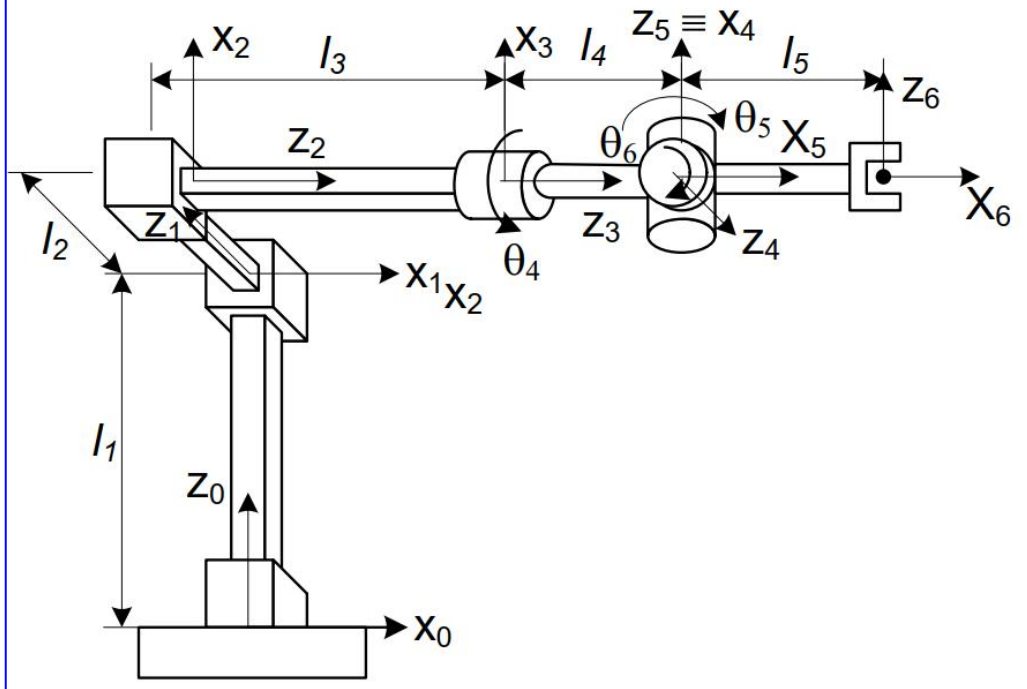


Bài 1



$$\begin{aligned}
 {}^0P &= {}^0T_7 \cdot {}^7P \\
 &= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5T_6 \cdot {}^6P \\
 &= T(l_3, l_2, l_1) * R(x, \theta_4) * T(l_4, 0, 0) * R(z, \theta_5) * R(y, \theta_6) * T(l_5, 0, 0) * P \\
 &= \begin{bmatrix} 1 & 0 & 0 & l_3 \\ 0 & 1 & 0 & l_2 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_4 & -\sin\theta_4 & 0 \\ 0 & \sin\theta_4 & \cos\theta_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \\
 &\quad \begin{bmatrix} \cos\theta_5 & -\sin\theta_5 & 0 & 0 \\ \sin\theta_5 & \cos\theta_5 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_6 & 0 & \sin\theta_6 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_6 & 0 & \cos\theta_6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \\
 &= \begin{bmatrix} l_3 + l_4 + l_5 * \cos(t_5) * \cos(t_6) \\ l_2 + l_5 * (\sin(t_4) * \sin(t_6) + \cos(t_4) * \cos(t_6) * \sin(t_5)) \\ l_1 - l_5 * (\cos(t_4) * \sin(t_6) - \cos(t_6) * \sin(t_4) * \sin(t_5)) \\ 1 \end{bmatrix}
 \end{aligned}$$

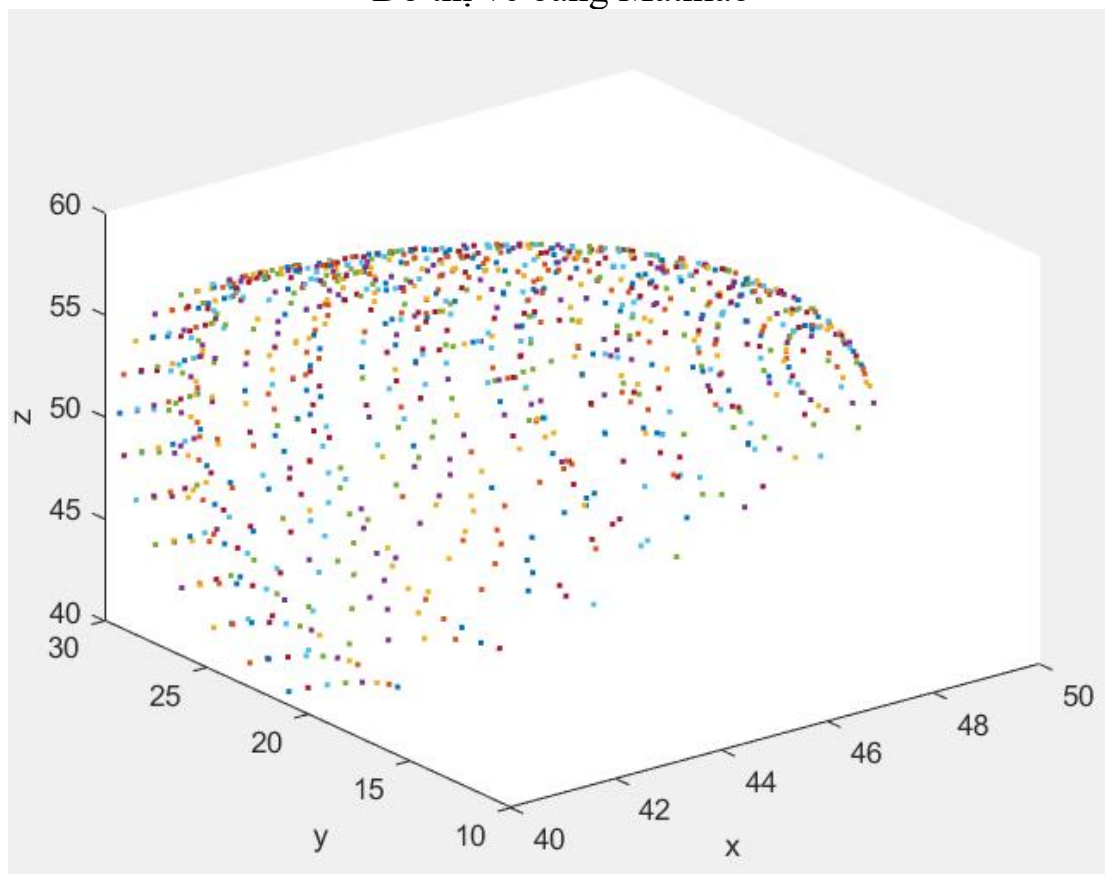
Vậy

$$x = l_3 + l_4 + l_5 * \cos(t_5) * \cos(t_6)$$

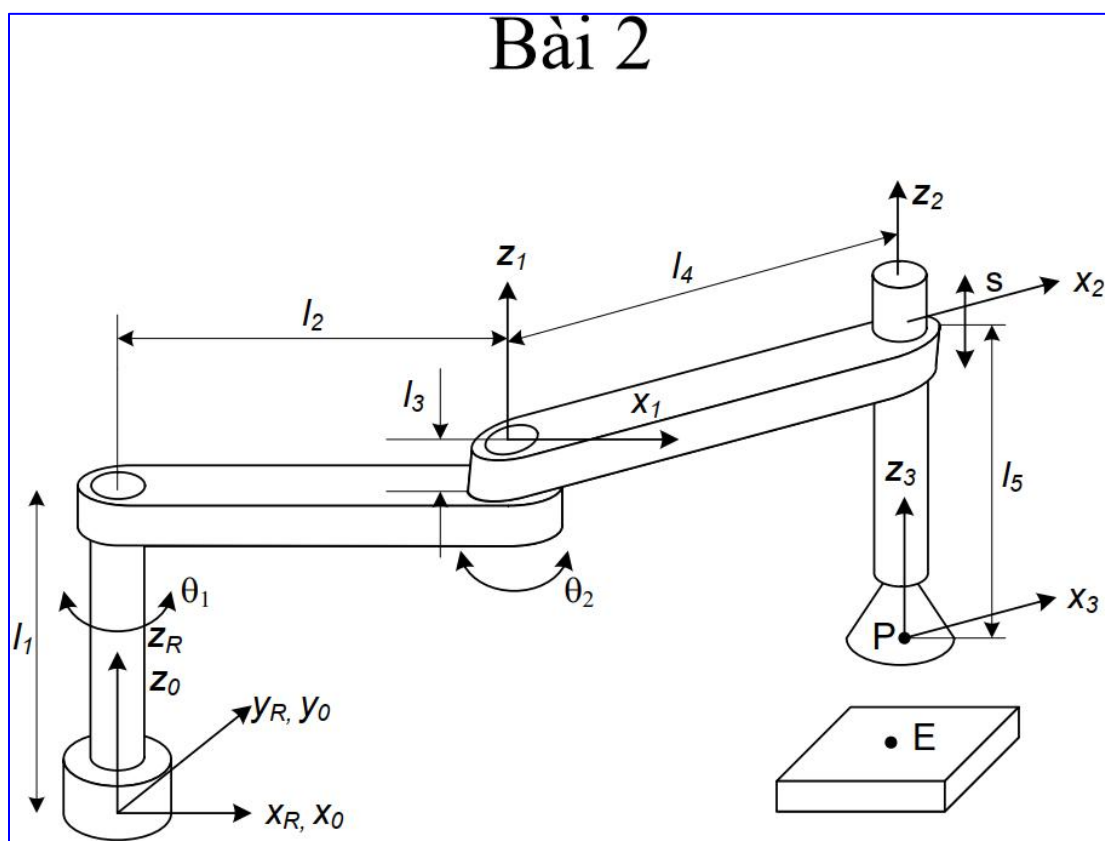
$$y = l_2 + l_5 * (\sin(t_4) * \sin(t_6) + \cos(t_4) * \cos(t_6) * \sin(t_5))$$

