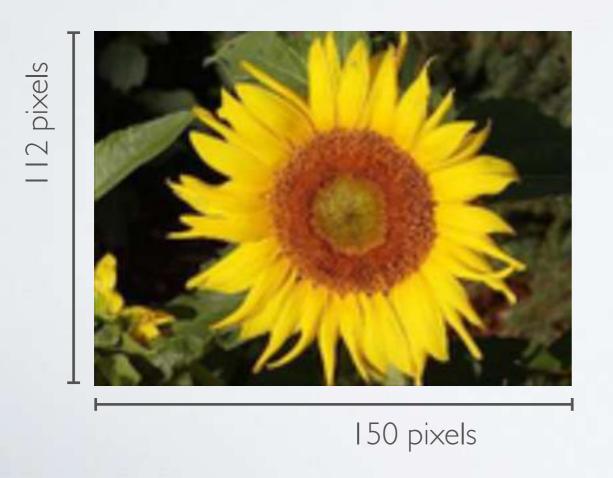
# Convolutional Networks I

Topics: computer vision, object recognition

- GOAL: Process visual data and accomplish some given task.
  - we will focus on object recognition: given some input image, identify which object it contains.



Caltech 101 dataset



"sun flower"

#### Topics: computer vision

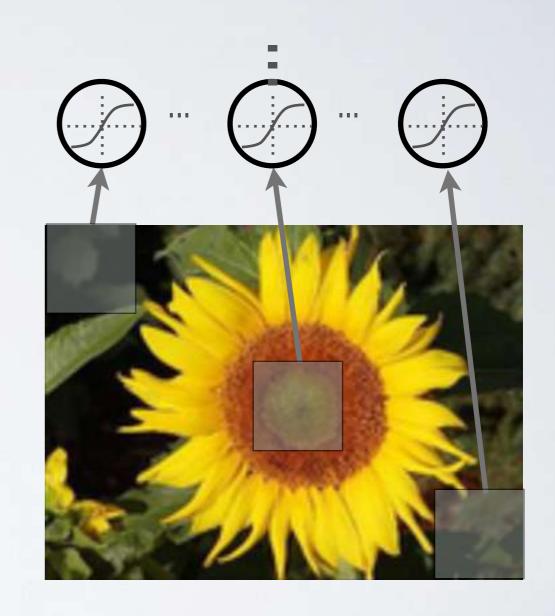
- We can design neural networks that are specifically adapted for such problems
  - can deal with very high-dimensional inputs
    - $150 \times 150$  pixels = 22500 inputs, or  $3 \times 22500$  if RGB pixels
  - can exploit the 2D topology of pixels (or 3D for video data)
  - can build-in invariance to certain variations we can expect
    - translations, illumination, etc.
- Convolutional networks leverage these ideas
  - local connectivity
  - parameter sharing
  - pooling / subsampling hidden units

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#### Topics: local connectivity

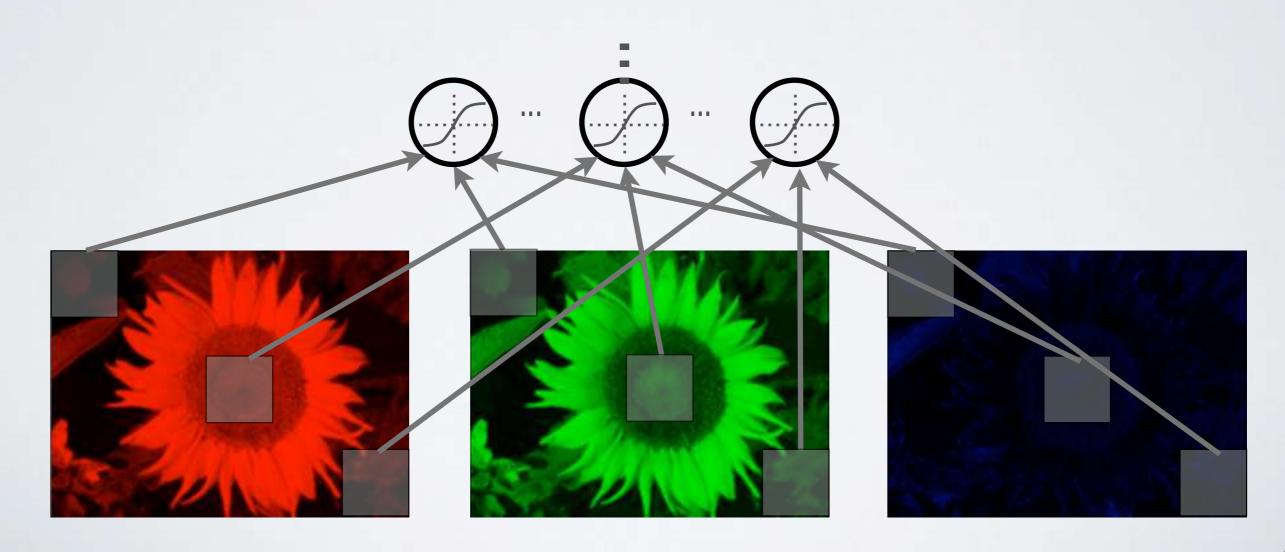
- First idea: use a local connectivity of hidden units
  - each hidden unit is connected only to a subregion (patch) of the input image
  - it is connected to all channels
    - I if greyscale image
    - 3 (R, G, B) for color image
- Solves the following problems:
  - fully connected hidden layer would have an unmanageable number of parameters
  - computing the linear activations of the hidden units would be very expensive



$$r = receptive field$$

#### Topics: local connectivity

- Units are connected to all channels:
  - ▶ I channel if grayscale image, 3 channels (R, G, B) if color image



#### Topics: parameter sharing

- · Second idea: share matrix of parameters across certain units
  - units organized into the same "feature map" share parameters
  - ▶ hidden units within a feature map cover different positions in the image



same color

=

same matrix

of connections

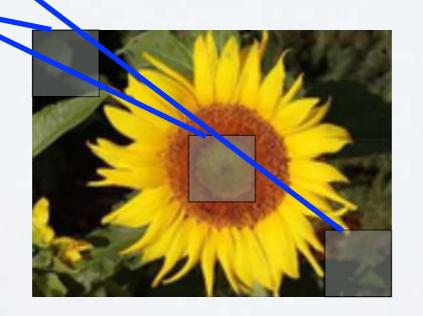


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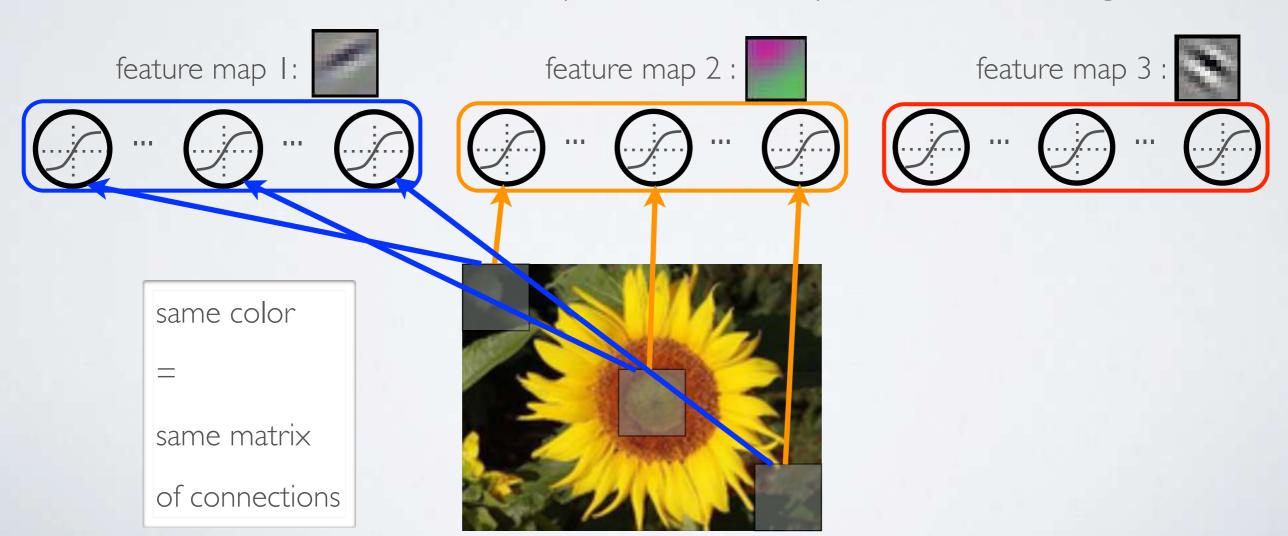


same color
=
same matrix
of connections



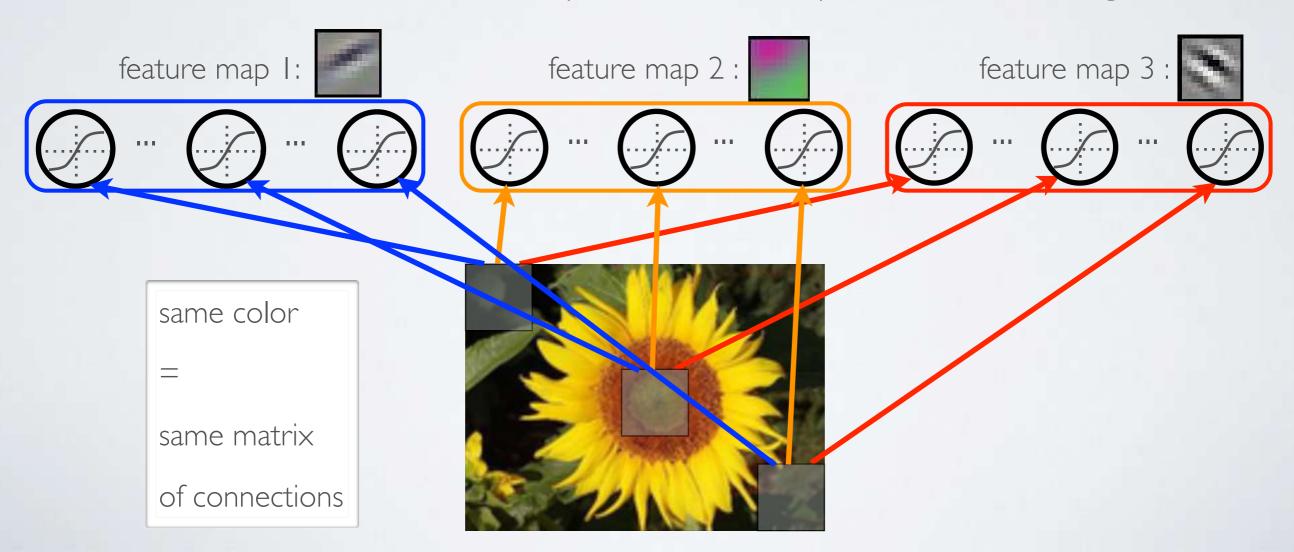
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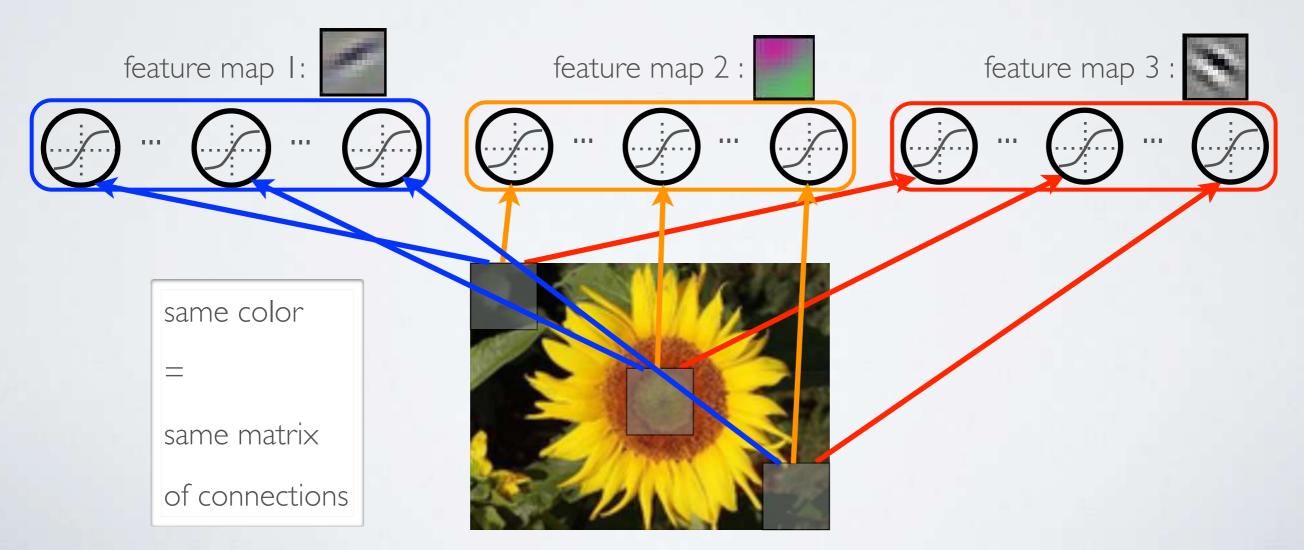
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#### Topics: parameter sharing

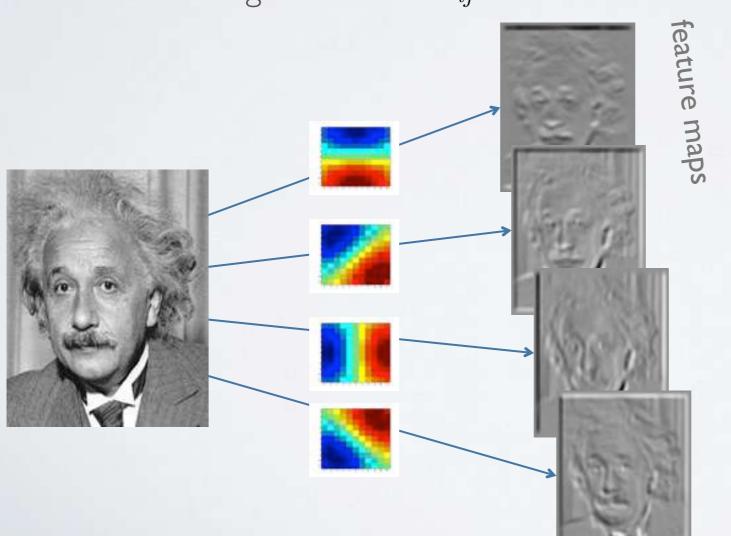
- Solves the following problems:
  - reduces even more the number of parameters
  - will extract the same features at every position (features are "equivariant")



#### Topics: parameter sharing

Jarret et al. 2009

- Each feature map forms a 2D grid of features
  - can be computed with a discrete convolution (\*) of a kernel matrix  $k_{ij}$  which is the hidden weights matrix  $W_{ij}$  with its rows and columns flipped



- $\rightarrow x_i$  is the i<sup>th</sup> channel of input
- $ightharpoonup k_{ij}$  is the convolution kernel
- $g_j$  is a learned scaling factor
- $y_j$  is the hidden layer

$$y_j = g_j \tanh(\sum_i k_{ij} * x_i)$$

#### Topics: discrete convolution

• The convolution of an image x with a kernel k is computed as follows:

Pre-activation

feature map

#### Topics: discrete convolution

• The convolution of an image x with a kernel k is computed as follows:

$$(x * k)_{ij} = \sum_{pq} x_{i+p,j+q} k_{r-p,r-q}$$

Example:

 $1 \times 0 + 0.5 \times 80 + 0.25 \times 20 + 0 \times 40$ 

#### Topics: discrete convolution

• The convolution of an image x with a kernel k is computed as follows:

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Example:

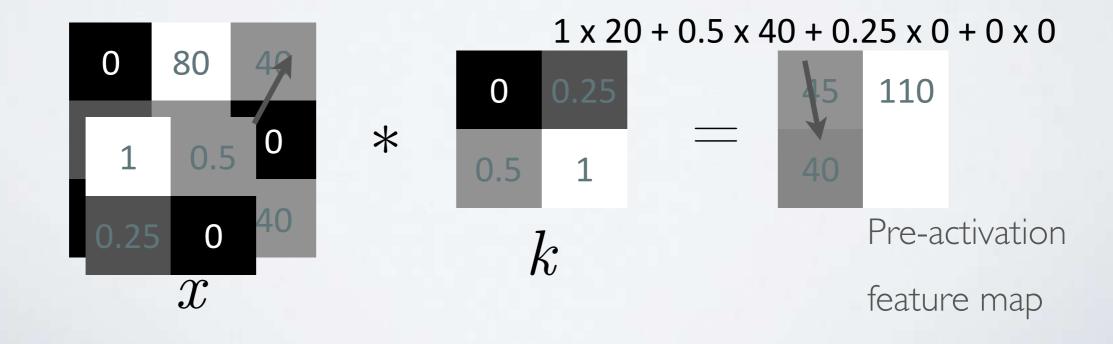
 $1 \times 80 + 0.5 \times 40 + 0.25 \times 40 + 0 \times 0$ 

#### Topics: discrete convolution

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• Example:

