



System Velocity:

A new method for dimension reduction and ecological regime shift detection

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Ecological Regime Shifts

what? a persistent change in the structure or functioning of a system

how? loss of negative feedback(s) maintaining the system

goal? predict in time to prevent

Regime Shifts



Ecosystems are Complex

(and complicated)

- **high dimensional**
- **many (∞ ?) interactions**
- **non-linear**
- **non-ergodic (open)**
- **dynamic**
- **difficult to model mathematically**

(Too Many) Methods for Detecting Regime Shifts

> 70 (!) methods proposed in literature

10 suitable for multivariable data

few explicitly handle **noisy** data

few explicitly handle **irregular sampling**

Regime Shifts Detection Methods

Rising Variance/Critical Slowing Down

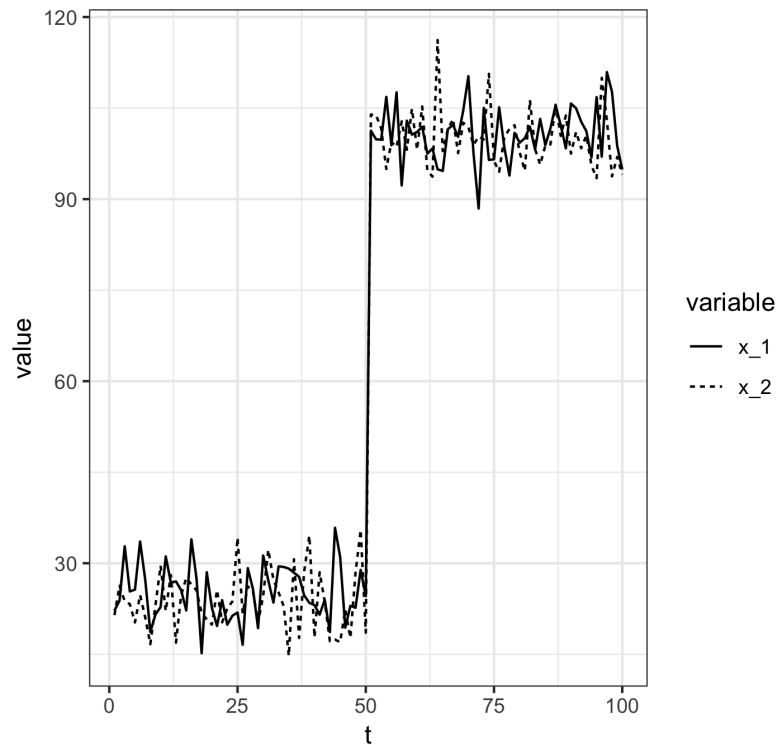
Variance Index (max eigenvalue of covariance matrix)

Principal Coordinates Analysis

Fisher Information

Velocity, v

Toy System

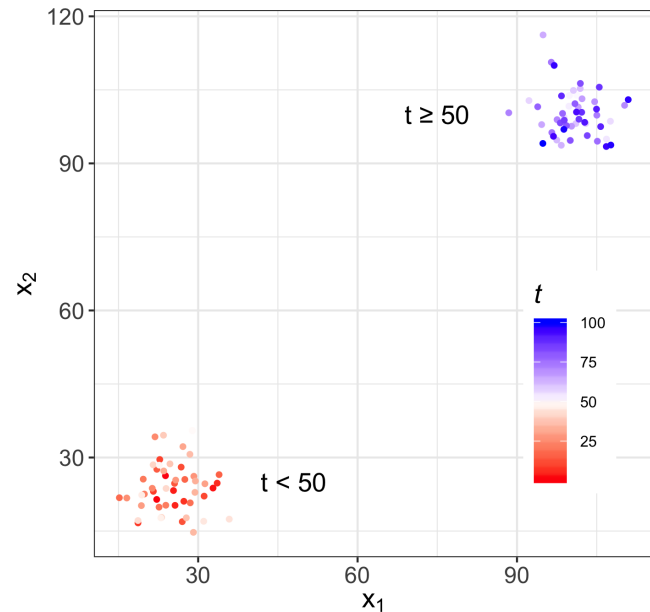
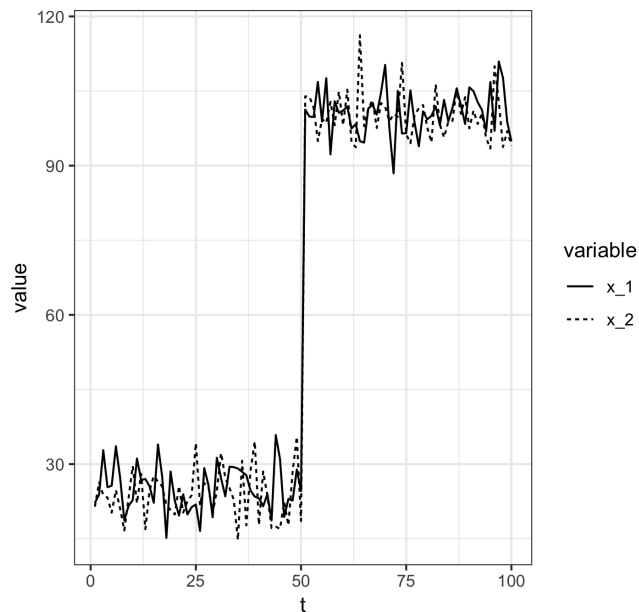