$$z = l_1 - l_5 * (\cos(t_4) * \sin(t_6) - \cos(t_6) * \sin(t_4) * \sin(t_5))$$

Đồ thị vẽ bằng Matlab



Bài 2



$$\begin{aligned}
{}^0P &= {}^0T_4 \cdot {}^4P \\
&= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4P \\
&= R(z, \theta_1) * T(l_2, 0, l_1) * R(z, \theta_2) * T(l_4, 0, l_3 - l_5 + s) * P
\end{aligned}$$

$$= \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_2 & -\sin\theta_2 & 0 & 0 \\ \sin\theta_2 & \cos\theta_2 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & l_4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_3 - l_5 + s \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} l_4 * \cos(t_1 + t_2) + l_2 * \cos(t_1) \\ l_4 * \sin(t_1 + t_2) + l_2 * \sin(t_1) \\ l_1 + l_3 - l_5 + s \\ 1 \end{bmatrix}$$

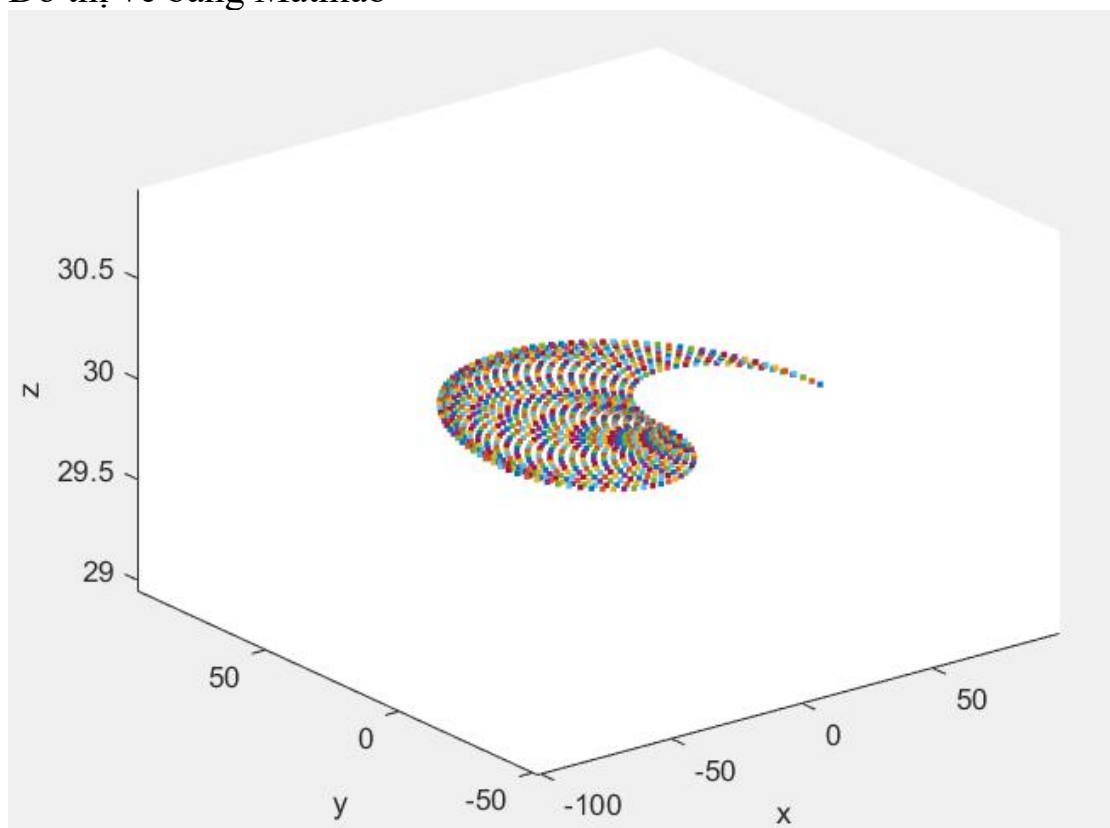
Vậy

$$x = l_4 * \cos(t_1 + t_2) + l_2 * \cos(t_1)$$

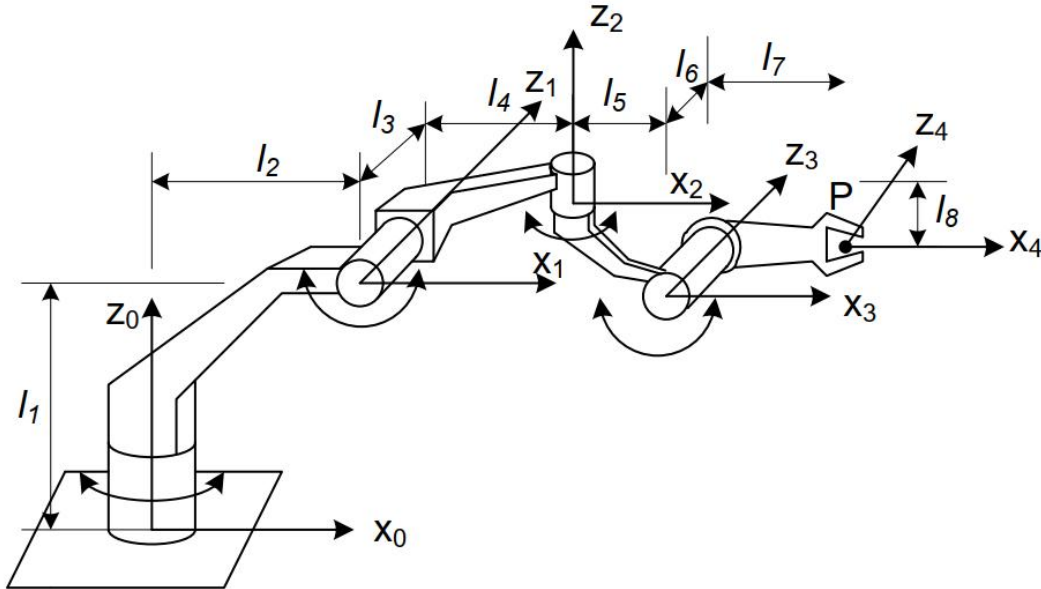
$$y = l_4 * \sin(t_1 + t_2) + l_2 * \sin(t_1)$$

$$z = l_1 + l_3 - l_5 + s$$

Đồ thị vẽ bằng Matlab



Bài 3



$$\begin{aligned}
 {}^0P &= {}^0T_8 \cdot {}^8P \\
 &= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5T_6 \cdot {}^6T_7 \cdot {}^7T_8 \cdot {}^8P \\
 &= R(z, \theta_1) * T(l_2, 0, l_1) * R(y, \theta_2) * T(l_4, l_3, 0) * R(z, \theta_3) * T(l_5, 0, -l_8) \\
 &\quad * R(y, \theta_4) * T(l_7, l_6, 0) * P
 \end{aligned}$$