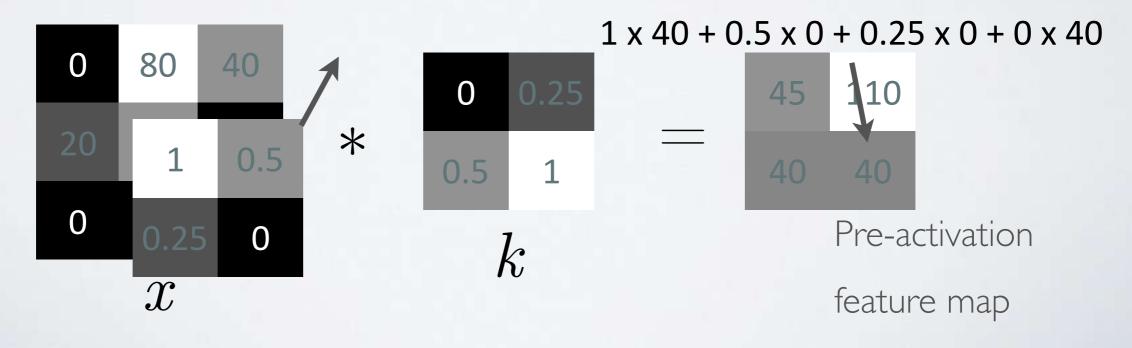


#### Topics: discrete convolution

• The convolution of an image x with a kernel k is computed as follows:

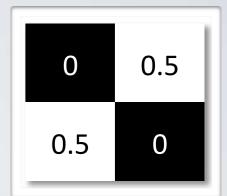
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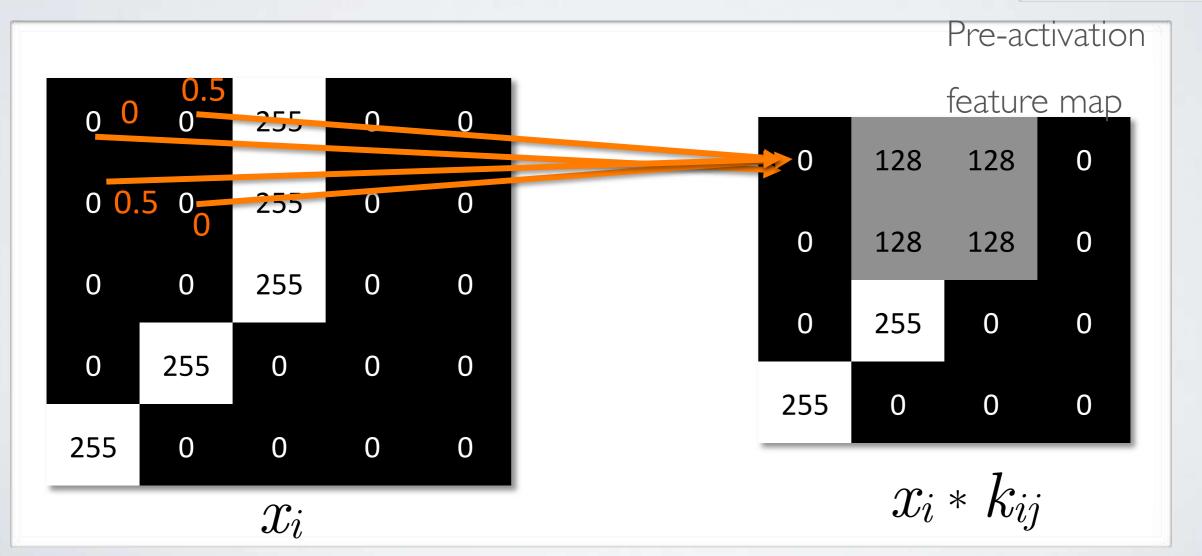
• Example:



Topics: discrete convolution

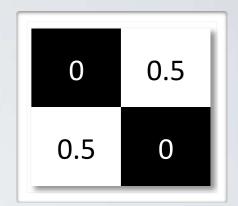
 $^{ullet}$  Simple illustration:  $x_i st k_{ij}$  where  $W_{ij} = W_{ij}$ 

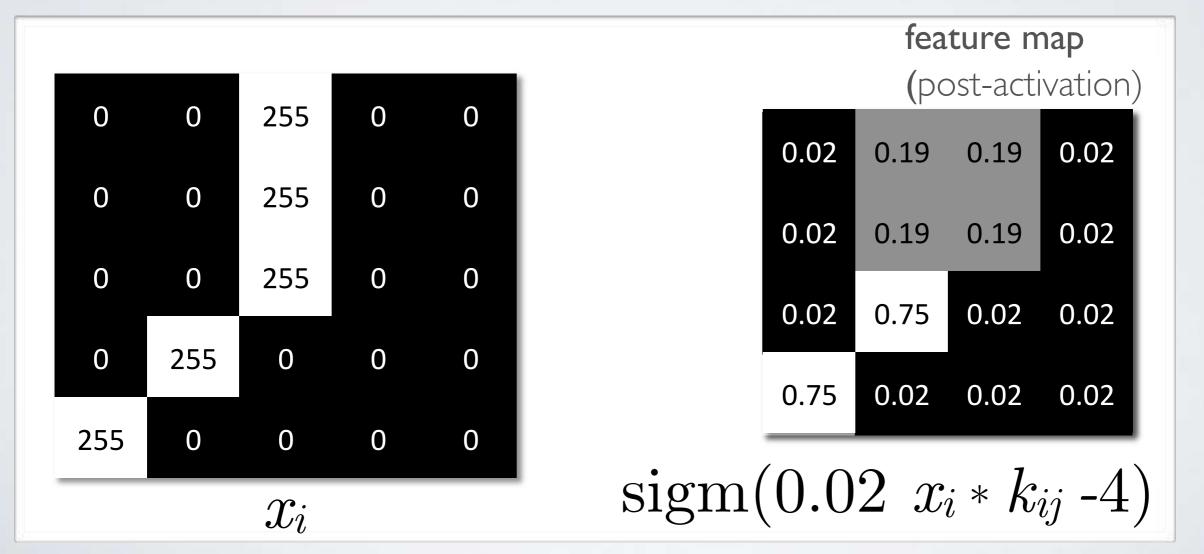




#### Topics: discrete convolution

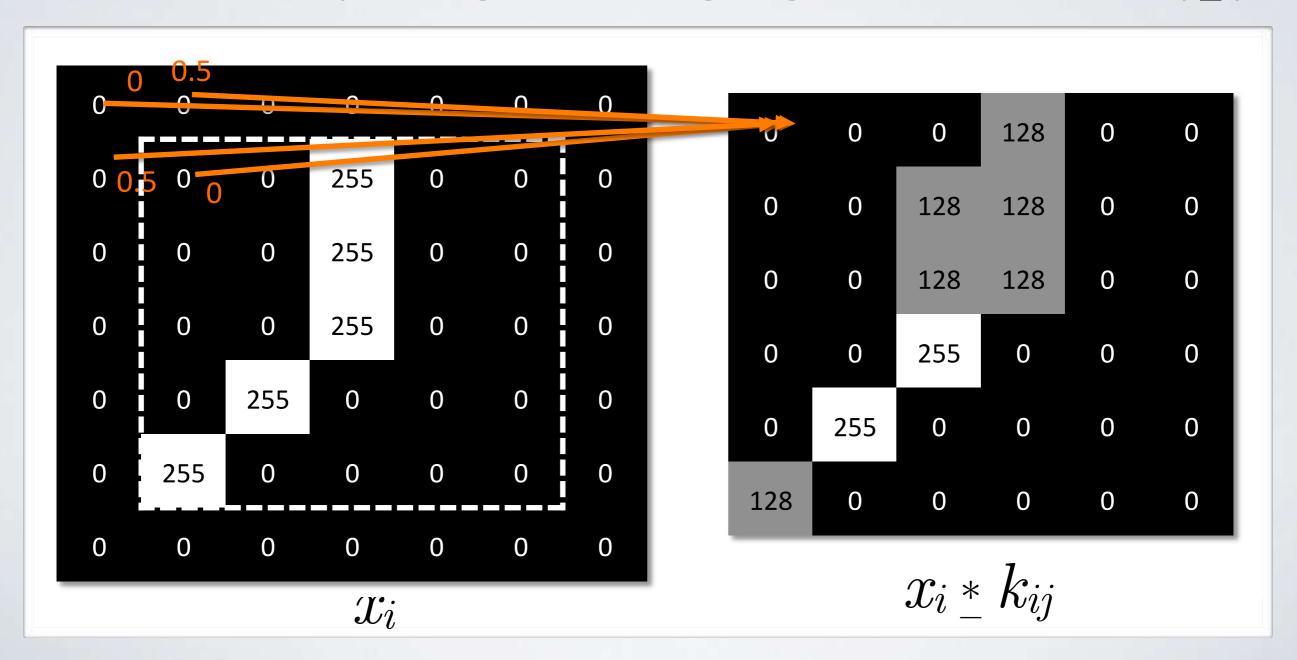
 With a non-linearity, we get a detector of a feature at any position in the image





Topics: discrete convolution

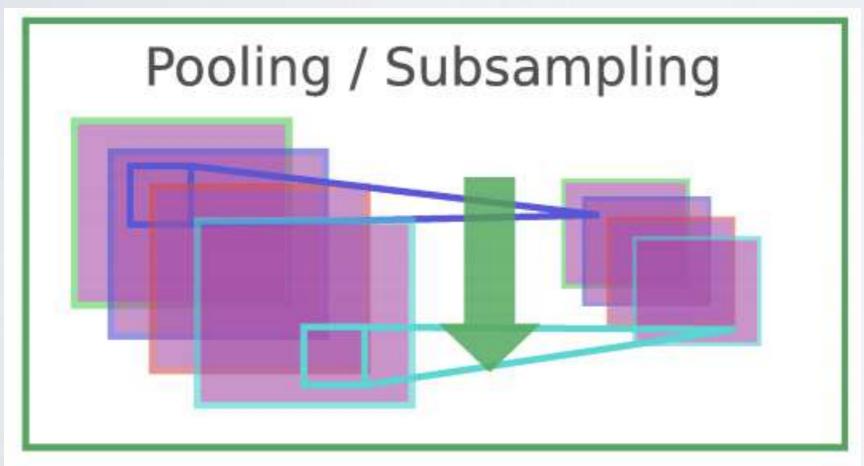
Can use "zero padding" to allow going over the borders (\*)



Topics: pooling and subsampling

Jarret et al. 2009

- · Third idea: pool hidden units in same neighborhood
  - pooling is performed in non-overlapping neighborhoods (subsampling)



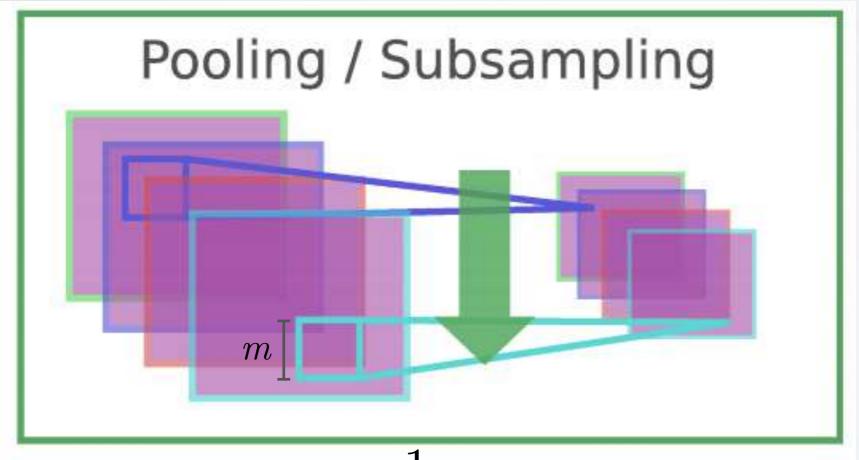
- $x_{i,j,k}$  is value of the i<sup>th</sup> feature map at position j,k
- p is vertical index in local neighborhood
- q is horizontal index in local neighborhood
- y<sub>ijk</sub> is pooled and subsampled layer

$$y_{ijk} = \max_{p,q} x_{i,j+p,k+q}$$

Topics: pooling and subsampling

Jarret et al. 2009

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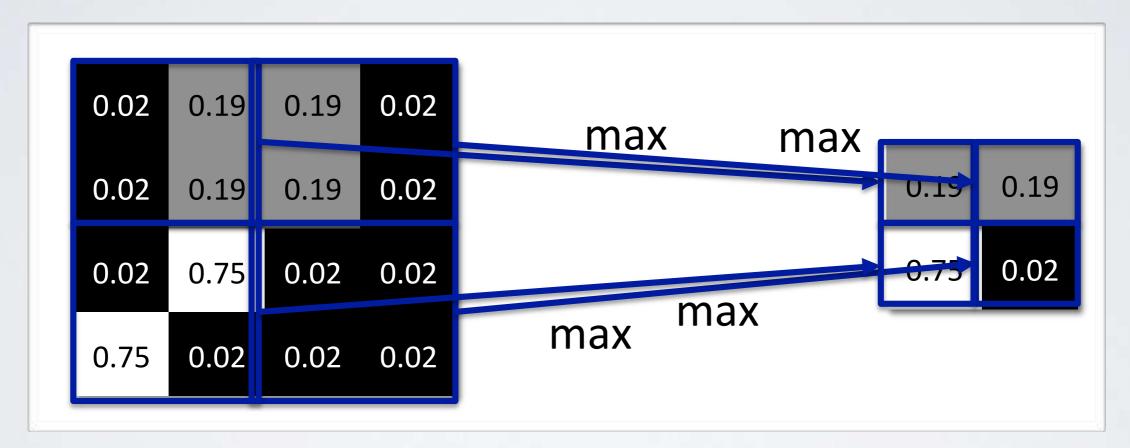


$$y_{ijk} = \frac{1}{m^2} \sum_{p,q} x_{i,j+p,k+q}$$

- $x_{i,j,k}$  is value of the i<sup>th</sup> feature map at position j,k
- p is vertical index in local neighborhood
- q is horizontal index in local neighborhood
- $y_{ijk}$  is pooled and subsampled layer
- *m* is the neighborhood height/width

#### Topics: pooling and subsampling

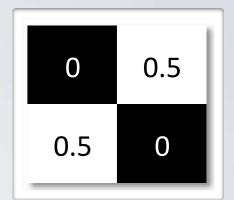
- · Third idea: pool hidden units in same neighborhood
  - pooling is performed in (mostly) non-overlapping neighborhoods (subsampling)



- Solves the following problems:
  - introduces invariance to local translations
  - reduces the number of hidden units in hidden layer

#### Topics: pooling and subsampling

- Illustration of local translation invariance
  - both images given the same feature map after pooling/subsampling

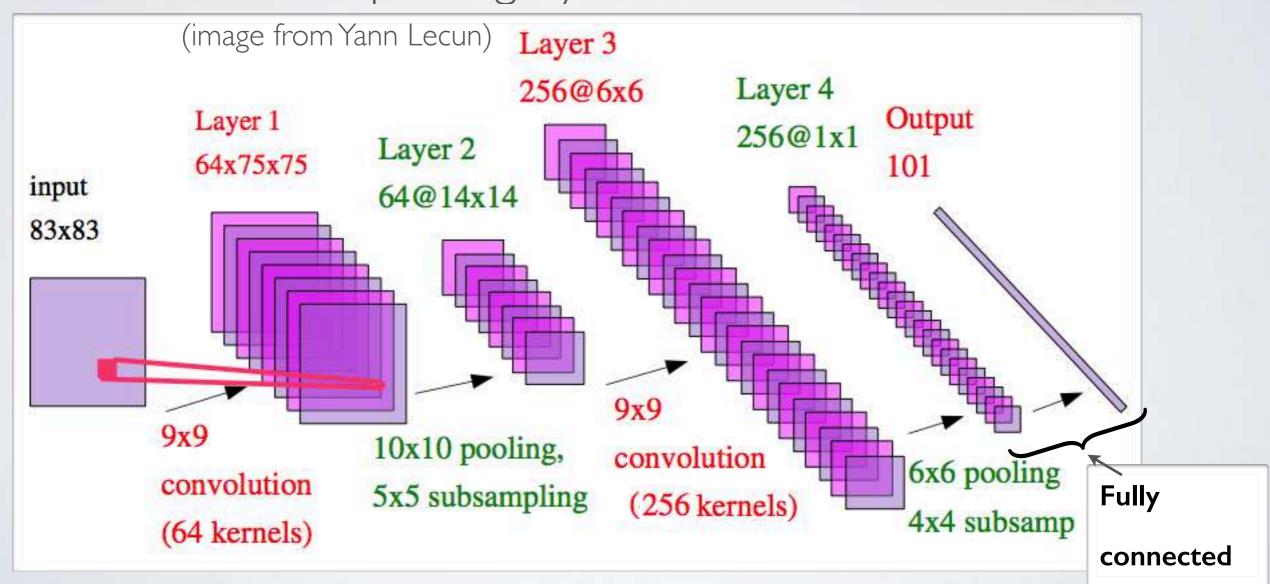




### CONVOLUTIONAL NETWORK

#### Topics: convolutional network

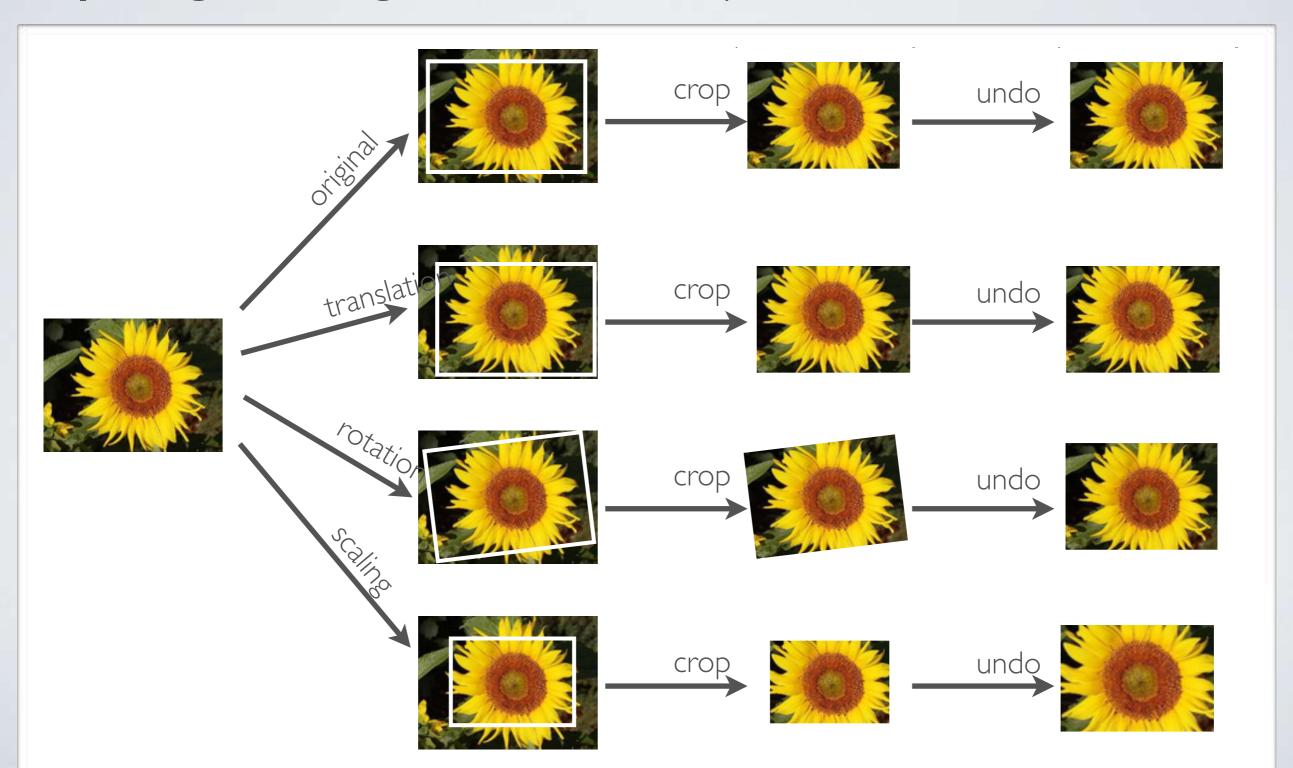
 Convolutional neural network alternates between the convolutional and pooling layers



