M = 2, n = 3:

Original equation:

$$+10f_{-1}^{3}f_{0}^{2} + 5f_{-1}^{4}f_{1} + 20f_{-2}f_{-1}f_{0}^{3} + 60f_{-2}f_{-1}^{2}f_{0}f_{1} + 20f_{-2}f_{-1}^{3}f_{2} + 30f_{-2}^{2}f_{0}^{2}f_{1} + 30f_{-2}^{2}f_{-1}f_{1}^{2} + 60f_{-2}^{2}f_{-1}f_{0}f_{2} + 20f_{-2}^{3}f_{1}f_{2} = 0$$
 (1)

Simplified equation, where $f_{-j} = \overline{f_j}$:

$$20f_0^3\overline{f_1f_2} + 30f_0^2f_1\overline{f_2}^2 + 10f_0^2\overline{f_1}^3 + 60f_0f_1\overline{f_1}^2\overline{f_2} + 60f_0f_2\overline{f_1f_2}^2 + 30f_1^2\overline{f_1f_2}^2 + 20f_1f_2\overline{f_2}^3 + 5f_1\overline{f_1}^4 + 20f_2\overline{f_1}^3\overline{f_2} = 0$$
(2)

All possible solutions:

$$\{f_1:0\}\tag{3}$$

$$\{f_1:0,\quad f_2:0\}$$
 (4)