$$= \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_2 & 0 & \sin\theta_2 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_2 & 0 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{aligned}
 &\begin{bmatrix} 1 & 0 & 0 & l_4 \\ 0 & 1 & 0 & l_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_3 & -\sin\theta_3 & 0 & 0 \\ \sin\theta_3 & \cos\theta_3 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -l_8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\
 &\times \begin{bmatrix} \cos\theta_4 & 0 & \sin\theta_4 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_4 & 0 & \cos\theta_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_7 \\ 0 & 1 & 0 & l_6 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}
 \end{aligned}$$

$$\begin{aligned}
 &= [l_2 \cdot \cos(t_1) - l_6 \cdot (\cos(t_3) \cdot \sin(t_1) + \cos(t_1) \cdot \cos(t_2) \cdot \sin(t_3)) - \\
 &l_5 \cdot (\sin(t_1) \cdot \sin(t_3) - \cos(t_1) \cdot \cos(t_2) \cdot \cos(t_3)) - l_3 \cdot \sin(t_1) - \\
 &l_7 \cdot (\cos(t_4) \cdot (\sin(t_1) \cdot \sin(t_3) - \cos(t_1) \cdot \cos(t_2) \cdot \cos(t_3)) + \\
 &\cos(t_1) \cdot \sin(t_2) \cdot \sin(t_4)) + l_4 \cdot \cos(t_1) \cdot \cos(t_2) - l_8 \cdot \cos(t_1) \cdot \sin(t_2)
 \end{aligned}$$

```
; l5*(cos(t1)*sin(t3) + cos(t2)*cos(t3)*sin(t1)) + l6*(cos(t1)*cos(t3) -
cos(t2)*sin(t1)*sin(t3)) + l3*cos(t1) + l2*sin(t1) +
l7*(cos(t4)*(cos(t1)*sin(t3) + cos(t2)*cos(t3)*sin(t1)) -
sin(t1)*sin(t2)*sin(t4)) + l4*cos(t2)*sin(t1) - l8*sin(t1)*sin(t2)
;
l1 - l7*(cos(t2)*sin(t4) + cos(t3)*cos(t4)*sin(t2)) - l8*cos(t2) - l4*sin(t2) -
l5*cos(t3)*sin(t2) + l6*sin(t2)*sin(t3)
;1]
```

Vậy

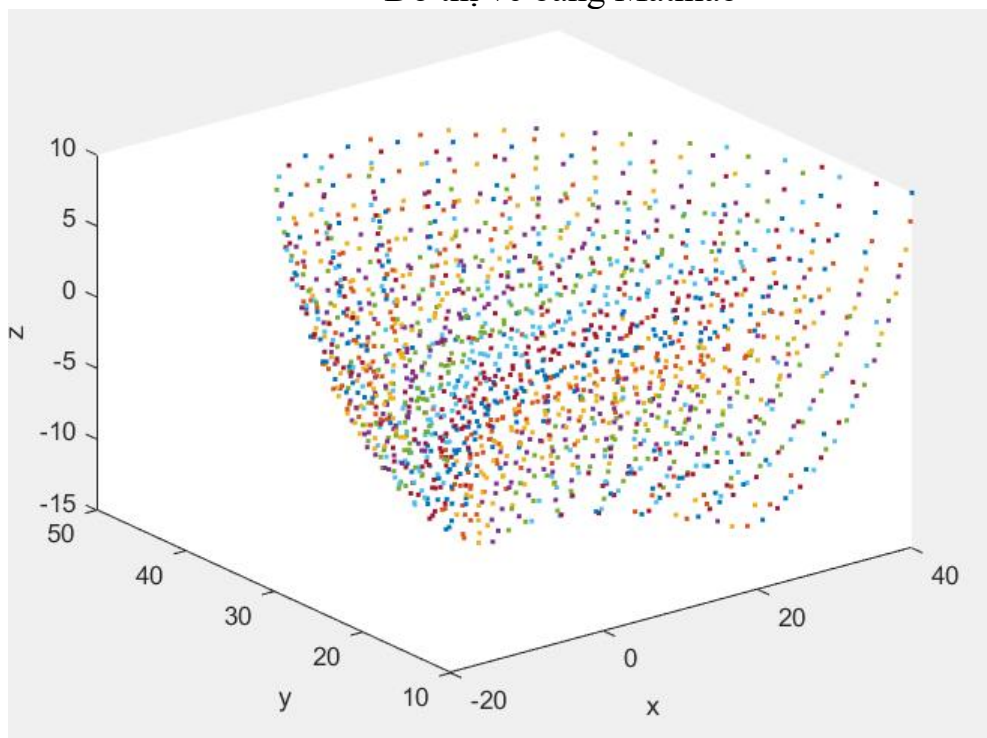
$$x = l_2 \cos(t_1) - l_6 (\cos(t_3) \sin(t_1) + \cos(t_1) \cos(t_2) \sin(t_3)) - l_5 (\sin(t_1) \sin(t_3) - \cos(t_1) \cos(t_2) \cos(t_3)) - l_3 \sin(t_1) - l_7 (\cos(t_4) (\sin(t_1) \sin(t_3) - \cos(t_1) \cos(t_2) \cos(t_3)) + \cos(t_1) \sin(t_2) \sin(t_4)) + l_4 \cos(t_1) \cos(t_2) - l_8 \cos(t_1) \sin(t_2)$$

$$y = l_5 (\cos(t_1) \sin(t_3) + \cos(t_2) \cos(t_3) \sin(t_1)) + l_6 (\cos(t_1) \cos(t_3) - \cos(t_2) \sin(t_1) \sin(t_3)) + l_3 \cos(t_1) + l_2 \sin(t_1) + l_7 (\cos(t_4) (\cos(t_1) \sin(t_3) + \cos(t_2) \cos(t_3) \sin(t_1)) - \sin(t_1) \sin(t_2) \sin(t_4)) + l_4 \cos(t_2) \sin(t_1) - l_8 \sin(t_1) \sin(t_2)$$

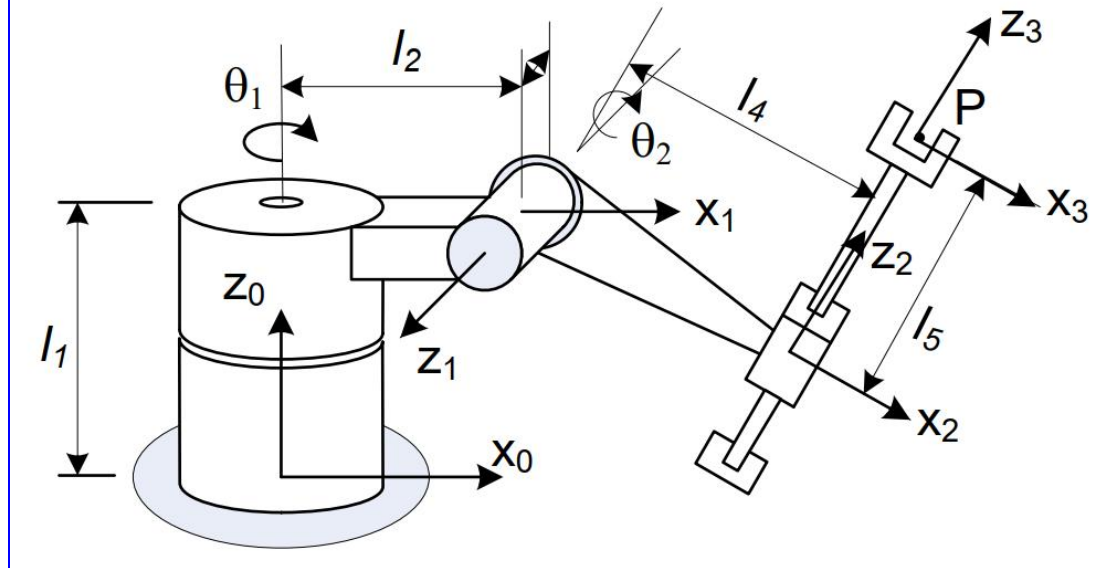
z=

$$l_1 - l_7 (\cos(t_2) \sin(t_4) + \cos(t_3) \cos(t_4) \sin(t_2)) - l_8 \cos(t_2) - l_4 \sin(t_2) - l_5 \cos(t_3) \sin(t_2) + l_6 \sin(t_2) \sin(t_3)$$

Đồ thị vẽ bằng Matlab



Bài 4



$$\begin{aligned}
 {}^0P &= {}^0T_4 \cdot {}^4P \\
 &= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4P \\
 &= R(z, \theta_1) * T(l_2, 0, l_1) * R(y, \theta_2) * T(l_4, 0, l_5) * P \\
 &= \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_2 & 0 & \sin\theta_2 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_2 & 0 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}
 \end{aligned}$$

$$\begin{aligned}
 &\times \begin{bmatrix} 1 & 0 & 0 & l_4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_5 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \\
 &= \begin{bmatrix} \cos(t_1) * (l_2 + l_4 * \cos(t_2) + l_5 * \sin(t_2)) \\ \sin(t_1) * (l_2 + l_4 * \cos(t_2) + l_5 * \sin(t_2)) \\ l_1 + l_5 * \cos(t_2) - l_4 * \sin(t_2) \\ 1 \end{bmatrix}
 \end{aligned}$$