#### Topics: generating additional examples

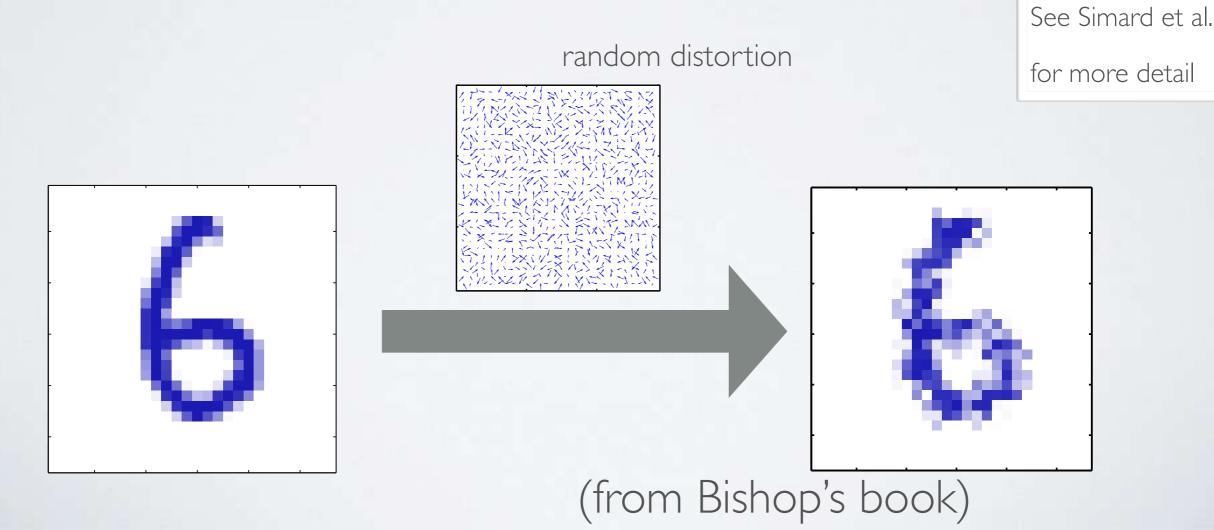
- Invariances built-in in convolutional network:
  - small translations: due to convolution and max pooling
- It is not invariant to other important variations such as rotations and scale changes
- However, it's easy to artificially generate data with such transformations
  - could use such data as additional training data
  - neural network will learn to be invariant to such transformations

Topics: generating additional examples



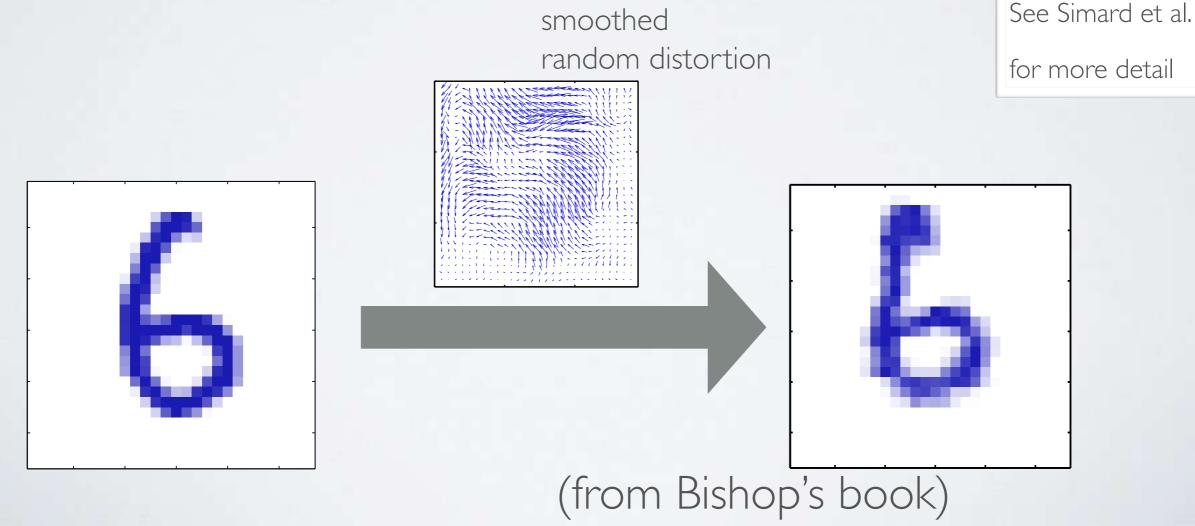
Topics: generating additional examples, distortion field

- · Can add "elastic" deformations (useful in character recognition)
- · We do this by applying a "distortion field" to the image
  - ▶ a distortion field specifies where to displace each pixel value



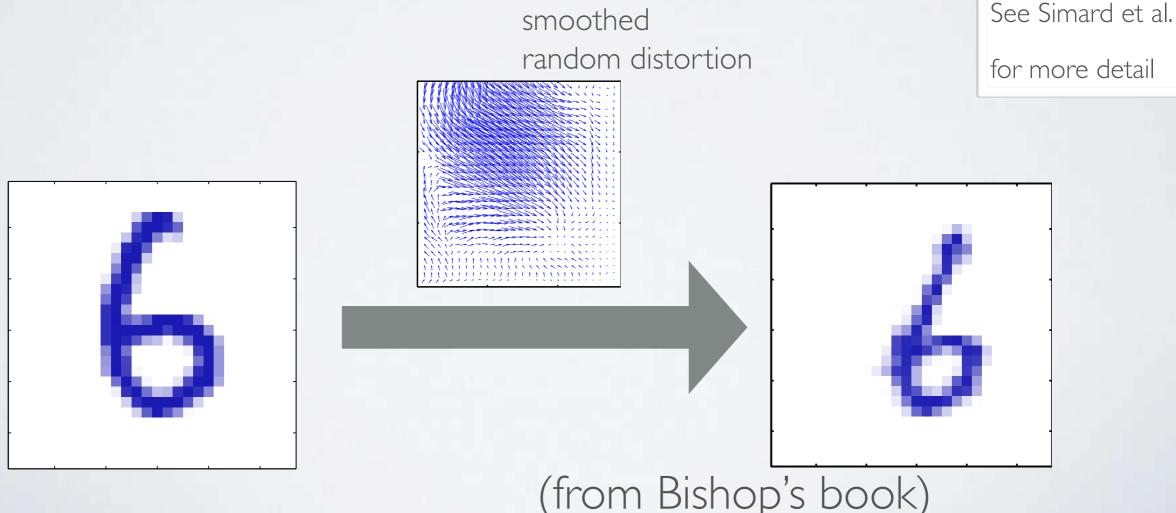
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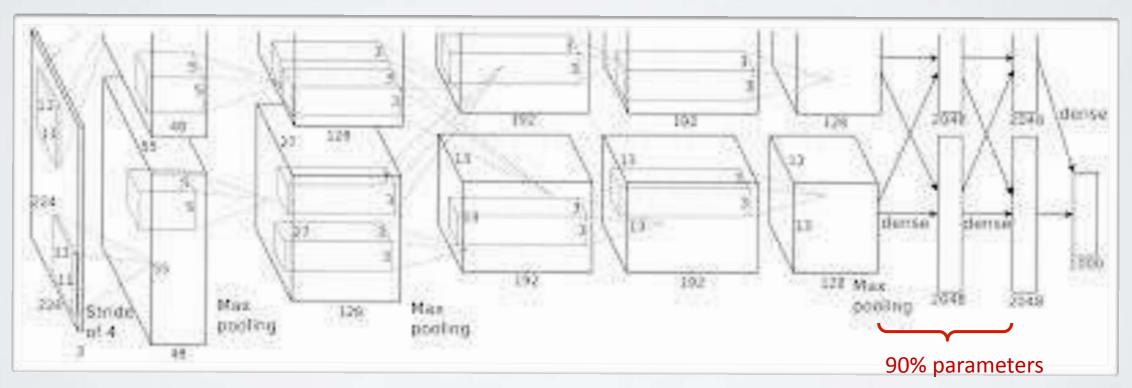
## CONVOLUTIONAL NETWORK

#### Topics: convolutional network

- The network is trained by stochastic gradient descent
  - backpropagation is used similarly as in a fully connected network
    - → need to pass gradients through the convolution operation and the pooling operation.
- Rectified linear activation functions and variants such as maxout (Goodfellow et al., 2013) are popular choices.
  - promote deeper models by allowing gradients to flow better.
- Network-in-network (Lin et al.; ICLR2014):
  - instead of convolving with a generalized linear unit (linear filter + nonlinear activation function), convolve a small network that includes internal hidden units.
  - Used in GoogLenet, the current state-of-the-art in the ImageNet challenge.

### CONVNET IN ACTION

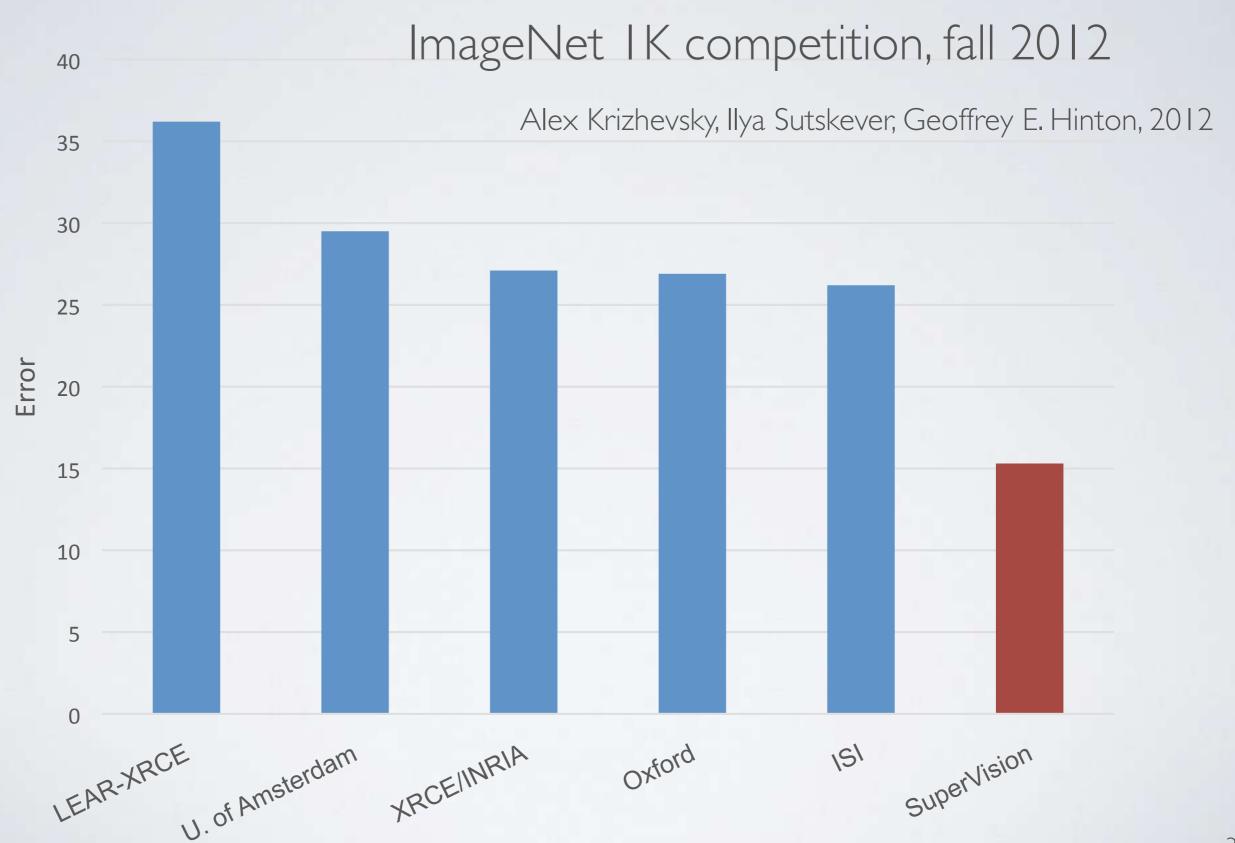
- SuperVision (a.k.a. AlexNet) CNN by the numbers
  - Trained on 1.2 million images, roughly 1K images for each of the 1K classes.
  - Trained with stochastic gradient descent on two NVIDIA GPUs for about a week
- ▶ 650,000 neurons, 60,000,000 parameters, 630,000,000 connections