$x \text{ normal}(\mu = 25, \sigma = 5)$ for $t < 50$

$x \text{ normal}(\mu = 100, \sigma = 5)$ for $t \geq 50$

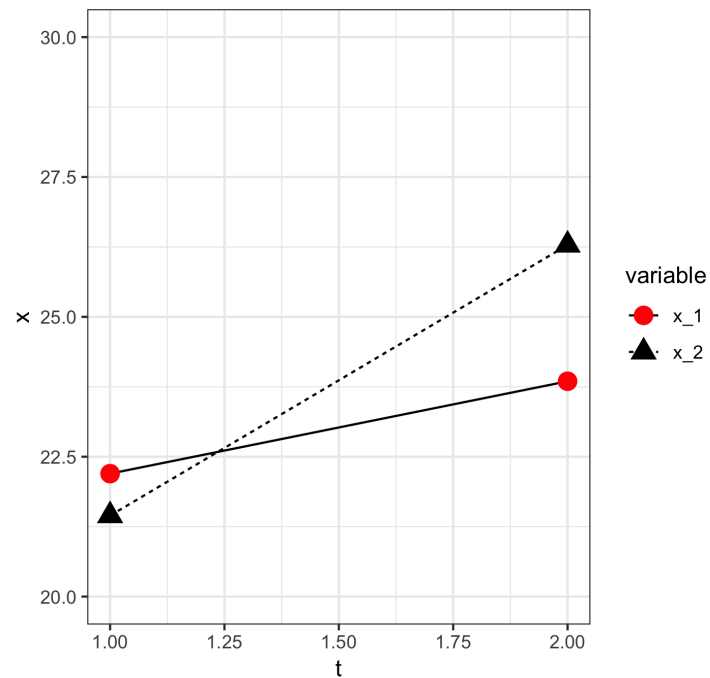
Velocity, $v = \frac{\Delta s}{\Delta t}$

the **linear speed** of a system's **trajectory** (e.g., in phase space)



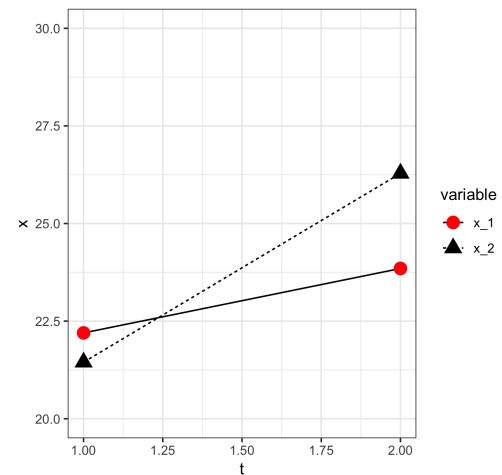
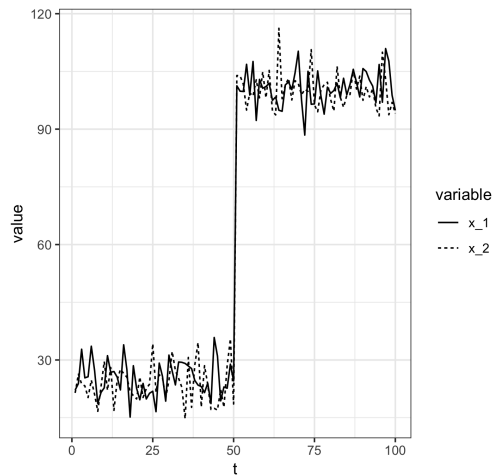
Step 1: Calculate Δx_i