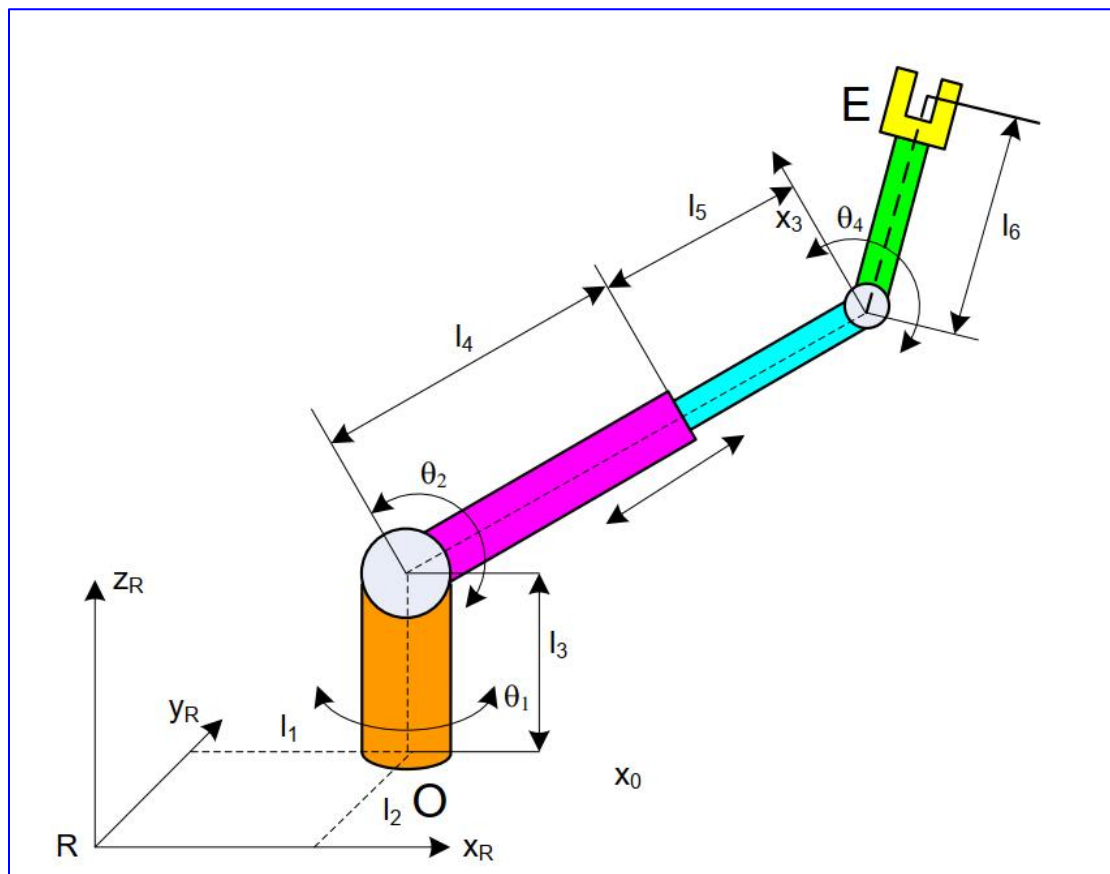
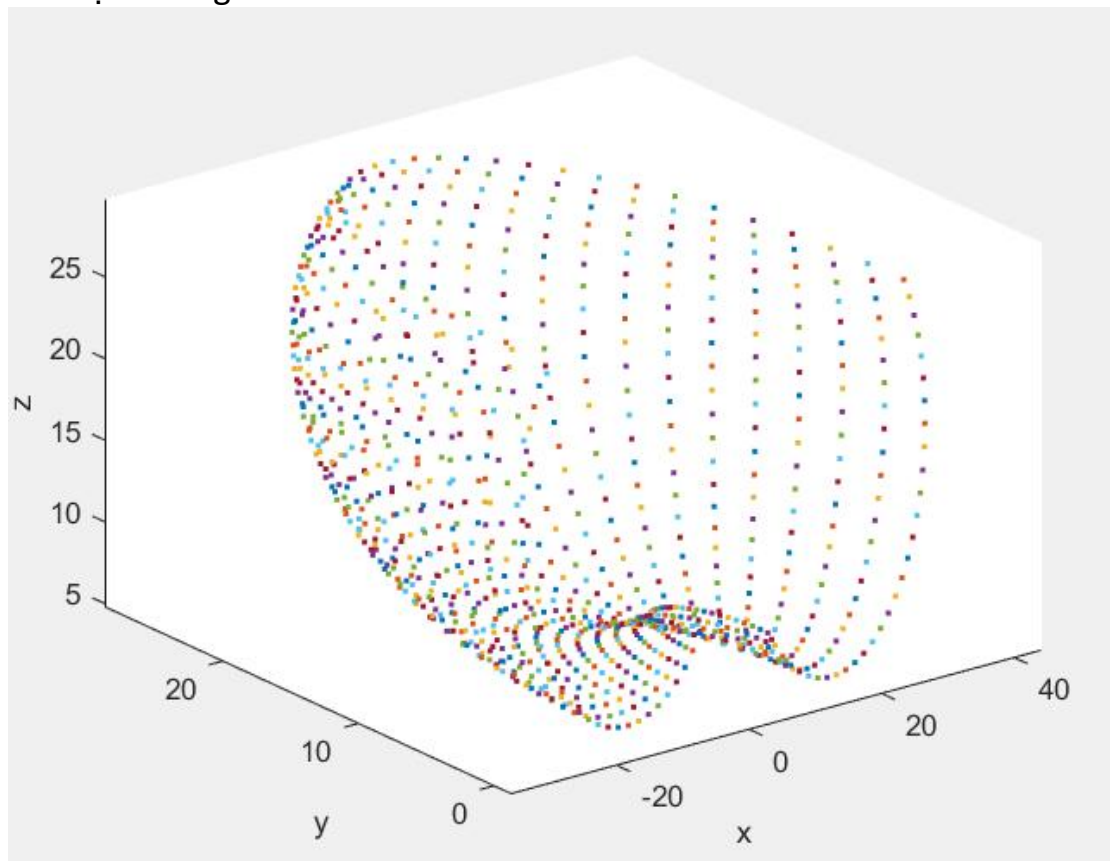
Vậy

$$x = \cos(t_1) * (l_2 + l_4 * \cos(t_2) + l_5 * \sin(t_2))$$

$$y = \sin(t_1) * (l_2 + l_4 * \cos(t_2) + l_5 * \sin(t_2))$$

$$z = l_1 + l_5 * \cos(t_2) - l_4 * \sin(t_2)$$

Đồ thị vẽ bằng Matlab



$$\begin{aligned}
{}^0P &= {}^0T_7 \cdot {}^7P \\
&= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5T_6 \cdot {}^6T_7 \cdot {}^7P \\
&= T(l_1, l_2, 0) * R(z, \theta_1) * T(0, 0, l_3) * R(y, \theta_2) * T(l_4 + l_5, 0, 0) * R(y, \theta_4) \\
&\quad * T(l_6, 0, 0) * P
\end{aligned}$$

$$= \begin{bmatrix} 1 & 0 & 0 & l_1 \\ 0 & 1 & 0 & l_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} \cos\theta_2 & 0 & \sin\theta_2 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_2 & 0 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_4 + l_5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_4 & 0 & \sin\theta_4 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_4 & 0 & \cos\theta_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & l_6 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} l_1 + \cos(t_1) * \cos(t_2) * (l_4 + l_5) + l_6 * \cos(t_2 + t_4) * \cos(t_1) \\ l_2 + \cos(t_2) * \sin(t_1) * (l_4 + l_5) + l_6 * \cos(t_2 + t_4) * \sin(t_1) \\ l_3 - \sin(t_2) * (l_4 + l_5) - l_6 * \sin(t_2 + t_4) \\ 1 \end{bmatrix}$$