Input image

Output class prediction

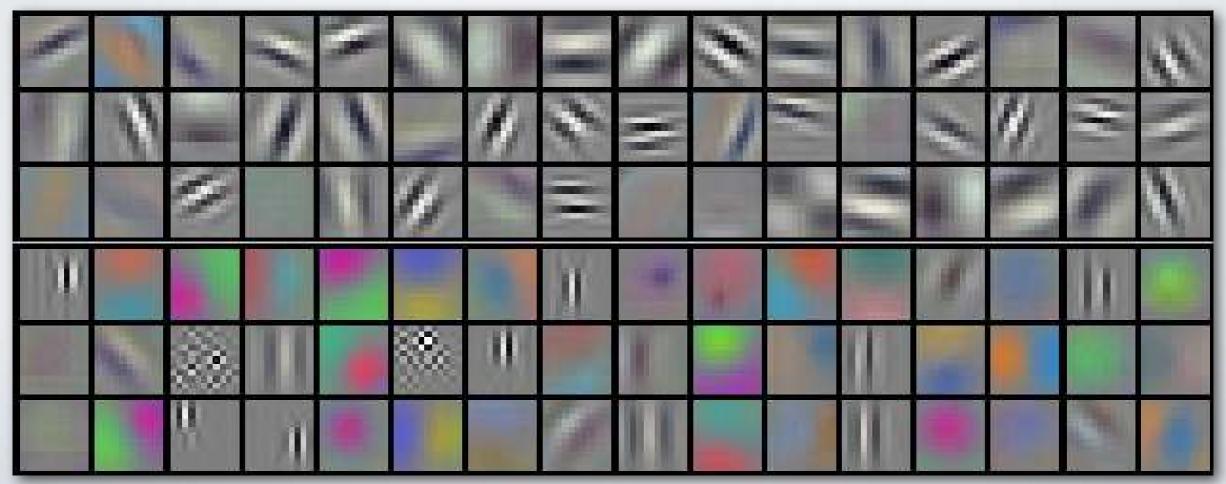
## CONVNET IN ACTION



## CONVNET IN ACTION

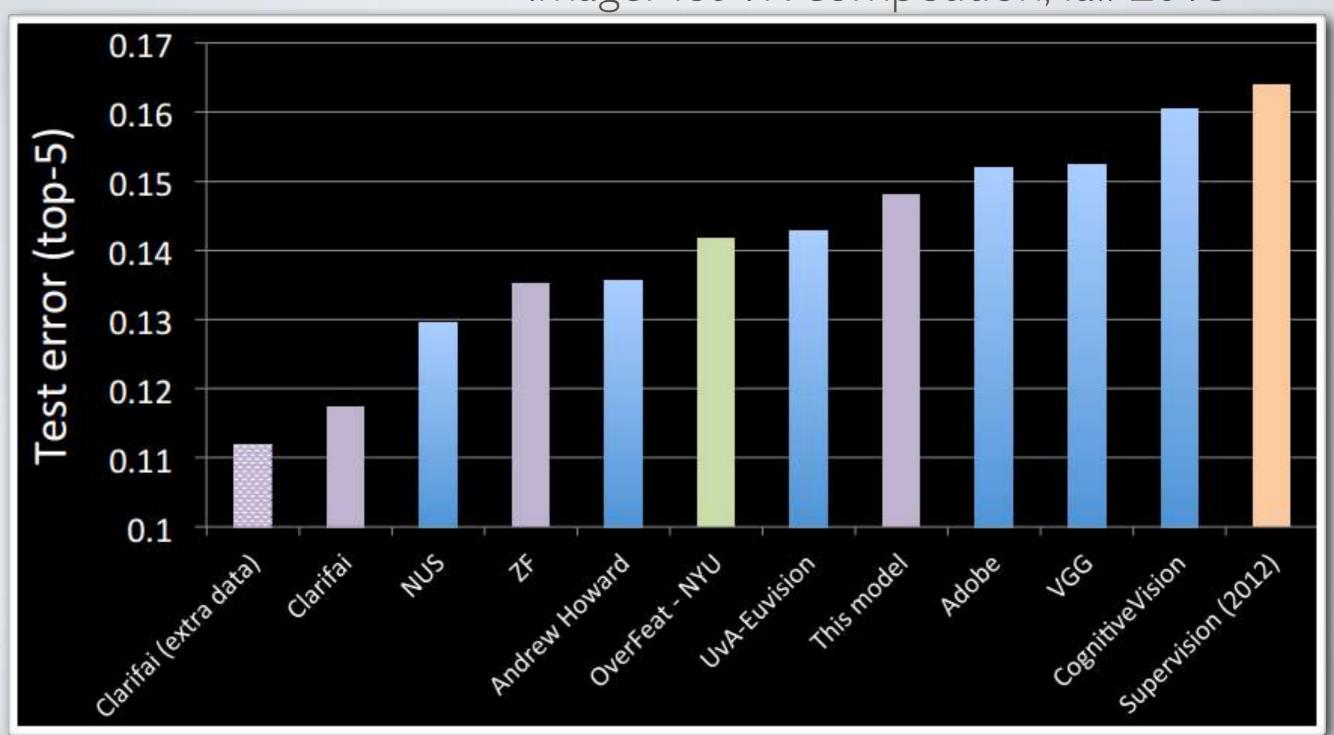
- Training paradigm:
  - Rectified linear activation functions.
  - Trained with **Dropout**.
  - Dataset expansion (data augmentation) employed.

96 low-level learned features:



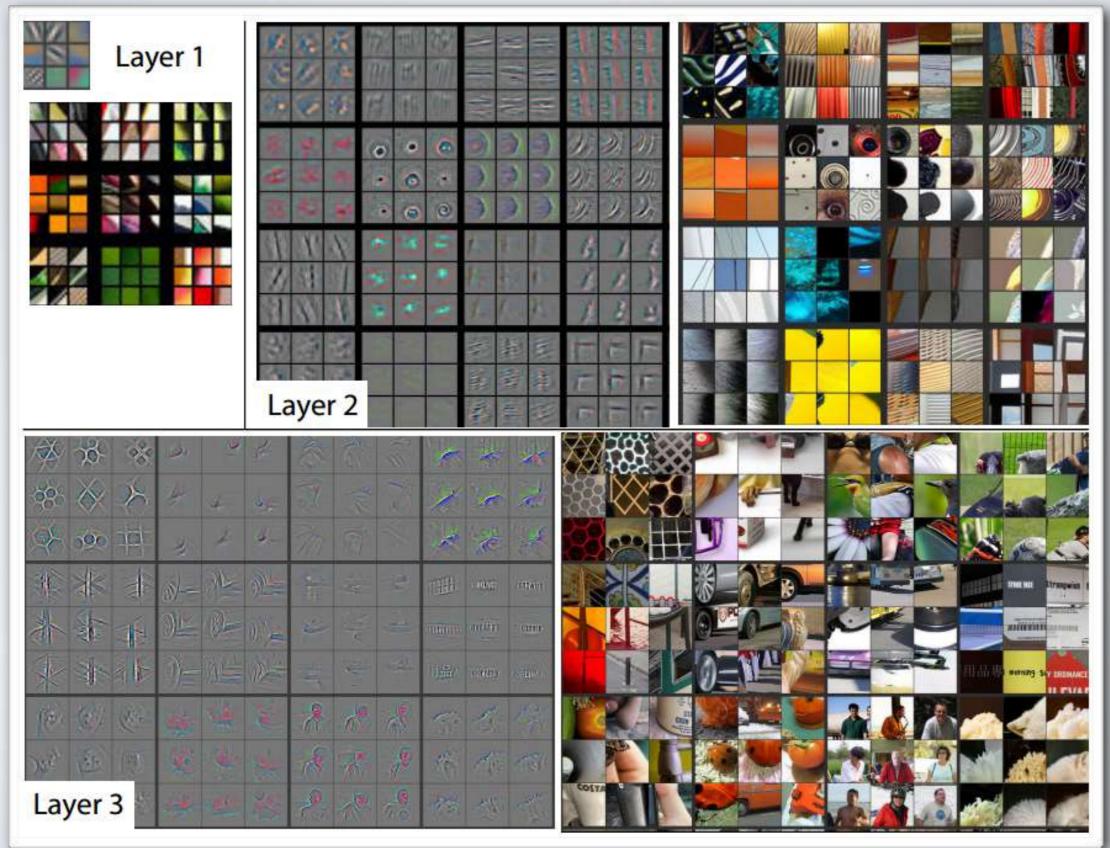
### ONE YEAR LATER

ImageNet IK competition, fall 2013



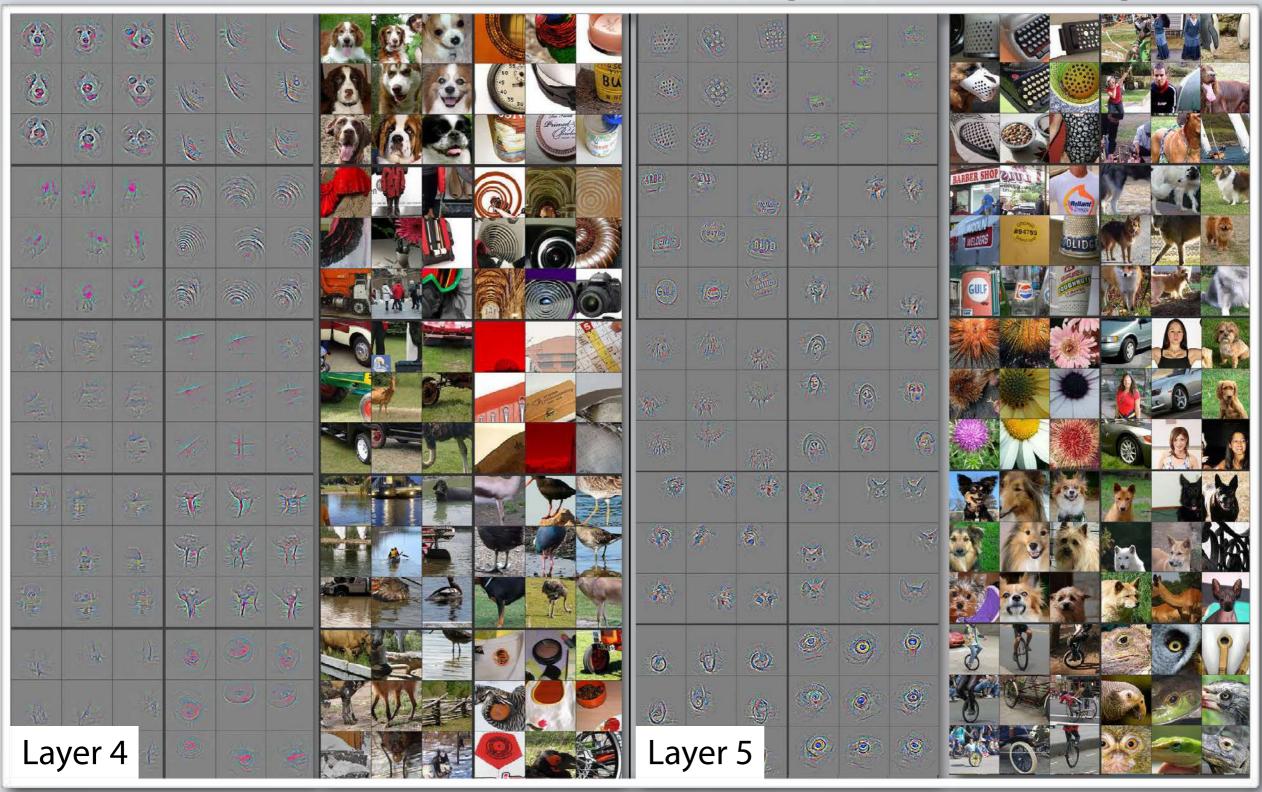
### UNDERSTANDING CNNS

Image from Zeiler and Fergus, 2013



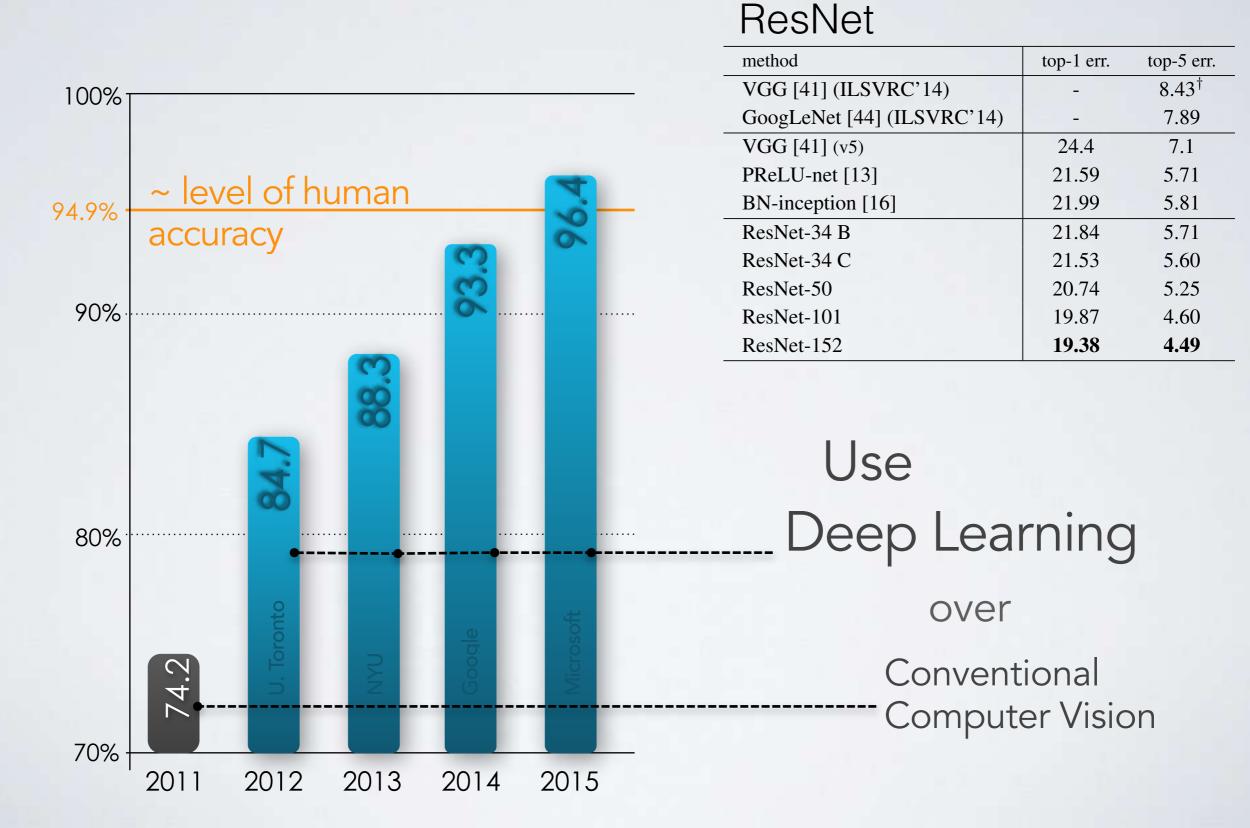
### UNDERSTANDING CNNS

Image from Zeiler and Fergus, 2013



#### IMAGENET ACCURACY STILL IMPROVING

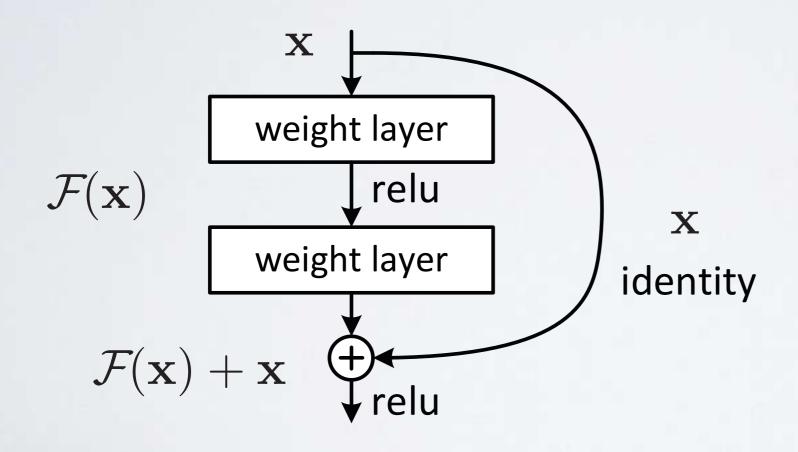
TOP-5 CLASSIFICATION TASK

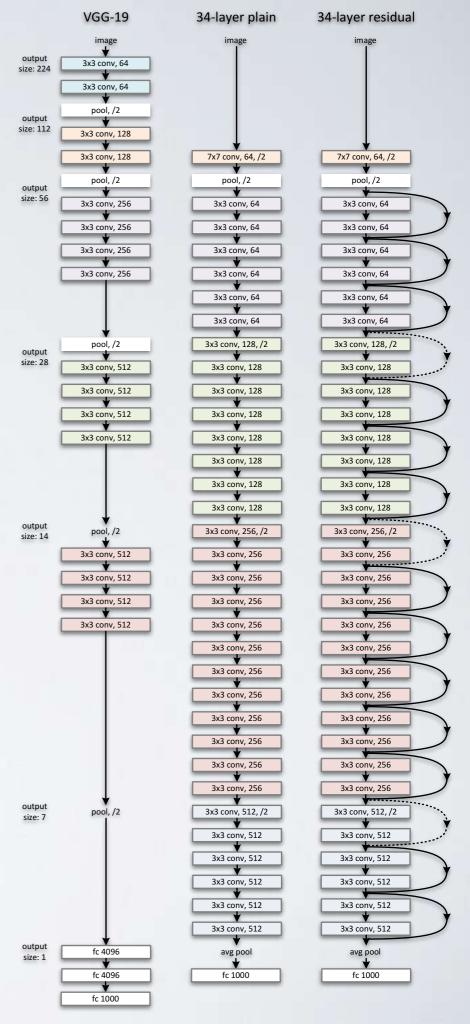


### RESNETS

(HE, ZHANG, REN AND SUN, 2015)

- Lastest state-of-the-art for ImageNet object recognition challenge.
- Uses "shortcut" connections that bypass the nonlinearity

