$$M = 4, n = 2$$
:

Original equation:

$$+6f_{-1}^{2}f_{0}^{2} + 4f_{-1}^{3}f_{1} + 4f_{-2}f_{0}^{3} + 24f_{-2}f_{-1}f_{0}f_{1} + 12f_{-2}f_{-1}^{2}f_{2}$$

$$+6f_{-2}^{2}f_{1}^{2} + 12f_{-2}^{2}f_{0}f_{2} + 12f_{-2}^{2}f_{-1}f_{3} + 4f_{-2}^{3}f_{4}$$

$$+12f_{-3}f_{0}^{2}f_{1} + 12f_{-3}f_{-1}f_{1}^{2} + 24f_{-3}f_{-1}f_{0}f_{2} + 12f_{-3}f_{-1}^{2}f_{3}$$

$$+24f_{-3}f_{-2}f_{1}f_{2} + 24f_{-3}f_{-2}f_{0}f_{3} + 24f_{-3}f_{-2}f_{-1}f_{4}$$

$$+6f_{-3}^{2}f_{2}^{2} + 12f_{-3}^{2}f_{1}f_{3} + 12f_{-3}^{2}f_{0}f_{4} + 12f_{-4}f_{0}f_{1}^{2}$$

$$+12f_{-4}f_{0}^{2}f_{2} + 24f_{-4}f_{-1}f_{1}f_{2} + 24f_{-4}f_{-1}f_{0}f_{3} + 12f_{-4}f_{-1}^{2}f_{4}$$

$$+12f_{-4}f_{-2}f_{2}^{2} + 24f_{-4}f_{-2}f_{1}f_{3} + 24f_{-4}f_{-2}f_{0}f_{4}$$

$$+24f_{-4}f_{-3}f_{2}f_{3} + 24f_{-4}f_{-3}f_{1}f_{4} + 6f_{-4}^{2}f_{3}^{2} + 12f_{-4}^{2}f_{2}f_{4} = 0$$

$$(1)$$

Equivalent equation, where $f_{-j} = \overline{f_j}$:

$$4f_{0}^{3}\overline{f_{2}} + 12f_{0}^{2}f_{1}\overline{f_{3}} + 12f_{0}^{2}f_{2}\overline{f_{4}} + 6f_{0}^{2}\overline{f_{1}}^{2} + 12f_{0}f_{1}^{2}\overline{f_{4}} + 24f_{0}f_{1}\overline{f_{1}f_{2}} + 24f_{0}f_{2}\overline{f_{1}f_{3}} + 12f_{0}f_{2}\overline{f_{2}}^{2} + 24f_{0}f_{3}\overline{f_{1}f_{4}} + 24f_{0}f_{3}\overline{f_{2}f_{3}} + 24f_{0}f_{4}\overline{f_{2}f_{4}} + 12f_{0}f_{4}\overline{f_{3}}^{2} + 12f_{1}^{2}\overline{f_{1}f_{3}} + 6f_{1}^{2}\overline{f_{2}}^{2} + 24f_{1}f_{2}\overline{f_{1}f_{4}} + 24f_{1}f_{2}\overline{f_{2}f_{3}} + 24f_{1}f_{3}\overline{f_{2}f_{4}} + 6f_{2}^{2}\overline{f_{3}}^{2} + 12f_{1}f_{3}\overline{f_{3}}^{2} + 24f_{1}f_{4}\overline{f_{3}f_{4}} + 4f_{1}\overline{f_{1}}^{3} + 12f_{2}^{2}\overline{f_{2}f_{4}} + 6f_{2}^{2}\overline{f_{3}}^{2} + 24f_{2}f_{3}\overline{f_{3}f_{4}} + 12f_{2}f_{4}\overline{f_{4}}^{2} + 12f_{2}\overline{f_{1}}^{2}\overline{f_{2}} + 6f_{3}^{2}\overline{f_{4}}^{2} + 12f_{3}\overline{f_{1}}^{2}\overline{f_{3}} + 12f_{3}\overline{f_{1}}^{2}\overline{f_{3}} + 24f_{4}\overline{f_{1}}^{2}\overline{f_{2}} + 24f_{4}\overline{f_{1}}^{2}\overline{f_{2}} + 4f_{4}\overline{f_{2}}^{3} = 0$$

$$(2)$$

All possible solutions:

$$\{f_1:0, f_2:0, f_3:0\}$$
 (3)

$$\{f_1:0,\quad f_2:0,\quad f_3:0\}$$
 (4)

$$\{f_1:0, f_2:0, f_4:0\}$$
 (5)

$$\{f_1:0, f_2:0, f_3:0, f_4:0\}$$
 (6)

Time elapsed: 2.372112512588501 seconds