$$\Delta x_i = (x_{i,j} - x_{i-1,j})^2$$



Step 2: Calculate Δs , 'distance travelled'

$$\Delta s_i = \sqrt{\sum_{j=1}^n (x_{i,j} - x_{i-1,j})^2}$$



Step 3: Calculate s , cumulative distance travelled

$$\Delta s_i = \sqrt{\sum_{j=1}^n (x_{i,j} - x_{i-1,j})^2}$$

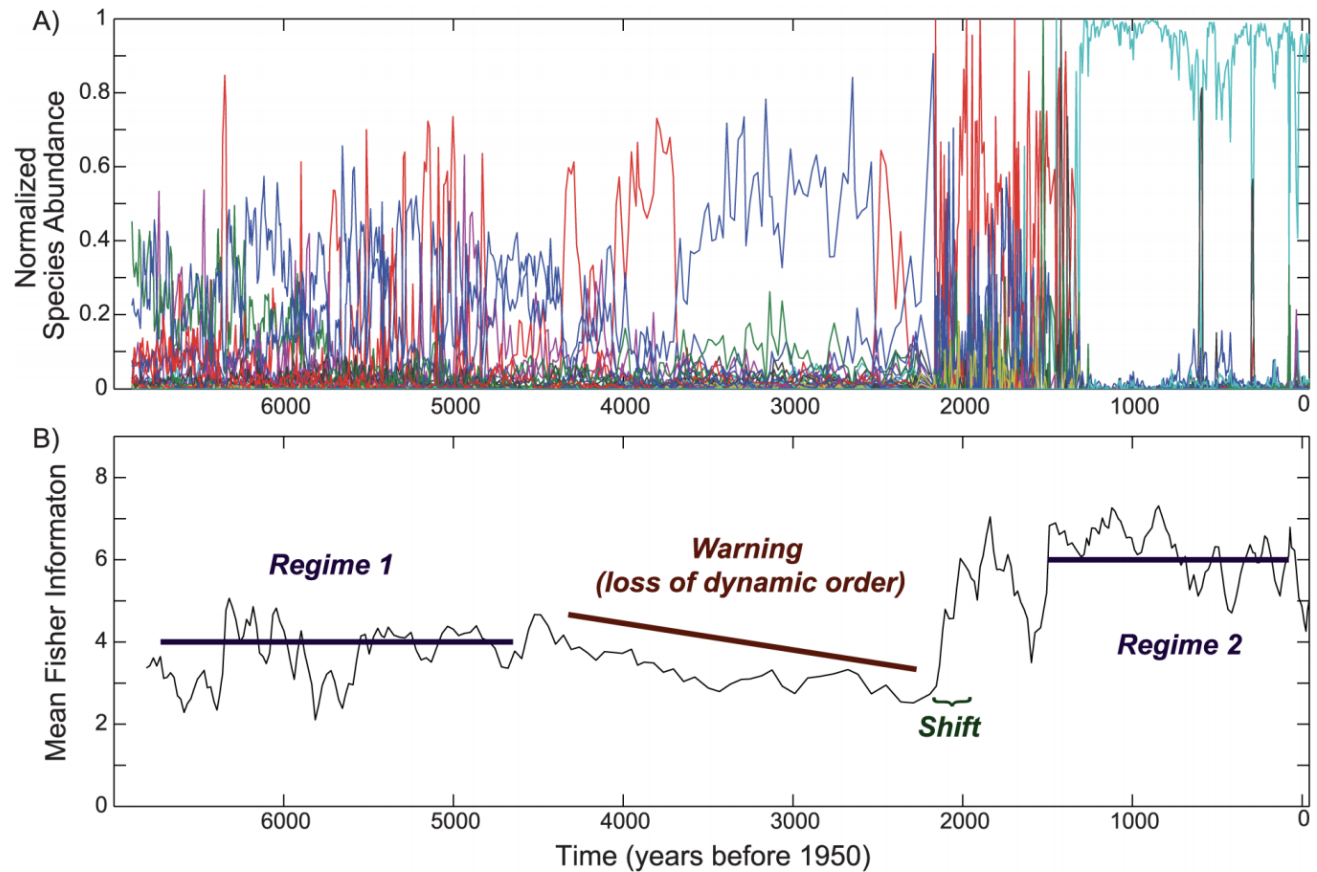
$$s_k = \sum_{i=2}^k \Delta s_i$$

$$2 \leq k \leq n$$

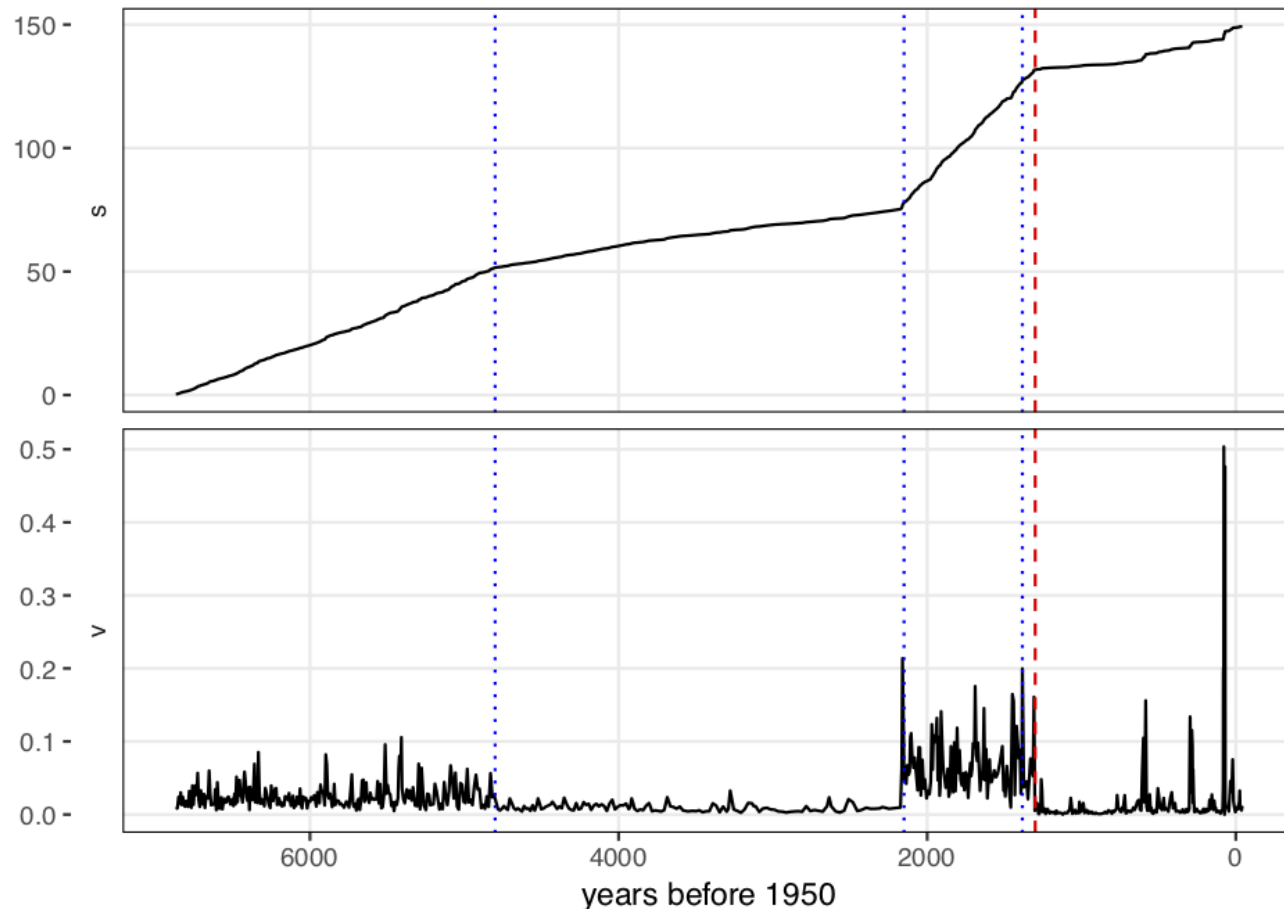
Step 4: Calculate v , the linear speed of s