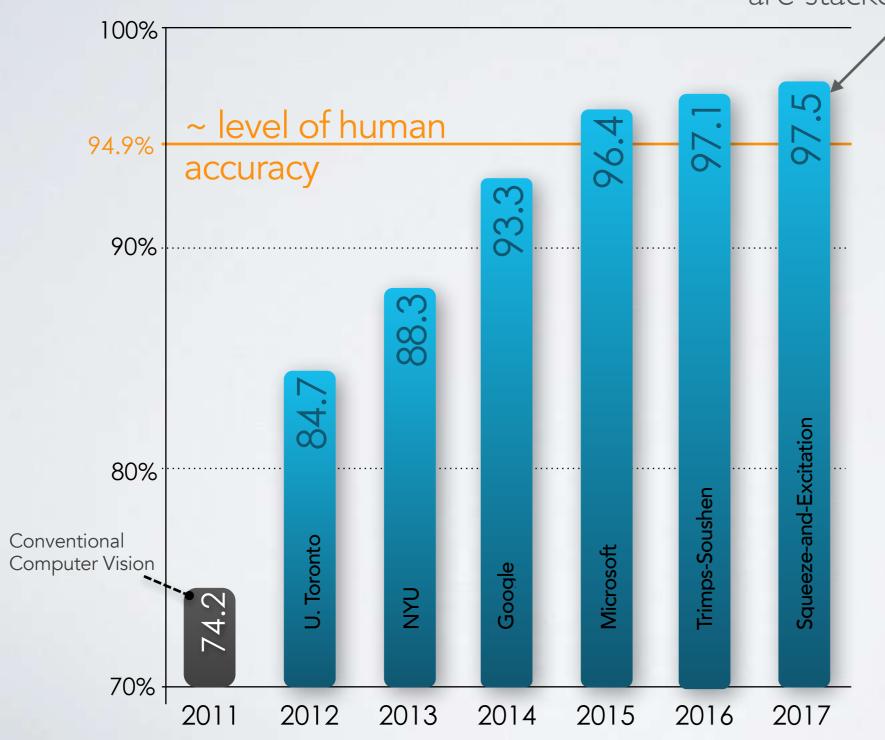




#### IMAGENET ACCURACY STILL IMPROVING

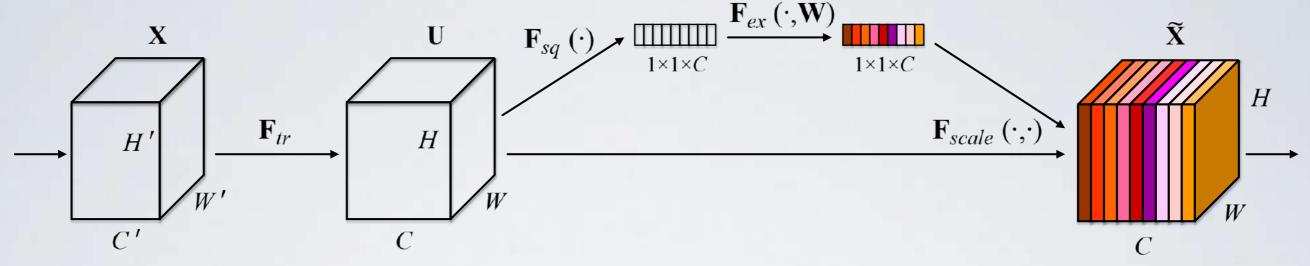
TOP-5 CLASSIFICATION TASK

Squeeze-and-Excitation (SE) blocks are stacked to form the **SENet** 



## SQUEEZE-AND-EXCITATION

(HU, SHEN AND SUN, 2017)



$$\mathbf{u}_c = \mathbf{v}_c * \mathbf{X} = \sum_{s=1}^{C'} \mathbf{v}_c^s * \mathbf{x}^s$$

$$z_c = \mathbf{F}_{sq}(\mathbf{u}_c) = \frac{1}{W \times H} \sum_{i=1}^{W} \sum_{j=1}^{H} u_c(i,j)$$

$$\mathbf{s} = \mathbf{F}_{ex}(\mathbf{z}, \mathbf{W}) = \sigma(g(\mathbf{z}, \mathbf{W})) = \sigma(\mathbf{W}_2 \delta(\mathbf{W}_1 \mathbf{z}))$$

$$\widetilde{\mathbf{x}}_c = \mathbf{F}_{scale}(\mathbf{u}_c, s_c) = s_c \cdot \mathbf{u}_c$$

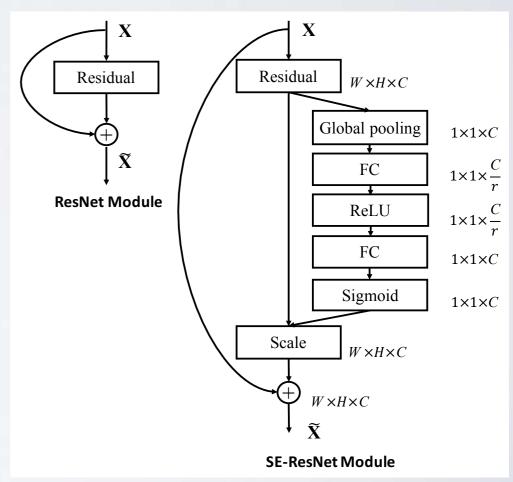


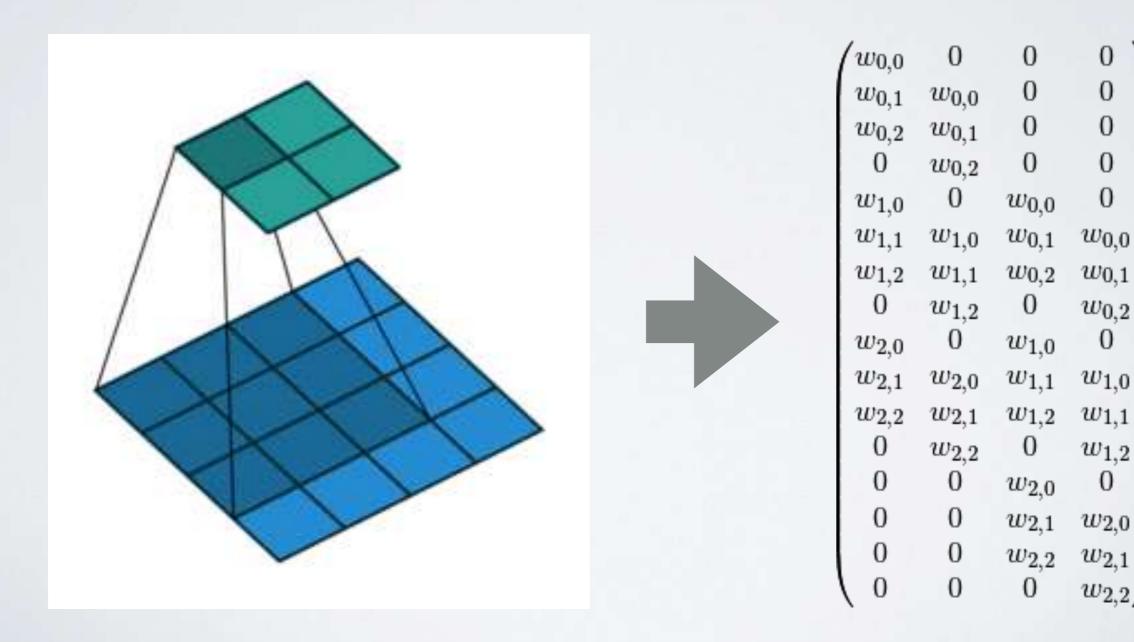
Figure 3. The schema of the original Residual module (left) and the SE-ResNet module (right).

# Convolutions in more detail

material for this part of the lecture is taken mainly from the theano tutorial: <a href="http://deeplearning.net/software/theano\_versions/dev/tutorial/conv\_arithmetic.html">http://deeplearning.net/software/theano\_versions/dev/tutorial/conv\_arithmetic.html</a>

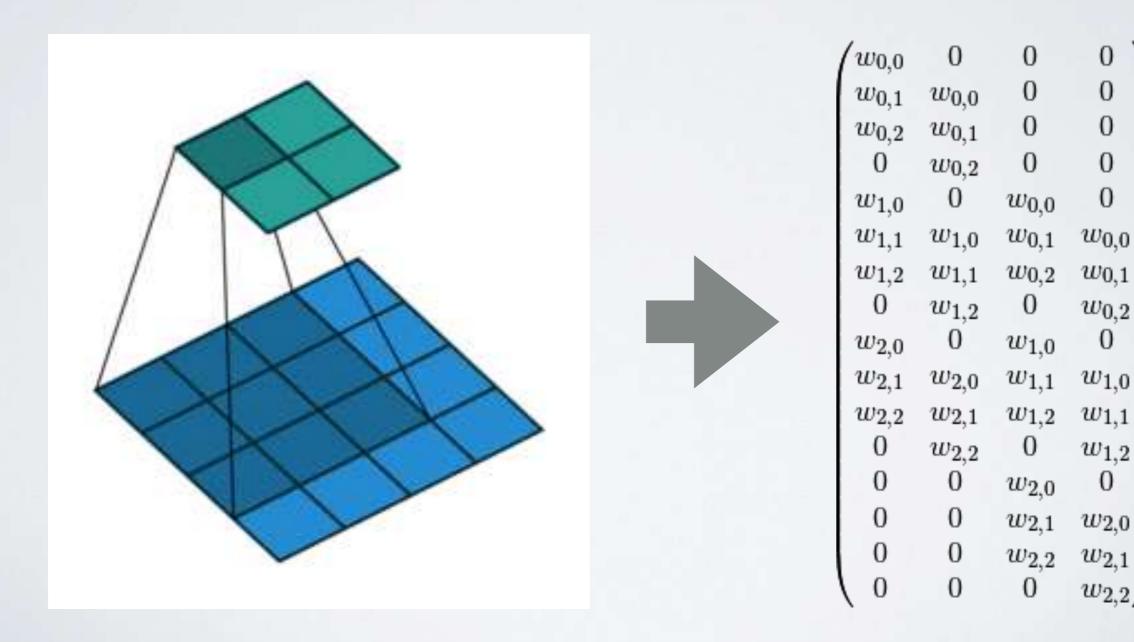
#### CONVOLUTION AS A MATRIX OPERATION

- Convolutions can be represented as a sparse matrix multiply:
  - unrolling the input and output into vectors (from left to right, top to bottom).



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## CNN: DYNAMIC SIZING

- How can we deal with variable sized inputs?
  - Use variable sized pooling regions to a fixed size (post-pooling) feature map.
    - lower feature map sizes will be a function of the input size.
  - Avoid fully-connected layers and use pooling to reduce down to a set of… IxI feature maps.

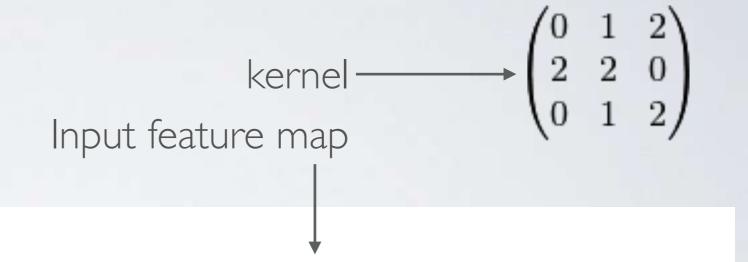


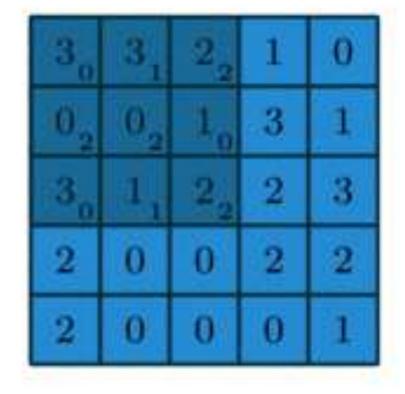
Image from Deep Learning Textbook (Goodfellow et al, 2016)

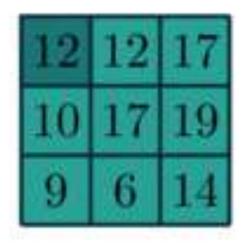
## CONVOLUTION BASICS

#### Properties of images

- Stored as multi-dimensional arrays.
- Feature one or more axes for which ordering matters
  - IMAGE: width and height axes
  - AUDIO: time axis.
- One axis, called the channel axis, is used to access different views of the data
  - IMAGE: red, green and blue channels of color.
  - AUDIO: left and right channels of a stereo track.



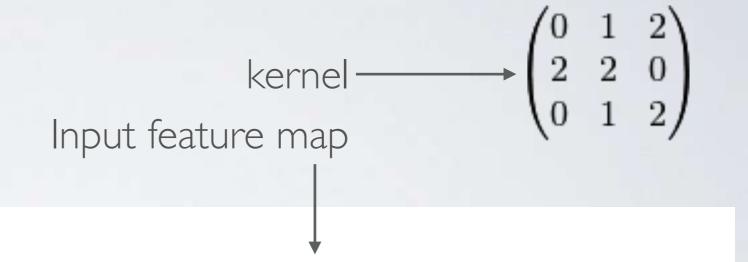


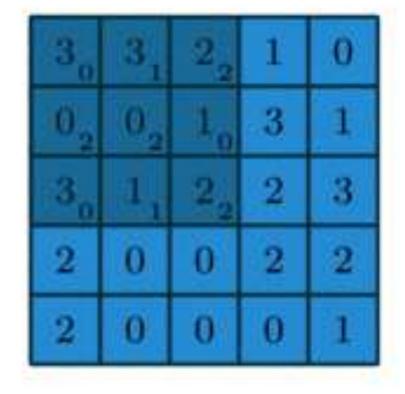


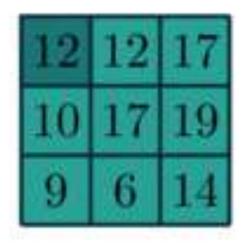
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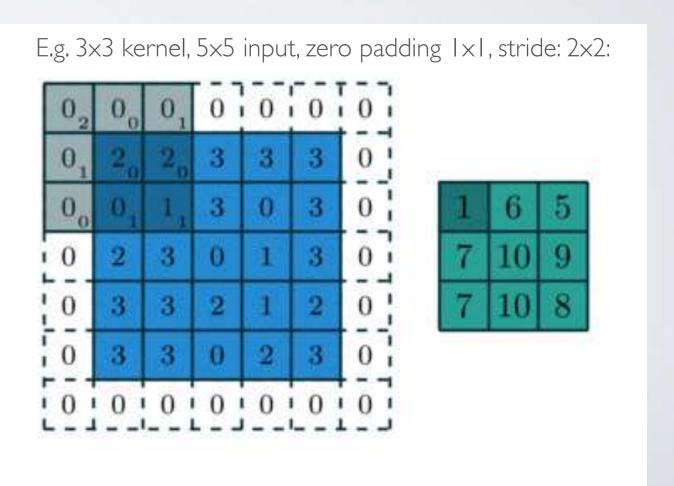






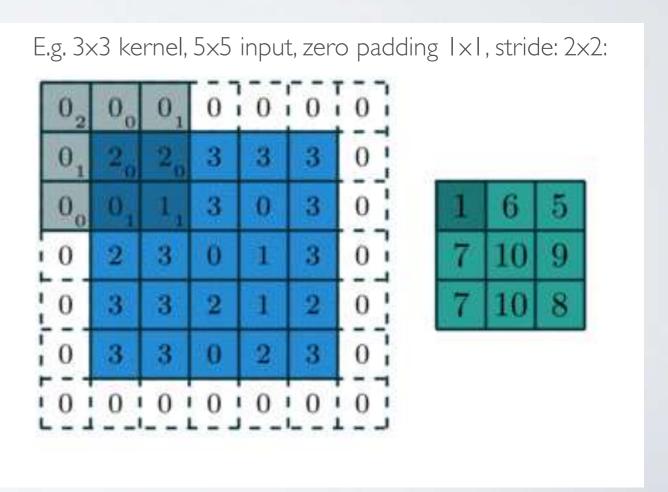
- Properties affecting the output size o<sub>j</sub> along axis j:
  - $ightharpoonup i_j$ : input size along axis j,
  - $\triangleright$   $k_j$ : kernel size along axis j,
  - ▶ sj: stride (distance between two consecutive positions of the kernel) along axis j,
  - $p_j$ : zero padding (number of zeros concatenated at the beginning and at the end of an axis) along axis j.

 $n \equiv \text{number of output feature maps},$   $m \equiv \text{number of input feature maps},$  $k_j \equiv \text{kernel size along axis } j.$ 



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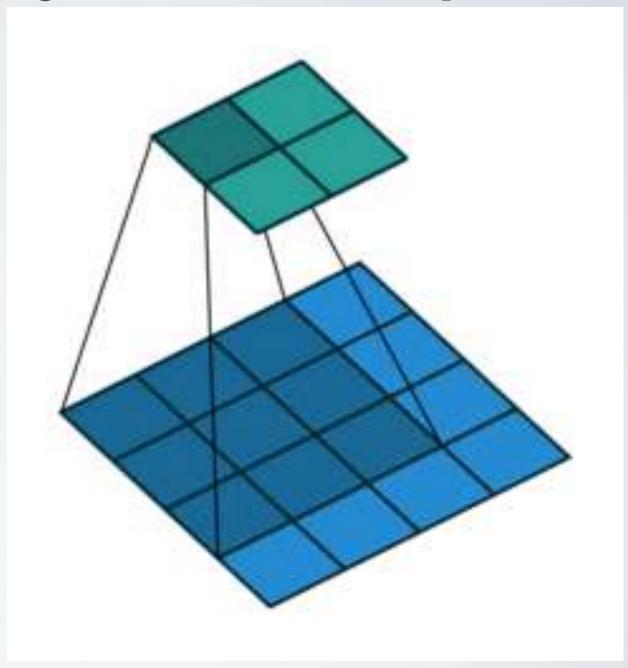
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- Simplifying assumptions:
  - ▶ 2-D discrete convolutions (N = 2),
  - square inputs  $(i_1 = i_2 = i)$ ,
  - square kernel size  $(k_1 = k_2 = k)$ ,
  - ightharpoonup same strides along axes  $(s_1 = s_2 = s)$
  - same zero padding along both axes  $(p_1 = p_2 = p)$ .
- Can comput the output dimension as a function of these quantities:

$$o = \left\lfloor \frac{i + 2p - k}{s} \right\rfloor + 1.$$
 floor function

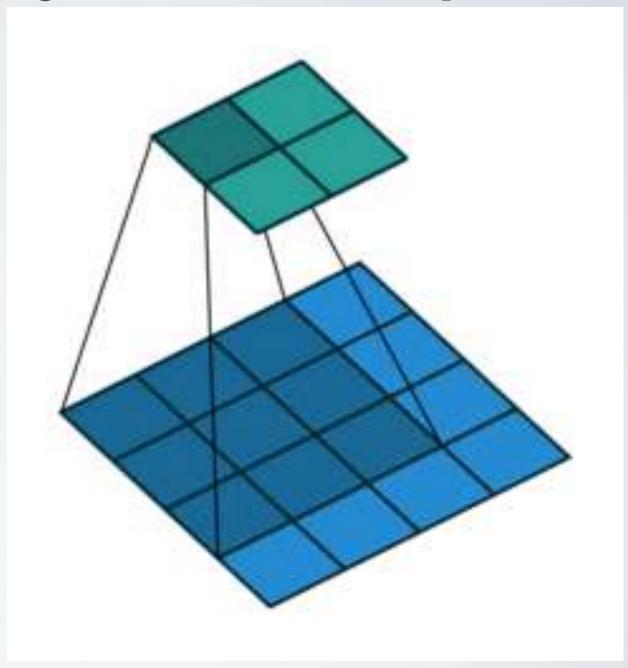
E.g. i = 4 and k = 3, s = 1 and p = 0.