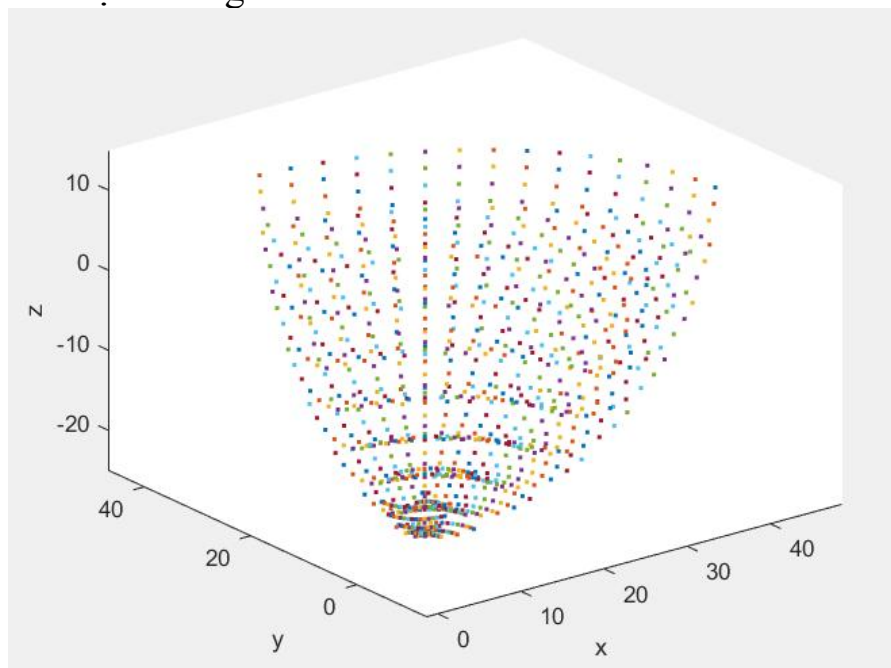
Vậy

$$x = l_1 + \cos(t_1) * \cos(t_2) * (l_4 + l_5) + l_6 * \cos(t_2 + t_4) * \cos(t_1)$$

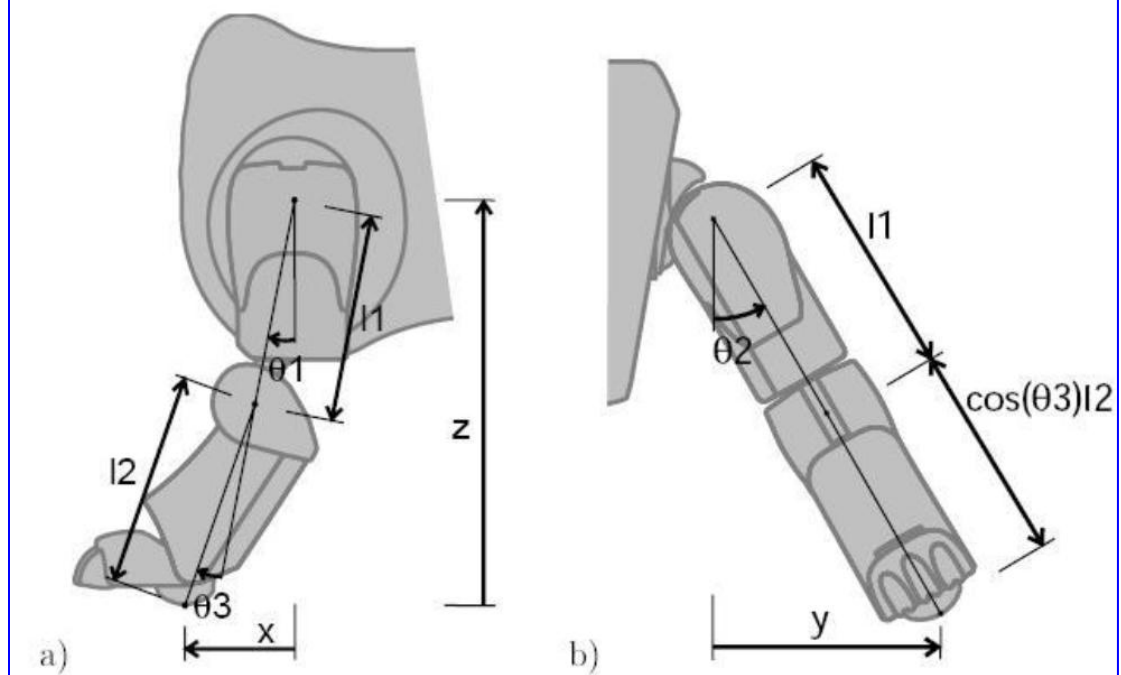
$$y = l_2 + \cos(t_2) * \sin(t_1) * (l_4 + l_5) + l_6 * \cos(t_2 + t_4) * \sin(t_1)$$

$$z = l_3 - \sin(t_2) * (l_4 + l_5) - l_6 * \sin(t_2 + t_4)$$

Đồ thị vẽ bằng Matlab



Bài 5



Chọn gốc tọa độ ở tâm xoay góc θ_1

$${}^0P = {}^0T_5 \cdot {}^5P$$

$$= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5P$$

$$= R(y, \theta_1) \cdot R(x, \theta_2) \cdot T(0, 0, l_1) \cdot R(y, \theta_3) \cdot T(0, 0, l_2) \cdot P$$

$$= \begin{bmatrix} \cos\theta_1 & 0 & \sin\theta_1 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_1 & 0 & \cos\theta_1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_2 & -\sin\theta_2 & 0 \\ 0 & \sin\theta_2 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} \cos\theta_3 & 0 & \sin\theta_3 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_3 & 0 & \cos\theta_3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} \cos(t_2) * \sin(t_1) * (l_1 + l_2) \\ -\sin(t_2) * (l_1 + l_2) \\ \cos(t_1) * \cos(t_2) * (l_1 + l_2) \\ 1 \end{bmatrix}$$