$$v = \frac{\Delta s}{\Delta t}$$

Empirical System: Paleodiatom Community



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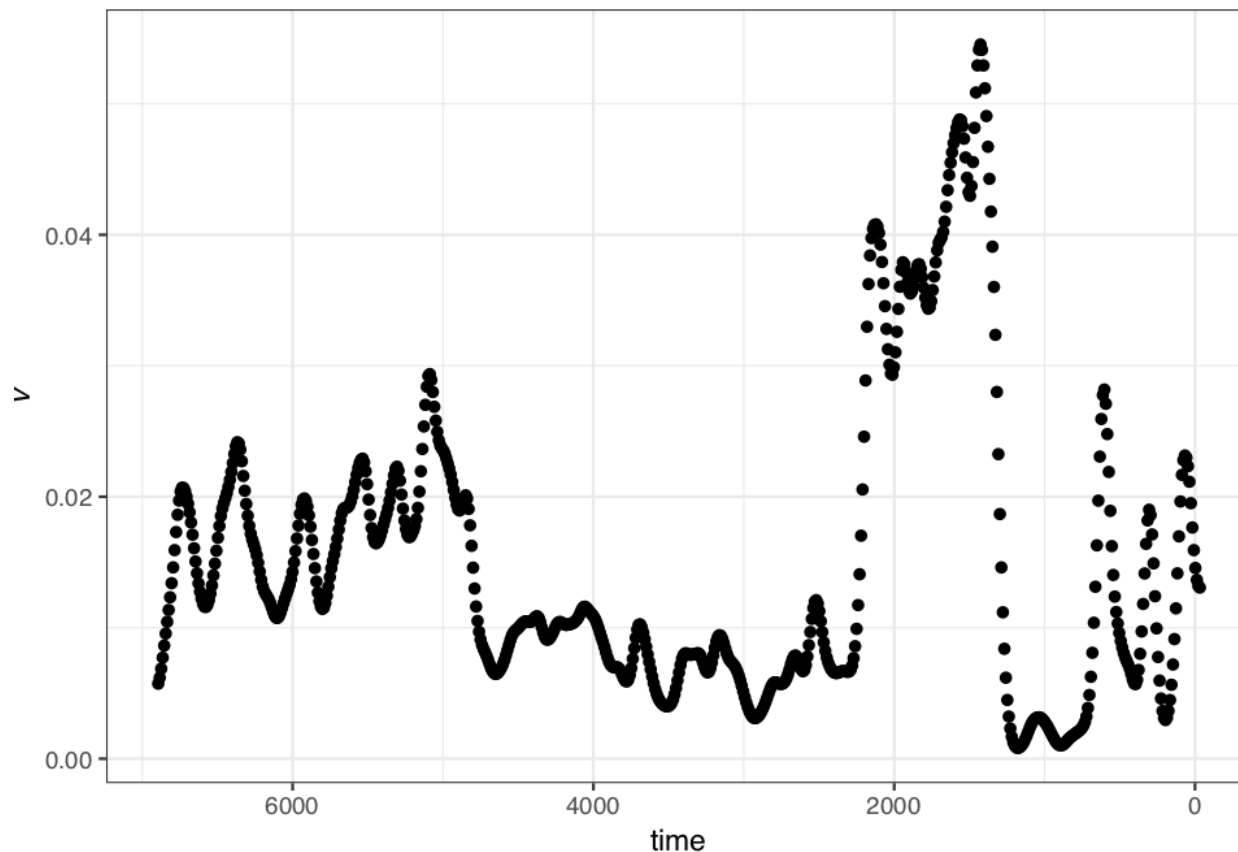