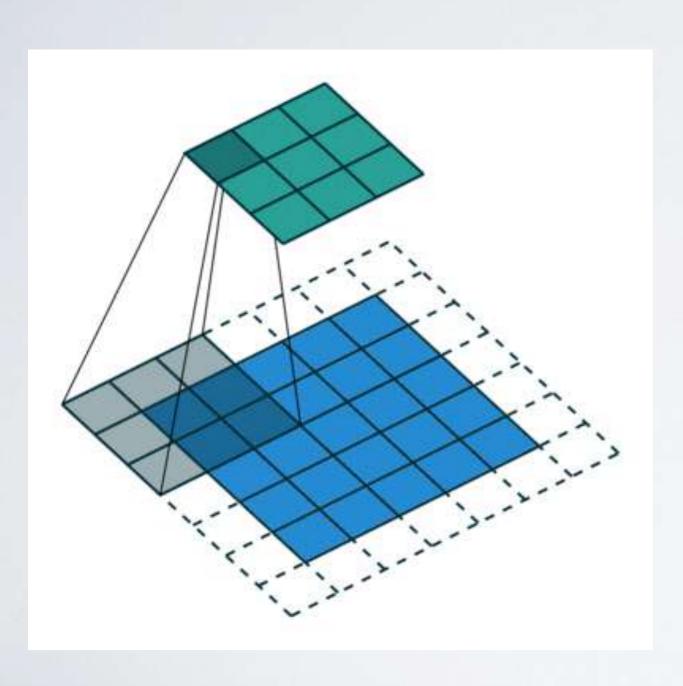


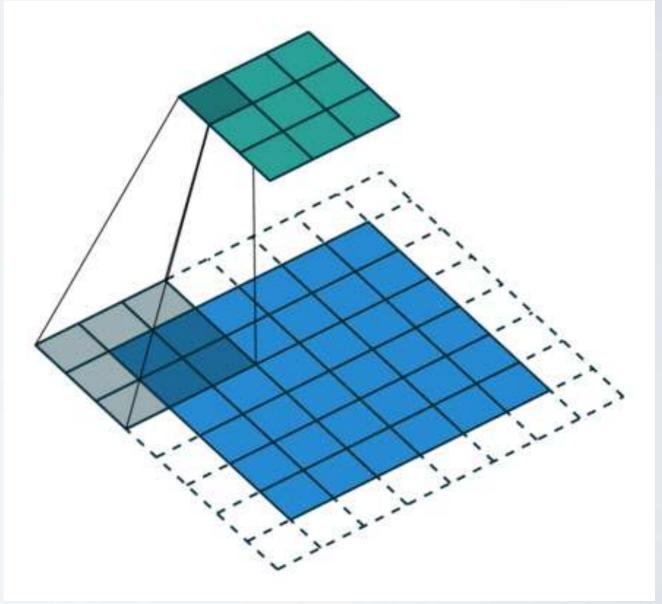
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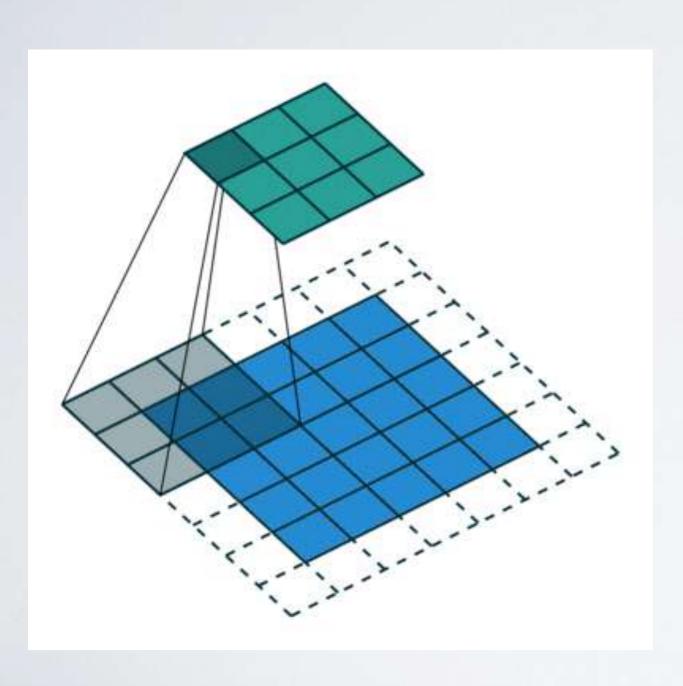
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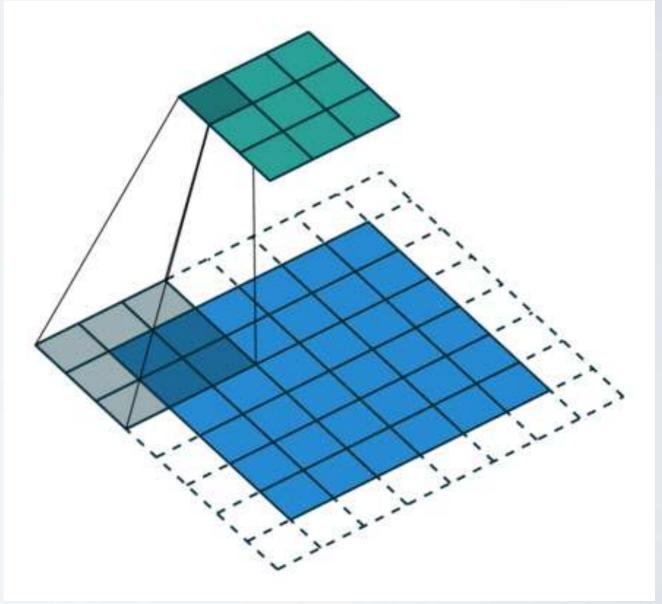
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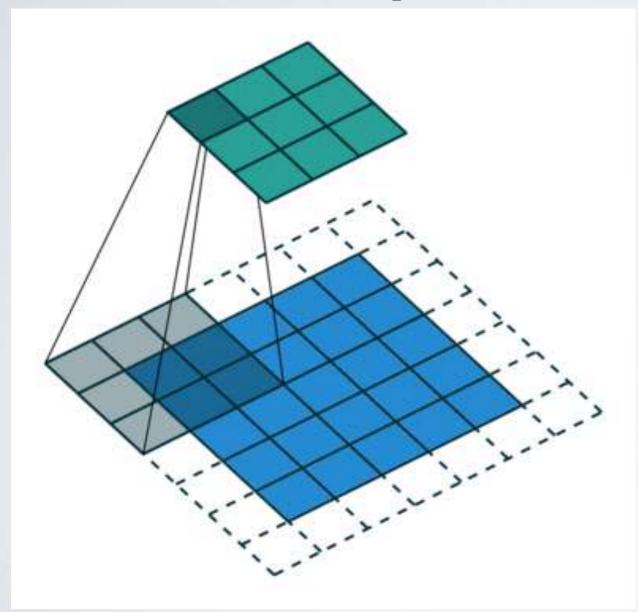


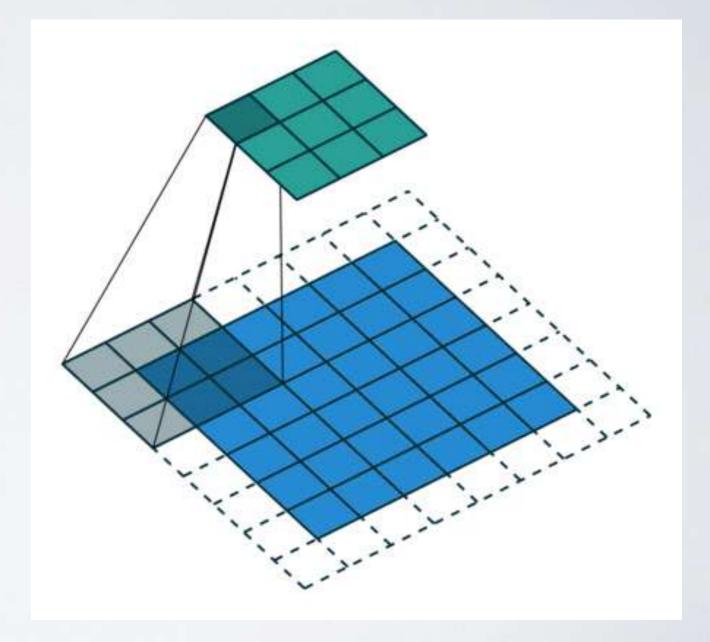




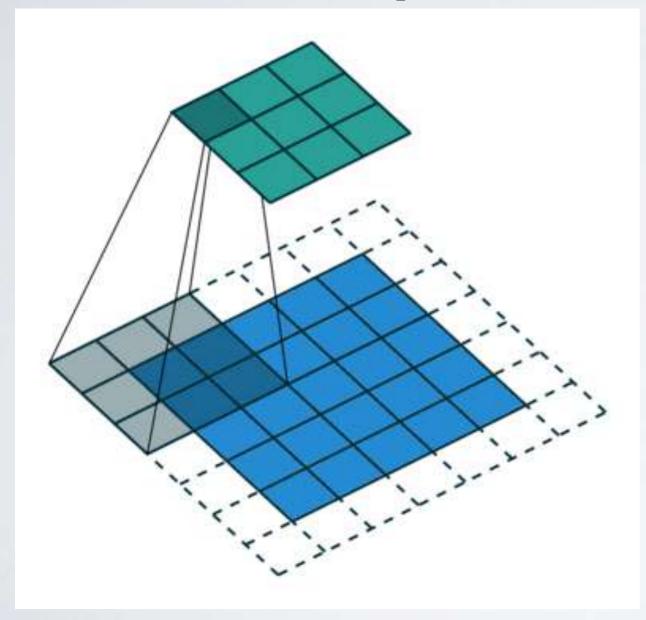


i = 5 and k = 3, s = 2 and p = 1.

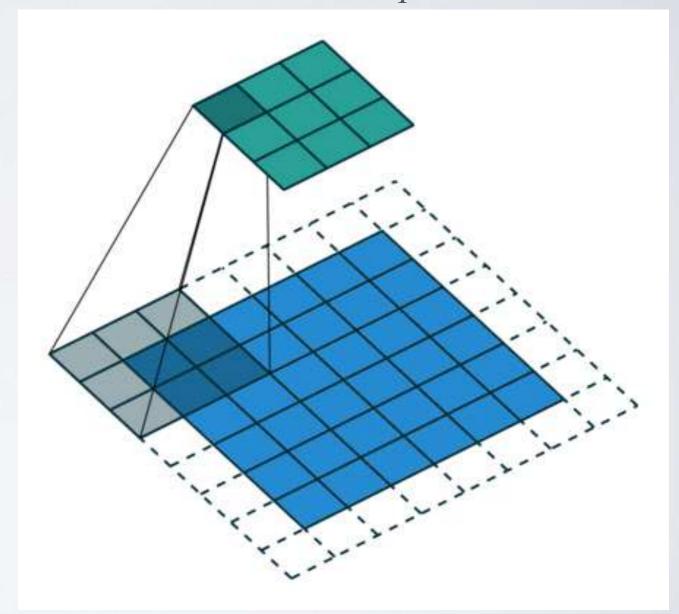


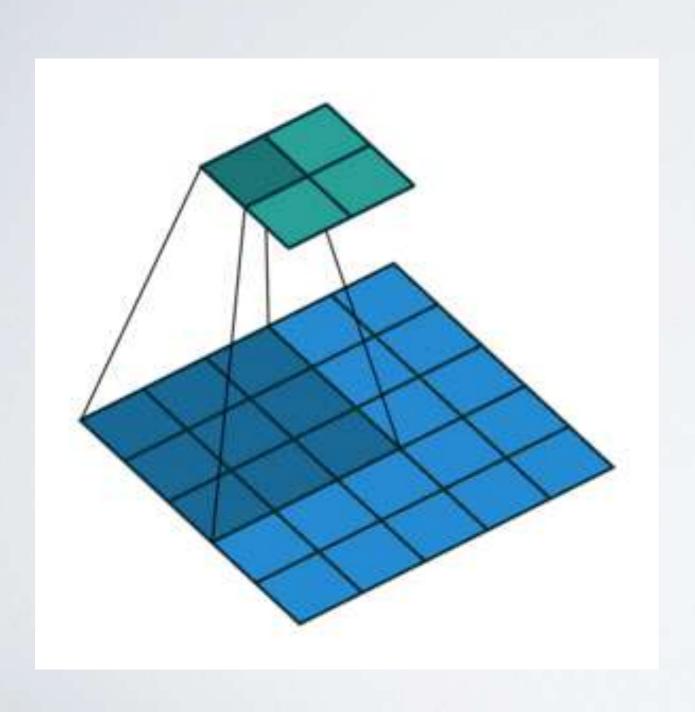


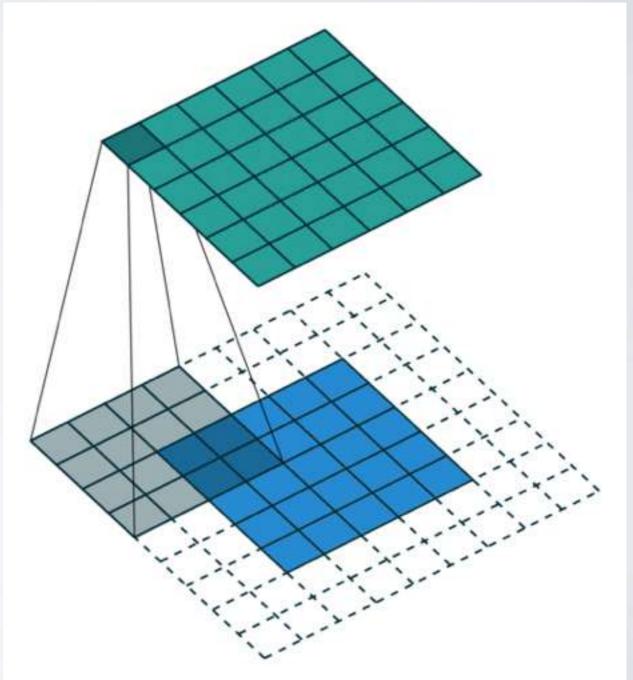
$$i = 5$$
 and  $k = 3$ ,  $s = 2$  and  $p = 1$ .

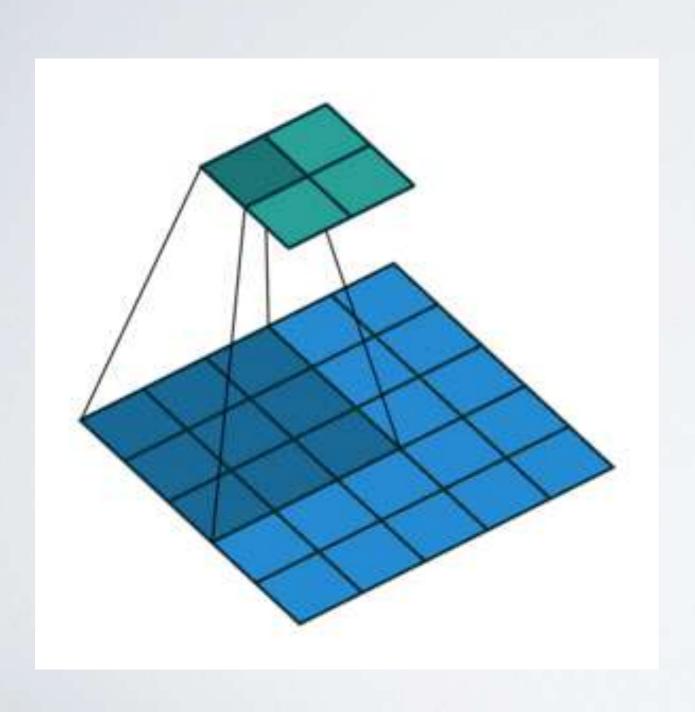


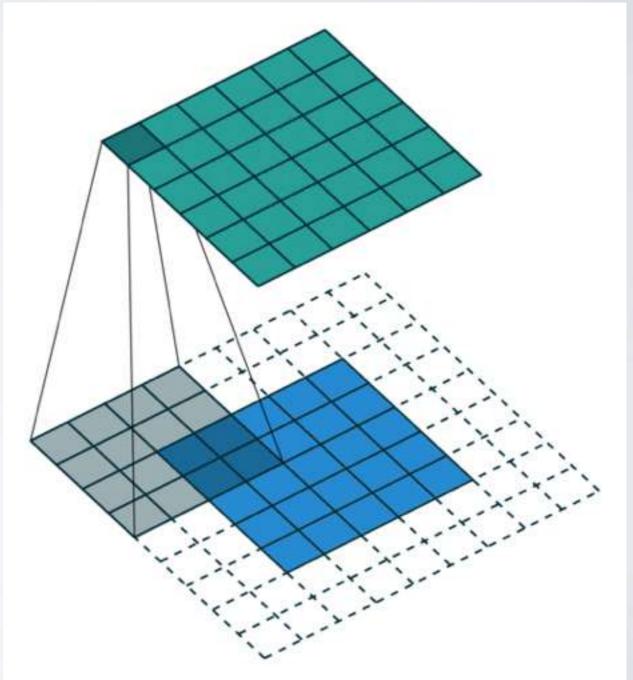
$$i = 6$$
 and  $k = 3$ ,  $s = 2$  and  $p = 1$ .