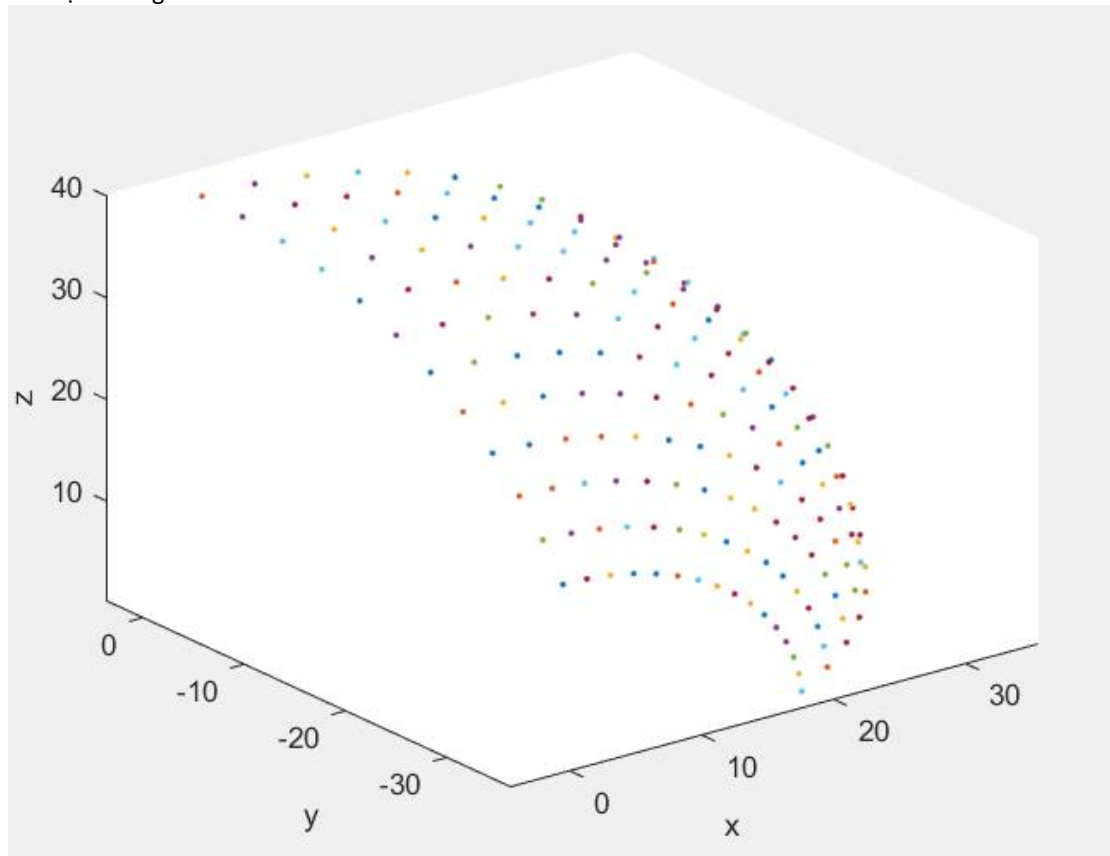
Vậy

$$Xx = \cos(t_2) * \sin(t_1) * (l_1 + l_2)$$

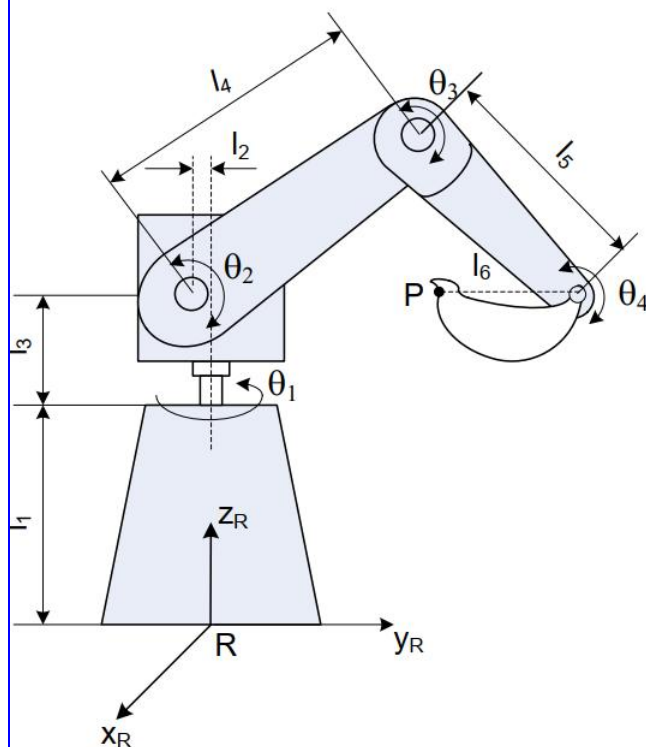
$$Yy = -\sin(t_2) * (l_1 + l_2)$$

$$Zz = \cos(t_1) * \cos(t_2) * (l_1 + l_2)$$

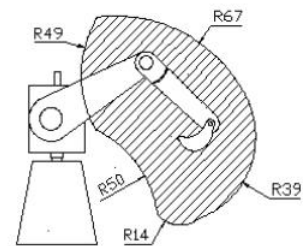
Đồ thị vẽ bằng Matlab



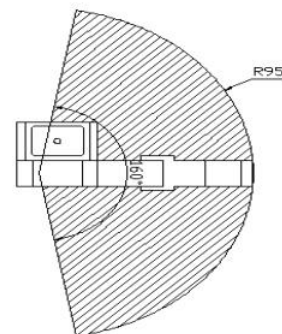
Bài 6



Chiếu cạnh



Chiếu bằng



$$\begin{aligned}
{}^0P &= {}^0T_7 \cdot {}^7P \\
&= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5T_6 \cdot {}^6T_7 \cdot {}^7P \\
&= T(0,0,l_1) * R(z,\theta_1) * T(0,-l_2,l_3) * R(x,\theta_2) * T(0,l_4,0) * R(x,\theta_3) \\
&\quad * T(0,l_5,0) * R(x,\theta_4) * T(0,-l_6,0) * P
\end{aligned}$$

$$= \begin{bmatrix} 1 & 0 & 0 & l_1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -l_2 \\ 0 & 0 & 1 & l_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} \cos\theta_2 & 0 & \sin\theta_2 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_2 & 0 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_4 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_3 & 0 & \sin\theta_3 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_3 & 0 & \cos\theta_3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_4 & 0 & \sin\theta_4 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_4 & 0 & \cos\theta_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -l_6 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} l_2 * \sin(t_1) + l_5 * \sin(t_2 + t_3) * \cos(t_1) + l_4 * \cos(t_1) * \sin(t_2) - l_6 * \sin(t_2 + t_3 + t_4) * \cos(t_1) \\ l_5 * \sin(t_2 + t_3) * \sin(t_1) - l_2 * \cos(t_1) + l_4 * \sin(t_1) * \sin(t_2) - l_6 * \sin(t_2 + t_3 + t_4) * \sin(t_1) \\ l_1 + l_3 + l_5 * \cos(t_2 + t_3) + l_4 * \cos(t_2) - l_6 * \cos(t_2 + t_3 + t_4) \\ 1 \end{bmatrix}$$

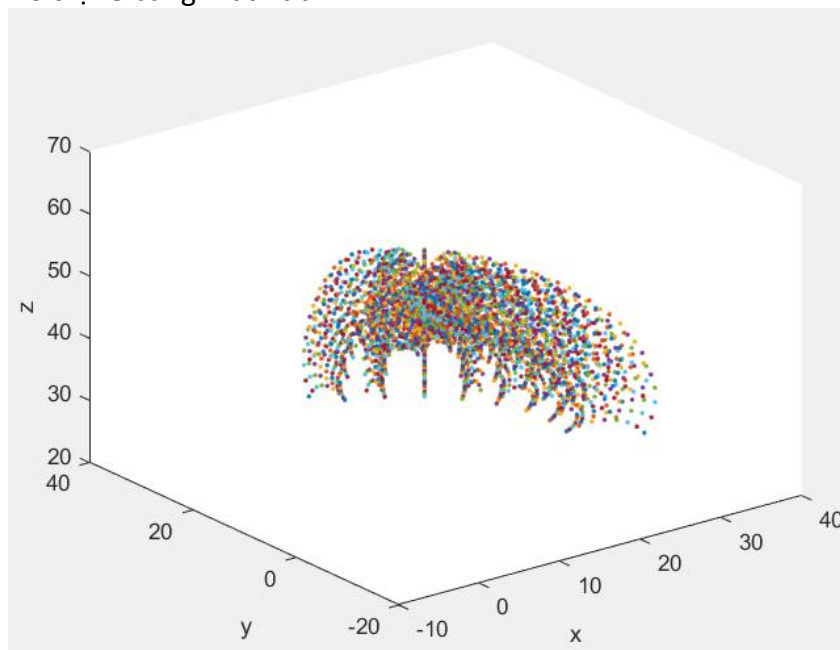
Vậy

$$x = l_2 * \sin(t_1) + l_5 * \sin(t_2 + t_3) * \cos(t_1) + l_4 * \cos(t_1) * \sin(t_2) - l_6 * \sin(t_2 + t_3 + t_4) * \cos(t_1)$$

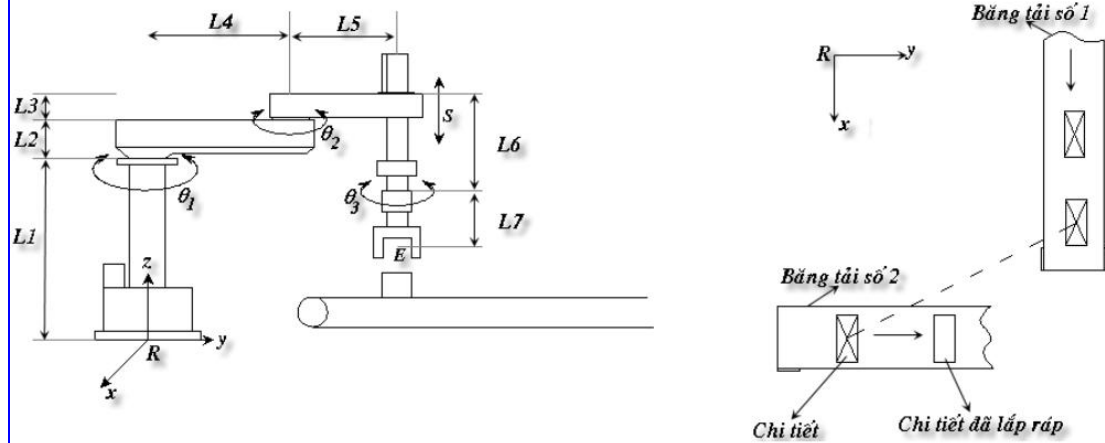
$$y = l_5 * \sin(t_2 + t_3) * \sin(t_1) - l_2 * \cos(t_1) + l_4 * \sin(t_1) * \sin(t_2) - l_6 * \sin(t_2 + t_3 + t_4) * \sin(t_1)$$

$$z = l_1 + l_3 + l_5 * \cos(t_2 + t_3) + l_4 * \cos(t_2) - l_6 * \cos(t_2 + t_3 + t_4)$$

