + 4} = y$$

$$\frac{x - 3}{2} = y$$

$$\frac{x - 2}{-5} = y$$

$$-\frac{1}{5}x + \frac{2}{5} = y$$

switch x and y and solve for y

5abcf

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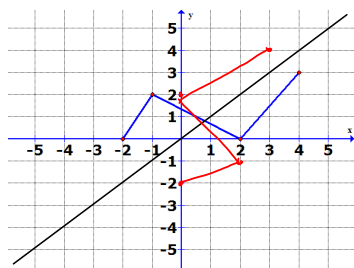
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ex3: For the graph of $y=f(x)$, draw the inverse $x=f(y)$.

$y=f(x)$		inverse	
x	y	x	y
-2	0	0	-2
-1	2	2	-1
2	0	0	2
4	3	3	4

switch!



notice the graph is a reflection, but not in the x or y axis...

2ab

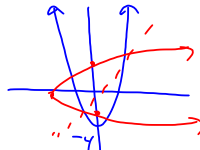
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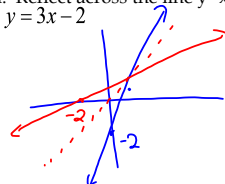
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ex4: Sketch the inverse of each function. Reflect across the line $y=x$.

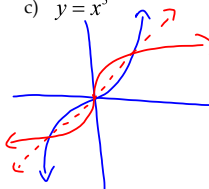
a) $y = x^2 - 4$



b) $y = 3x - 2$



c) $y = x^3$



8ab

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#w: p51#6, 10a, 13ab