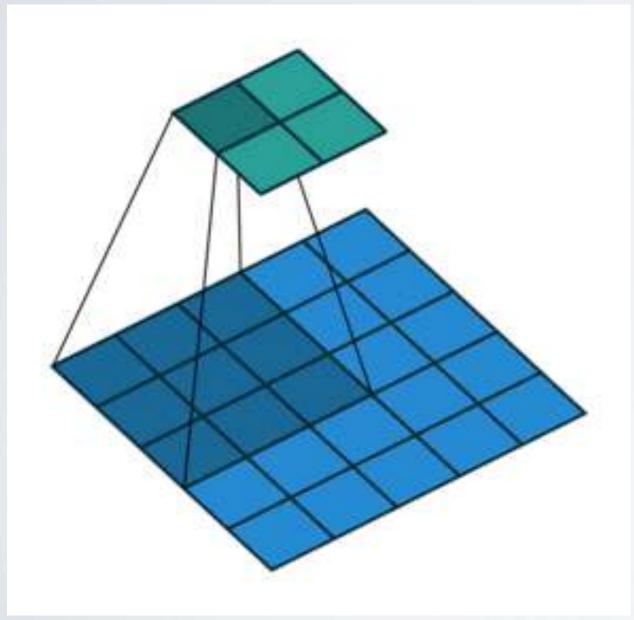


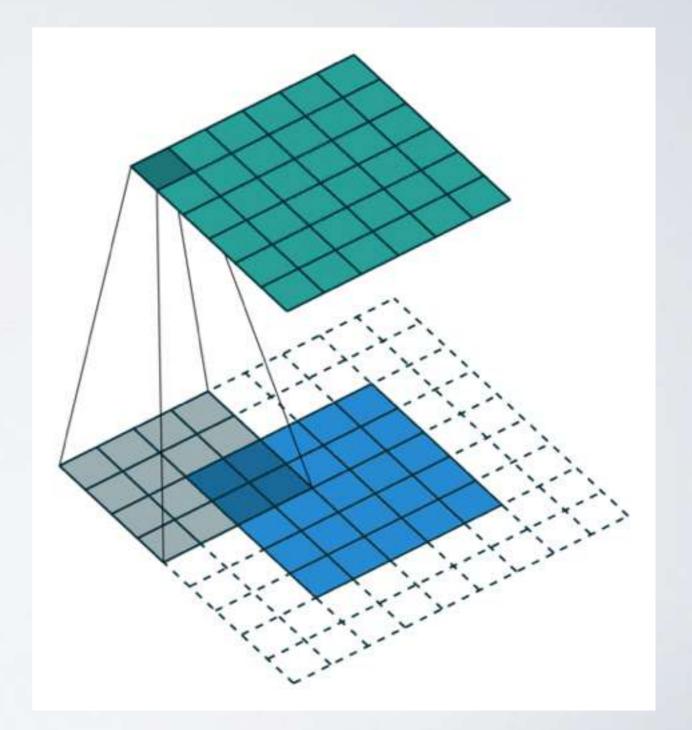




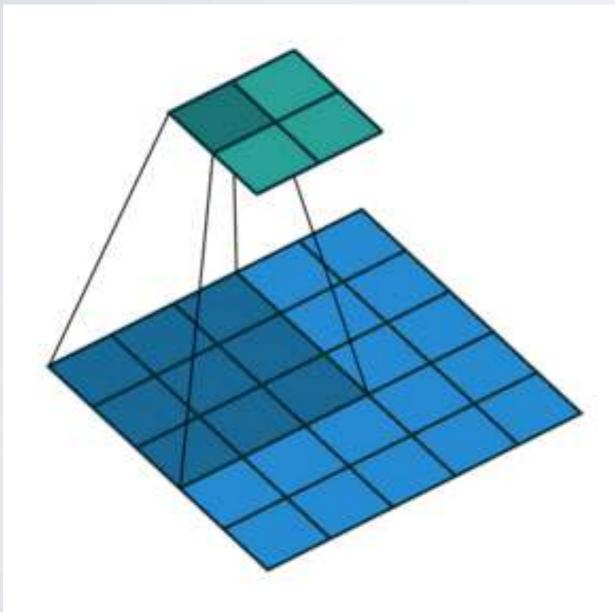


$$i = 5$$
 and  $k = 3$ ,  $s = 2$  and  $p = 0$ .

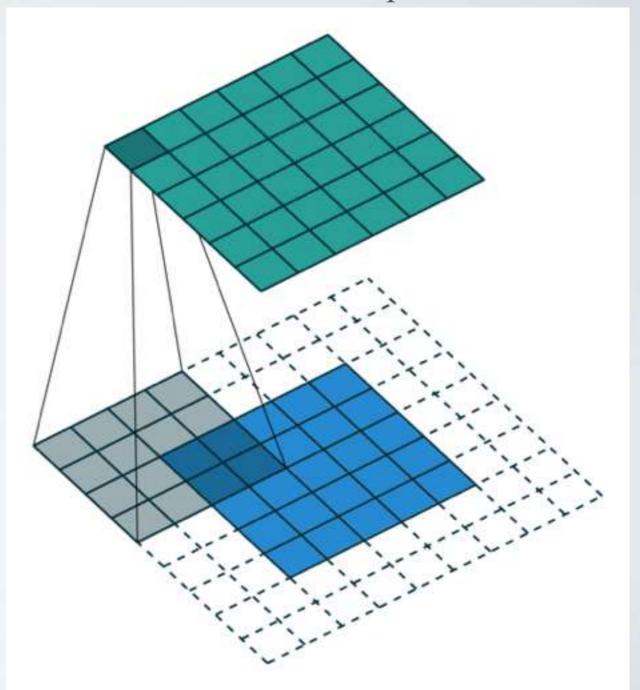




$$i = 5$$
 and  $k = 3$ ,  $s = 2$  and  $p = 0$ .



i = 5 and k = 4, s = 1 and p = 2.

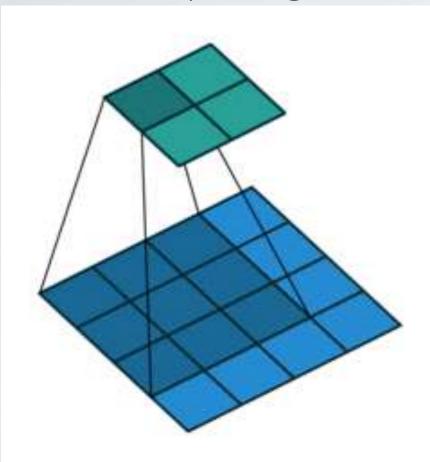


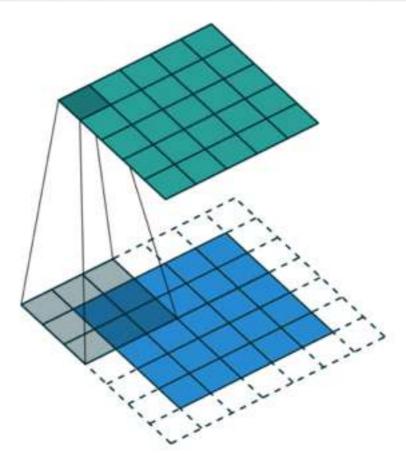
## PADDING: SPECIAL CASES

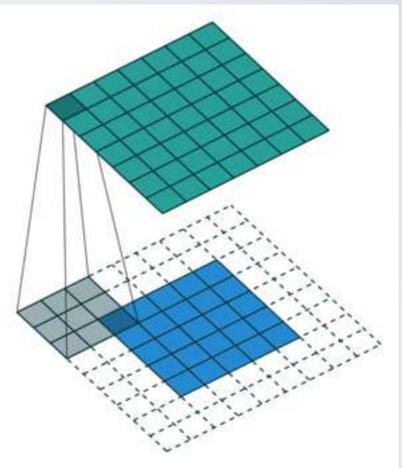
valid convolution no padding

same convolution half (or same) padding

full convolution full padding









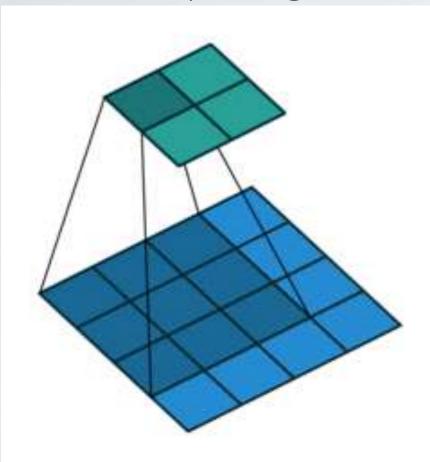
output dimension = input dimension

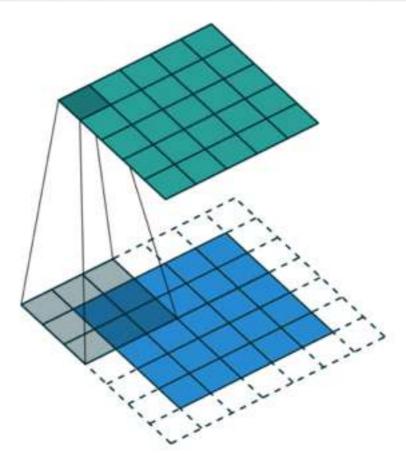
## PADDING: SPECIAL CASES

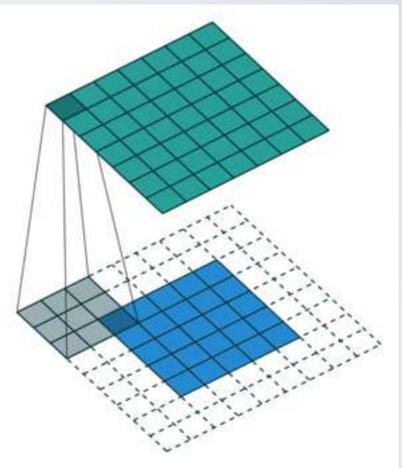
valid convolution no padding

same convolution half (or same) padding

full convolution full padding









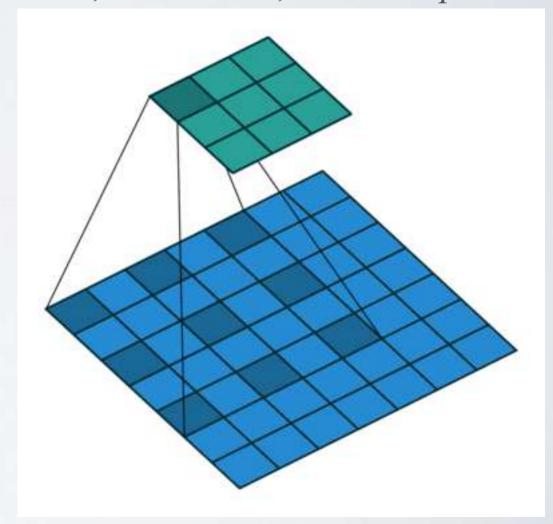
output dimension = input dimension

## DILATED CONVOLUTIONS

- Dilated convolutions "inflate" the kernel, inserting spaces between the kernel elements.
  - Dilation "rate" is controlled by an additional hyperparameter d.
  - Usually d 1 spaces inserted between kernel elements such that d = 1 corresponds to a regular convolution.
  - $\blacktriangleright$  A kernel of size k dilated by a factor d has an effective size:

$$\hat{k} = k + (k-1)(d-1).$$

$$i = 7, k = 3, d = 2, s = 1 \text{ and } p = 0.$$

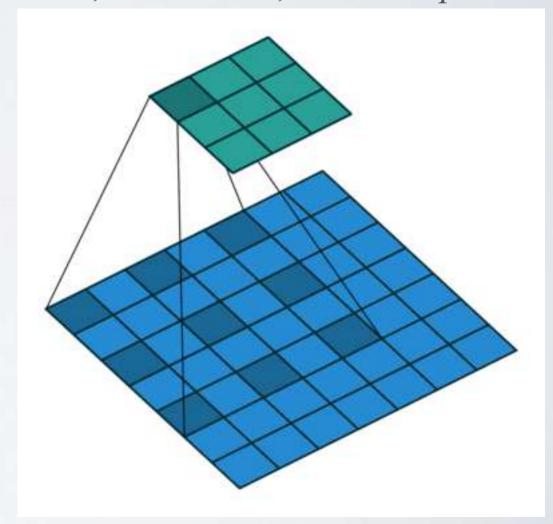


## DILATED CONVOLUTIONS

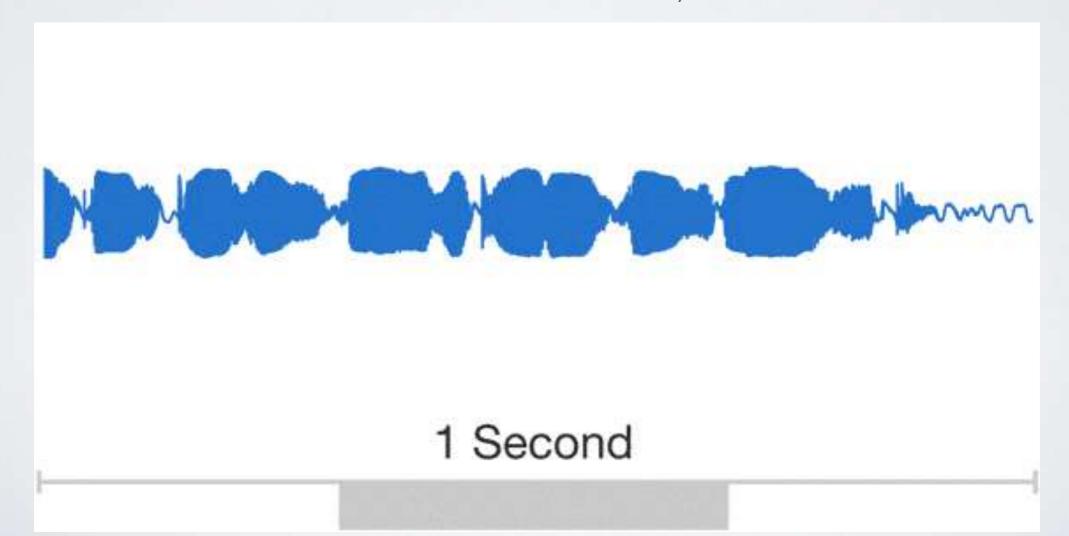
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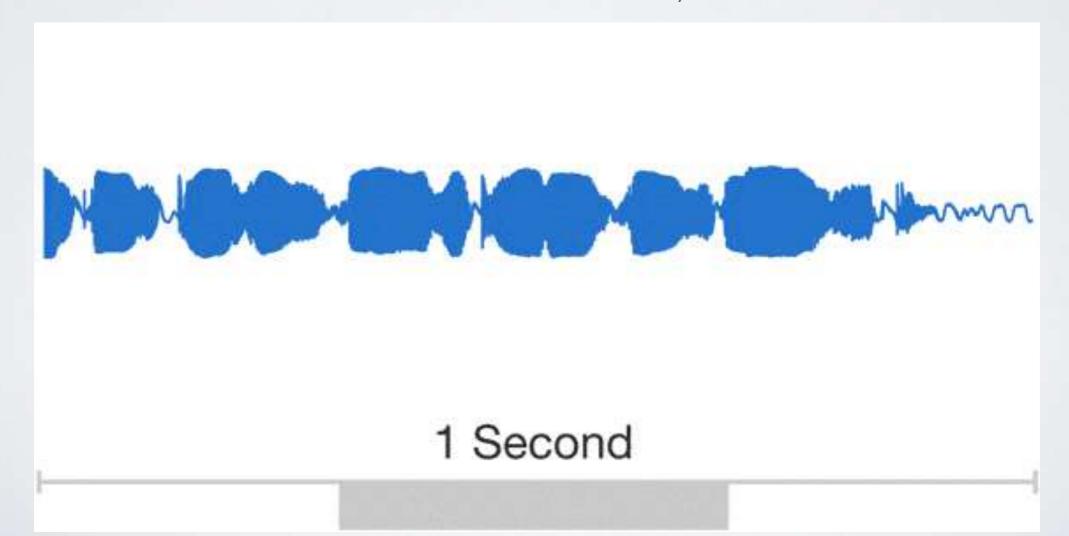
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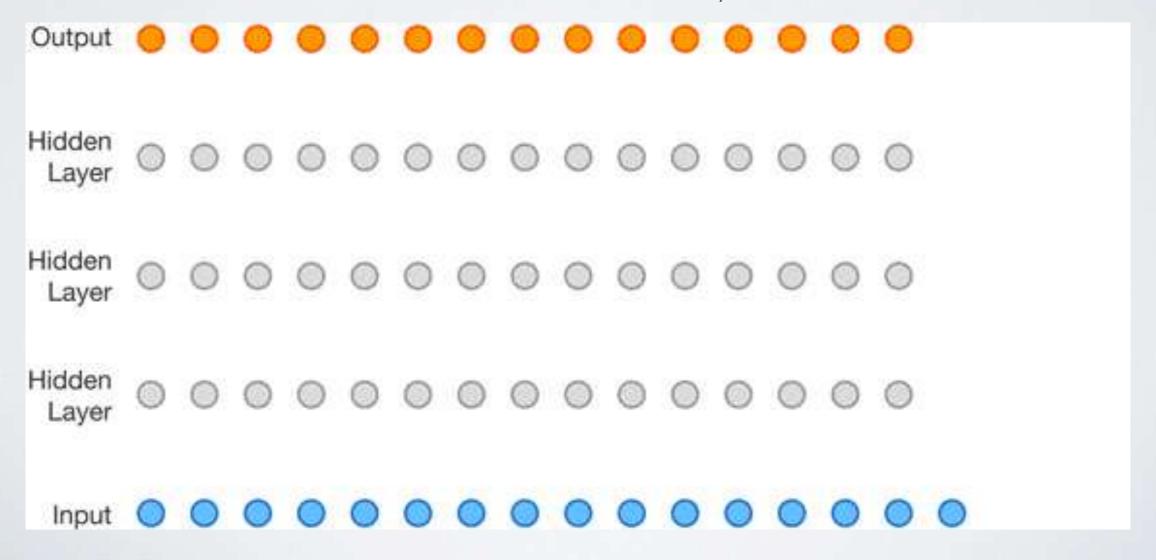
- WaveNet: Dilated CNNs for speech synthesis
  - Modeling audio data is challenging because of the many scales over which information is encoded.
  - ▶ WaveNet uses dilated CNNs in 1-D to efficiently cover the relavent scales.