Đồ thị vẽ bằng Matlab



Bài 7



$${}^0P = {}^0T_7 \cdot {}^7P$$

$$= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5T_6 \cdot {}^6T_7 \cdot {}^7P$$

$$= T(0,0,l_1) * R(z,\theta_1) * T(0,l_4,l_2) * R(z,\theta_2) * T(0,l_5,l_3-l_6+s) * R(z,\theta_3)$$

$$* T(0,0,-l_7) * P$$

$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_4 \\ 0 & 0 & 1 & l_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} \cos\theta_2 & -\sin\theta_2 & 0 & 0 \\ \sin\theta_2 & \cos\theta_2 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_5 \\ 0 & 0 & 1 & l_3 - l_6 + s \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_3 & -\sin\theta_3 & 0 & 0 \\ \sin\theta_3 & \cos\theta_3 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -l_7 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} -l_5 * \sin(t_1 + t_2) - l_4 * \sin(t_1) \\ l_5 * \cos(t_1 + t_2) + l_4 * \cos(t_1) \\ l_1 + l_2 + l_3 - l_6 - l_7 + s \\ 1 \end{bmatrix}$$

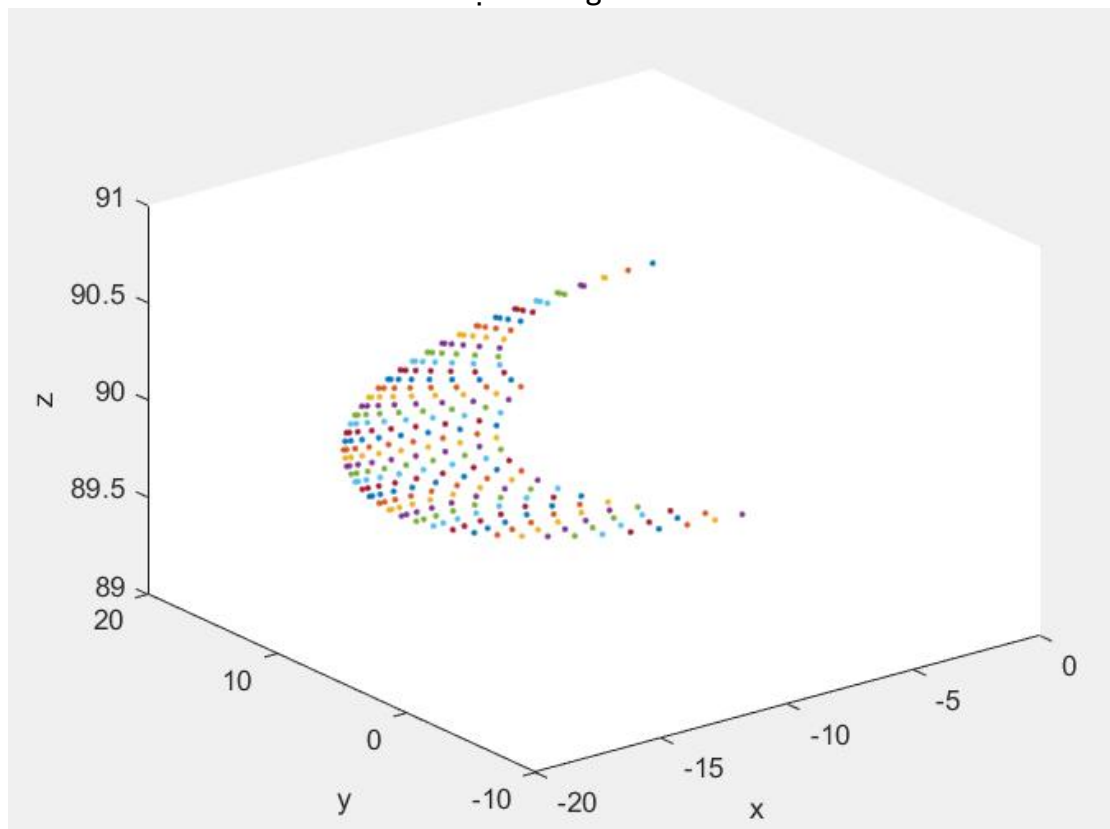
Vậy

$$X = -l_5 * \sin(t_1 + t_2) - l_4 * \sin(t_1)$$

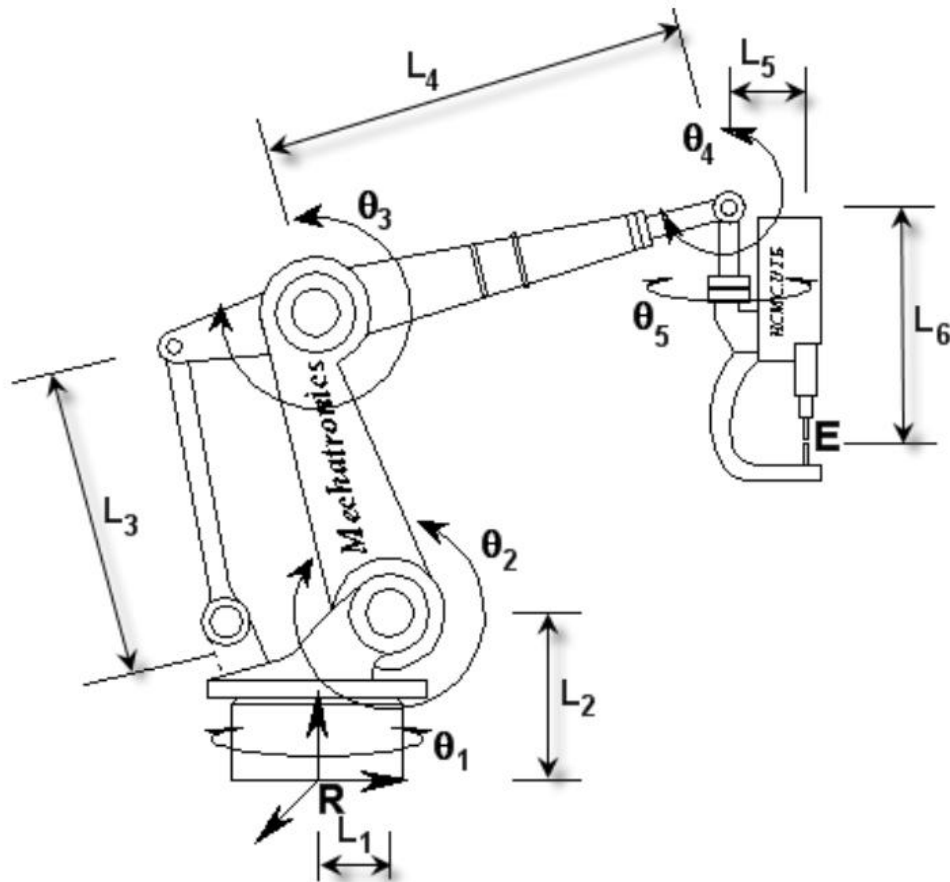
$$Y = I_5 \cos(t_1 + t_2) + I_4 \cos(t_1)$$

$$Z = I_1 + I_2 + I_3 - I_6 - I_7 + s$$

Đồ thị vẽ bằng Matlab



Bài 8



$${}^0P = {}^0T_9 \cdot {}^9P$$

$$= {}^0T_1 \cdot {}^1T_2 \cdot {}^2T_3 \cdot {}^3T_4 \cdot {}^4T_5 \cdot {}^5T_6 \cdot {}^6T_7 \cdot {}^7T_8 \cdot {}^8T_9 \cdot {}^9P$$

$$= R(z, \theta_1) * T(l_1, 0, l_2) * R(y, \theta_2) * T(0, 0, l_3) * R(y, \theta_3)$$

$$* T(l_4, 0, 0) * R(y, \theta_4) * R(z, \theta_5) * T(l_5, 0, l_6) * P$$

$$= \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_2 & 0 & \sin\theta_2 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_2 & 0 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_3 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_3 & 0 & \sin\theta_3 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_3 & 0 & \cos\theta_3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & l_4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} \cos\theta_4 & 0 & \sin\theta_4 & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta_4 & 0 & \cos\theta_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_5 & -\sin\theta_5 & 0 & 0 \\ \sin\theta_5 & \cos\theta_5 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_5 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} l1 + l6 * \sin(t2 + t3) * \cos(t1) + l4 * \cos(t1) * \cos(t2) - l6 * \sin(t2 + t3 + t4) * \cos(t1) \\ \sin(t1) * (l6 * \sin(t2 + t3) + l4 * \cos(t2) - l6 * \sin(t2 + t3 + t4)) \\ l2 + l3 + l6 * \cos(t2 + t3) - l4 * \sin(t2) - l6 * \cos(t2 + t3 + t4) \end{bmatrix}$$

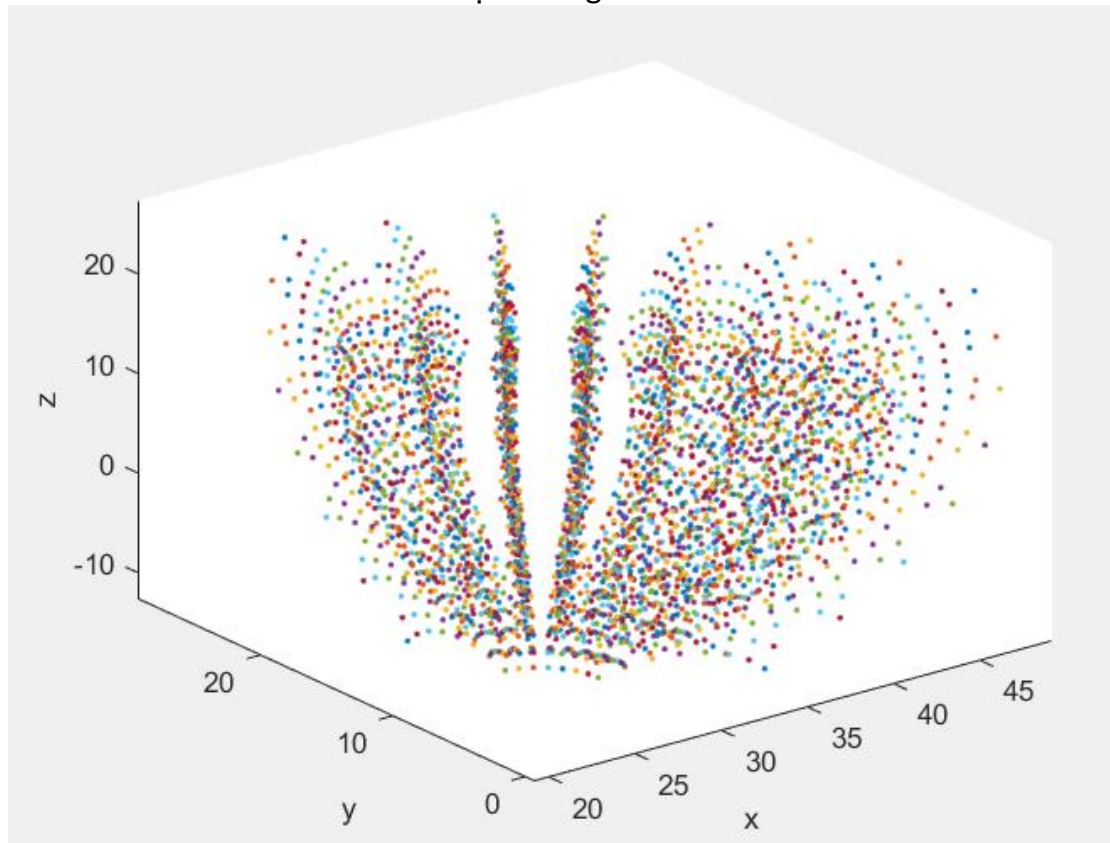
Vậy

$$X = l1 + l6 * \sin(t2 + t3) * \cos(t1) + l4 * \cos(t1) * \cos(t2) - l6 * \sin(t2 + t3 + t4) * \cos(t1)$$

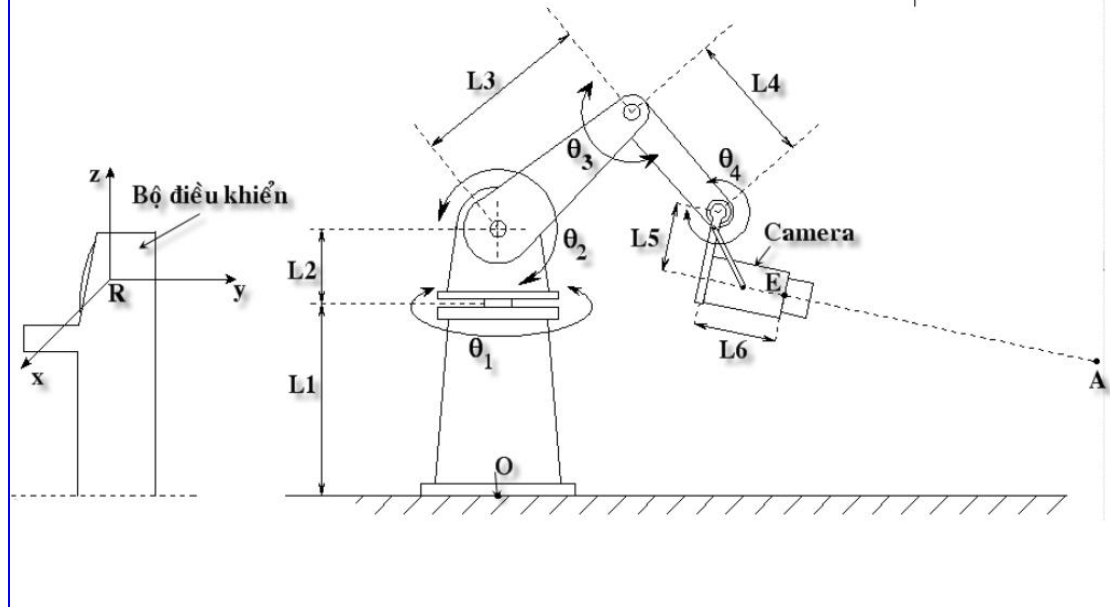
$$Y = \sin(t1) * (l6 * \sin(t2 + t3) + l4 * \cos(t2) - l6 * \sin(t2 + t3 + t4))$$

$$Z = l2 + l3 + l6 * \cos(t2 + t3) - l4 * \sin(t2) - l6 * \cos(t2 + t3 + t4)$$

Đồ thị vẽ bằng Matlab



Bài 10



$$\begin{aligned}
 {}^O P &= {}^O T_9 \cdot {}^9 P \\
 &= {}^O T_1 \cdot {}^1 T_2 \cdot {}^2 T_3 \cdot {}^3 T_4 \cdot {}^4 T_5 \cdot {}^5 T_6 \cdot {}^6 T_7 \cdot {}^7 T_8 \cdot {}^8 T_9 \cdot {}^9 P \\
 &= T(0,0,l_1) * R(z,\theta_1) * T(0,0,l_2) * R(x,\theta_2) * T(0,l_3,0) * R(x,\theta_3) \\
 &\quad * T(0,l_4,0) * R(x,\theta_4) * T(0,l_6,l_5) * P
 \end{aligned}$$

$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \cos\theta_1 & -\sin\theta_1 & 0 & 0 \\ \sin\theta_1 & \cos\theta_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & l_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_2 & -\sin\theta_2 & 0 \\ 0 & \sin\theta_2 & \cos\theta_2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_3 & -\sin\theta_3 & 0 \\ 0 & \sin\theta_3 & \cos\theta_3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_4 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_4 & -\sin\theta_4 & 0 \\ 0 & \sin\theta_4 & \cos\theta_4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_6 \\ 0 & 0 & 1 & l_5 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} -\sin(t_1) * (l_4 * \cos(t_2 + t_3) + l_3 * \cos(t_2) + l_6 * \cos(t_2 + t_3 + t_4) - l_5 * \sin(t_2 + t_3 + t_4)) \\ \cos(t_1) * (l_4 * \cos(t_2 + t_3) + l_3 * \cos(t_2) + l_6 * \cos(t_2 + t_3 + t_4) - l_5 * \sin(t_2 + t_3 + t_4)) \\ l_1 + l_2 + l_4 * \sin(t_2 + t_3) + l_3 * \sin(t_2) + l_5 * \cos(t_2 + t_3 + t_4) + l_6 * \sin(t_2 + t_3 + t_4) \\ 1 \end{bmatrix}$$

Vậy

$$X = -\sin(t_1) \cdot (l_4 \cdot \cos(t_2 + t_3) + l_3 \cdot \cos(t_2) + l_6 \cdot \cos(t_2 + t_3 + t_4) - l_5 \cdot \sin(t_2 + t_3 + t_4))$$

$$Y = \cos(t_1) \cdot (l_4 \cdot \cos(t_2 + t_3) + l_3 \cdot \cos(t_2) + l_6 \cdot \cos(t_2 + t_3 + t_4) - l_5 \cdot \sin(t_2 + t_3 + t_4))$$

$$Z = l_1 + l_2 + l_4 \cdot \sin(t_2 + t_3) + l_3 \cdot \sin(t_2) + l_5 \cdot \cos(t_2 + t_3 + t_4) + l_6 \cdot \sin(t_2 + t_3 + t_4)$$

Đồ thị vẽ bằng Matlab