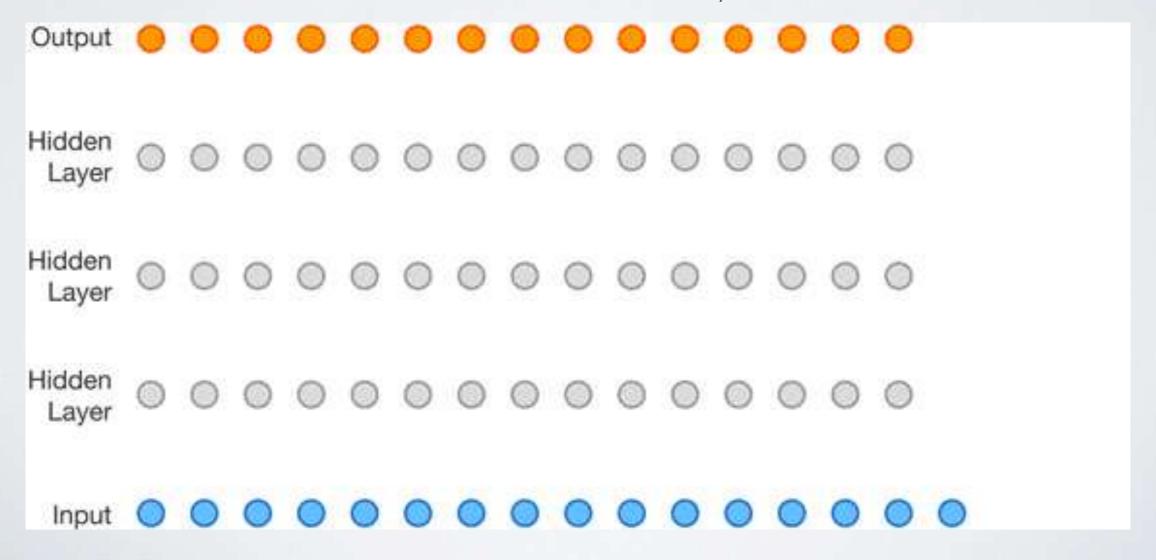
- WaveNet: Dilated CNNs for speech synthesis
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- WaveNet: dilated causal CNNs for speech synthesis
  - Modeling audio data is challenging because of the many scales over which information is encoded.
  - ▶ WaveNet uses dilated CNNs in 1-D to efficiently cover the relavent scales.



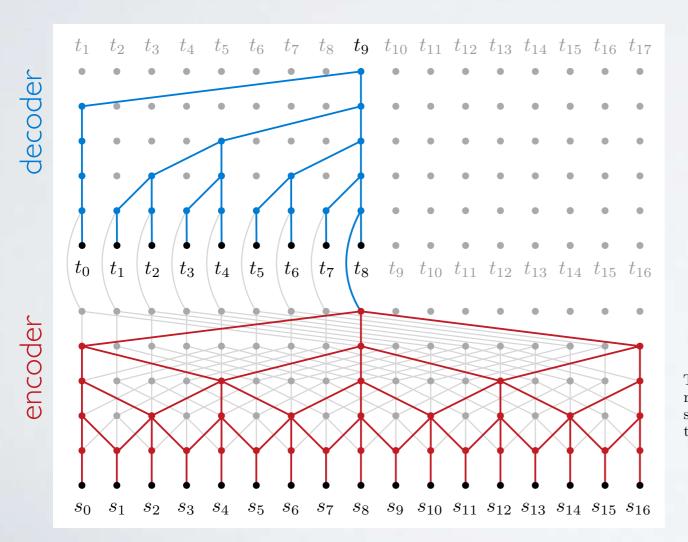
- WaveNet: dilated causal CNNs for speech synthesis
  - Modeling audio data is challenging because of the many scales over which information is encoded.
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### DILATED CONVOLUTIONS: BYTENET

(Kalchbrenner et al., 2016, arXiv: 1610.10099)

- ByteNet: dilated CNN for machine translation.
  - Uses an encoder-decoder structure with a causal convolution in the decoder.
  - State-of-the-art, computationally efficient machine translation



At the same time, around 3000 demonstrators attempted to reach the official residency of Prime Minister Nawaz Sharif.

Gleichzeitig versuchten rund 3000 Demonstranten, zur Residenz von Premierminister Nawaz Sharif zu gelangen.

Gleichzeitig haben etwa 3000 Demonstranten versucht, die offizielle Residenz des Premierministers Nawaz Sharif zu erreichen.

Just try it: Laura, Lena, Lisa, Marie, Bettina, Emma and manager Lisa Neitzel (from left to right) are looking forward to new members.

Einfach ausprobieren: Laura, Lena, Lisa, Marie, Bettina, Emma und Leiterin Lisa Neitzel (von links) freuen sich auf Mitstreiter.

Probieren Sie es aus: Laura, Lena, Lisa, Marie, Bettina, Emma und Manager Lisa Neitzel (von links nach rechts) freuen sich auf neue Mitglieder.

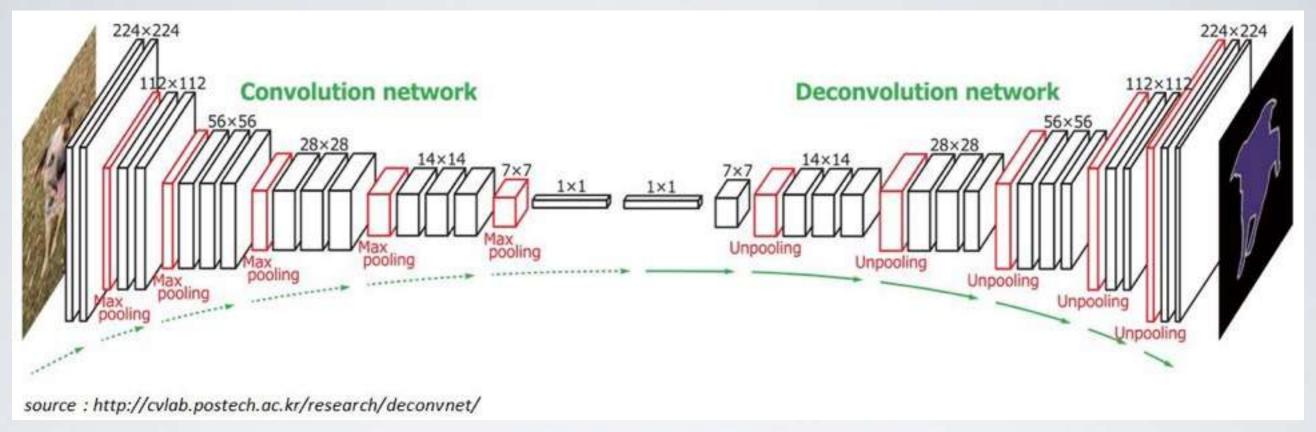
He could have said, "I love you," but it was too soon for that.

Er hätte sagen können "ich liebe dich", aber dafür war es noch zu früh.

Er hätte sagen können: "I love you", aber es war zu früh.

Table 4: Raw output translations generated from the ByteNet that highlight interesting reordering and transliteration phenomena. For each group, the first row is the English source, the second row is the ground truth German target, and the third row is the ByteNet translation.

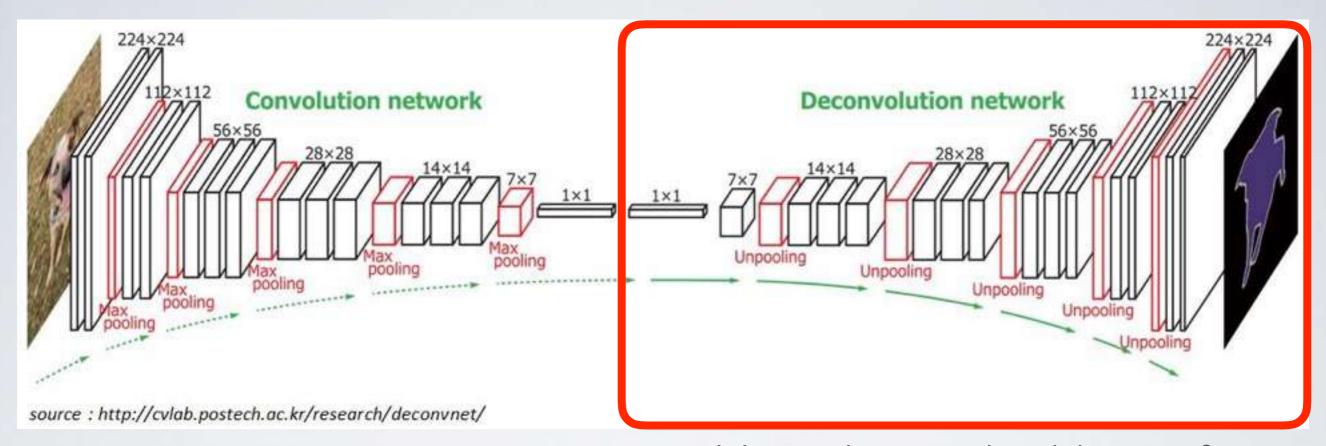
### (DE)CONVOLUTIONS FOR STRUCTURED OUTPUT



semantic segmentation (example taken from https://nrupatunga.github.io/convolution-1/)

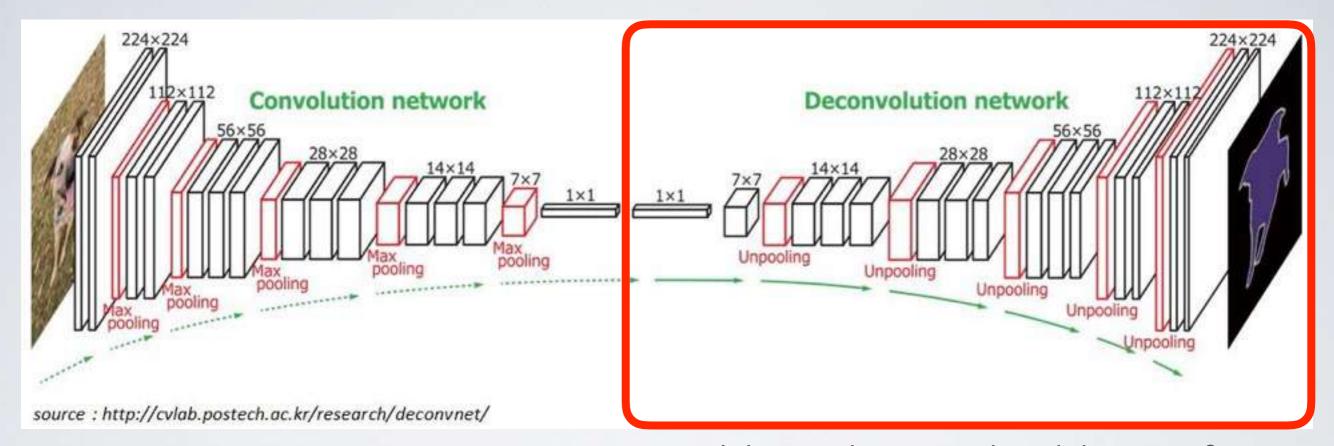
- We can use convolutions to build structure into high-dimensional outputs.
- Useful in applications such as:
  - → semantic segmentation (above)
  - → image generation

### (DE) CONVOLUTIONS FOR STRUCTURED OUTPUT



How do we do this part?

### (DE)CONVOLUTIONS FOR STRUCTURED OUTPUT

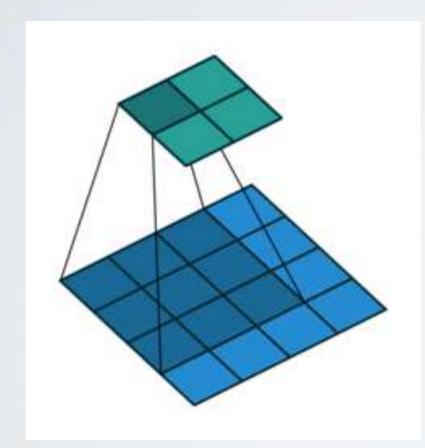


How do we do this part?

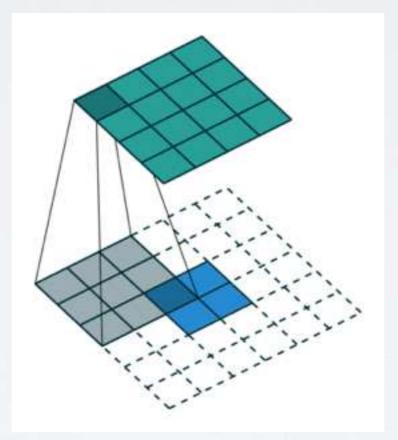
- Option I:Transposed (a.k.a. fractionally strided) convolution.
- Option 2: Upsampling (e.g. nearest-neighbour or bilinear) + convolution.

#### TRANSPOSE CONVOLUTION

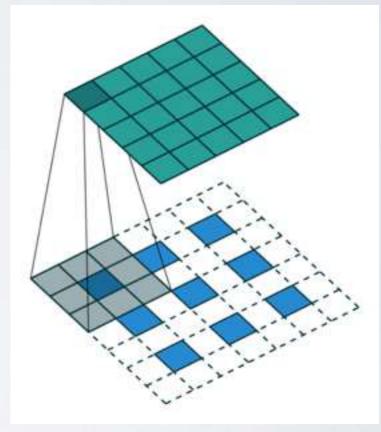
- Transposed convolution is the operation done in the backprop pass through a convolution.
- It's the natural "inverse" of the convolution operation.



Standard Convolution i = 5, k = 3 and s = 2



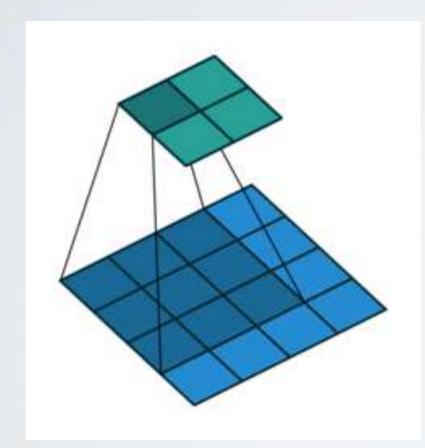
Equivalent to transpose conv. but less efficient (due to zero-padding)



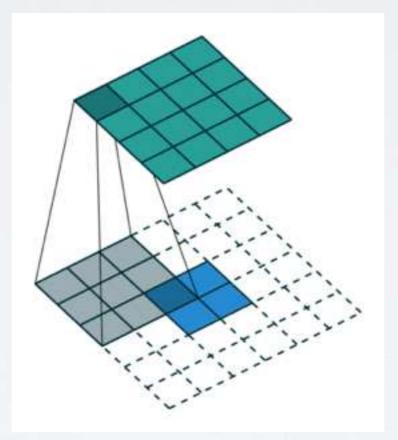
$$i = 5, k = 3, s = 2$$
 and  $p = 1$ 

#### TRANSPOSE CONVOLUTION

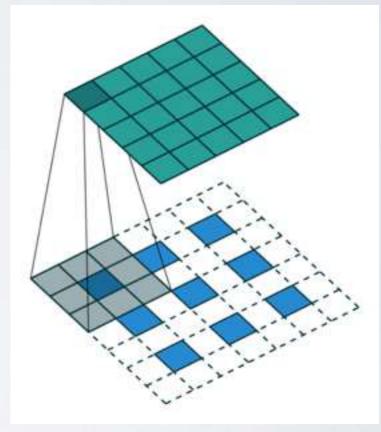
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Equivalent to transpose conv. but less efficient (due to zero-padding)



$$i = 5, k = 3, s = 2$$
 and  $p = 1$ 

#### INTERPOLATION + CONVOLUTION

- But transpose convolution can cause artifacts.
  - see http://distill.pub/2016/deconv-checkerboard
- Currently, interpolation and convolution is the preferred method for generative convolutional models.



Using transpose convolution: Heavy checkerboard artifacts.



Using resize-convolution.

No checkerboard artifacts.