Dotted blue lines = **our** shift points

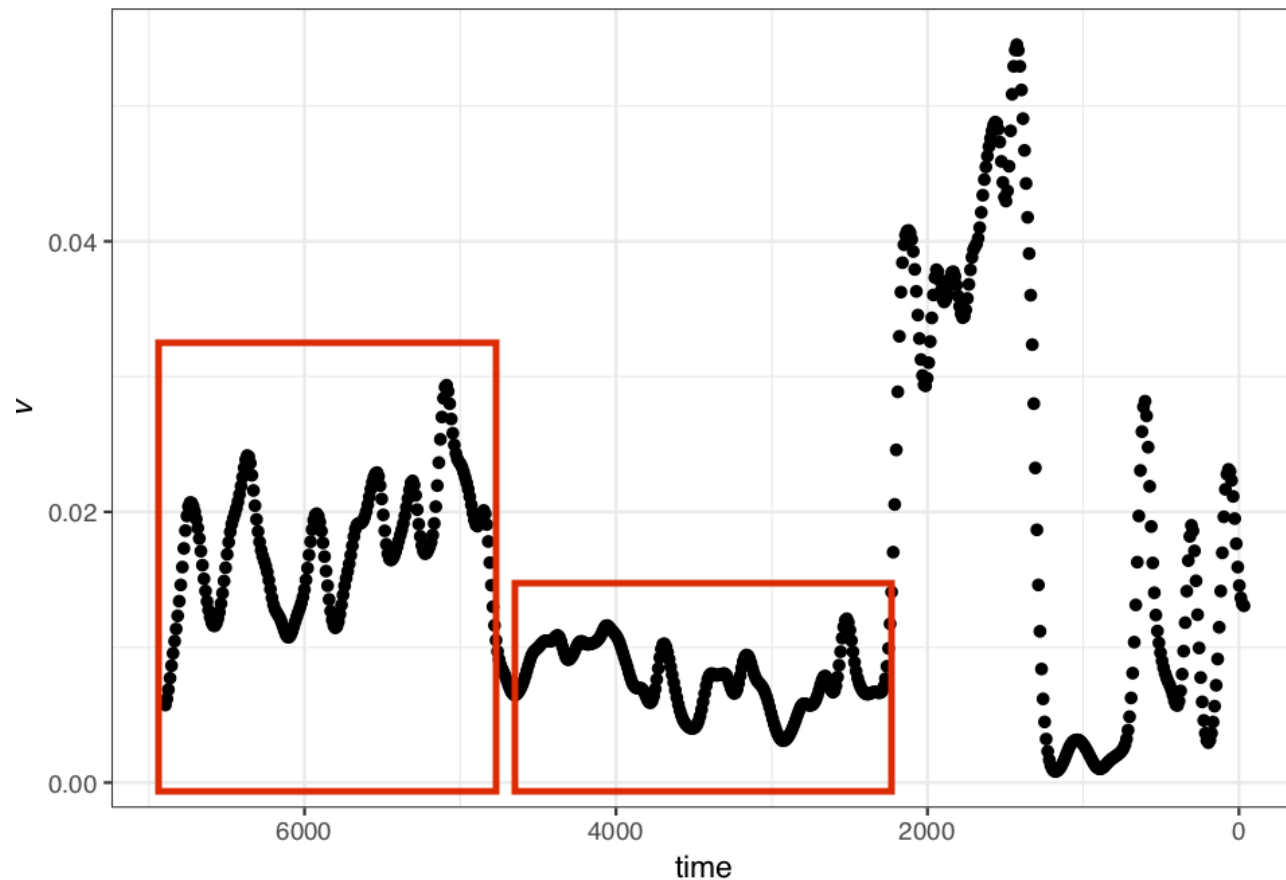
Dashed red line = Spanbauer *et al.* shift point

Getting the Derivatives of Noisy Data

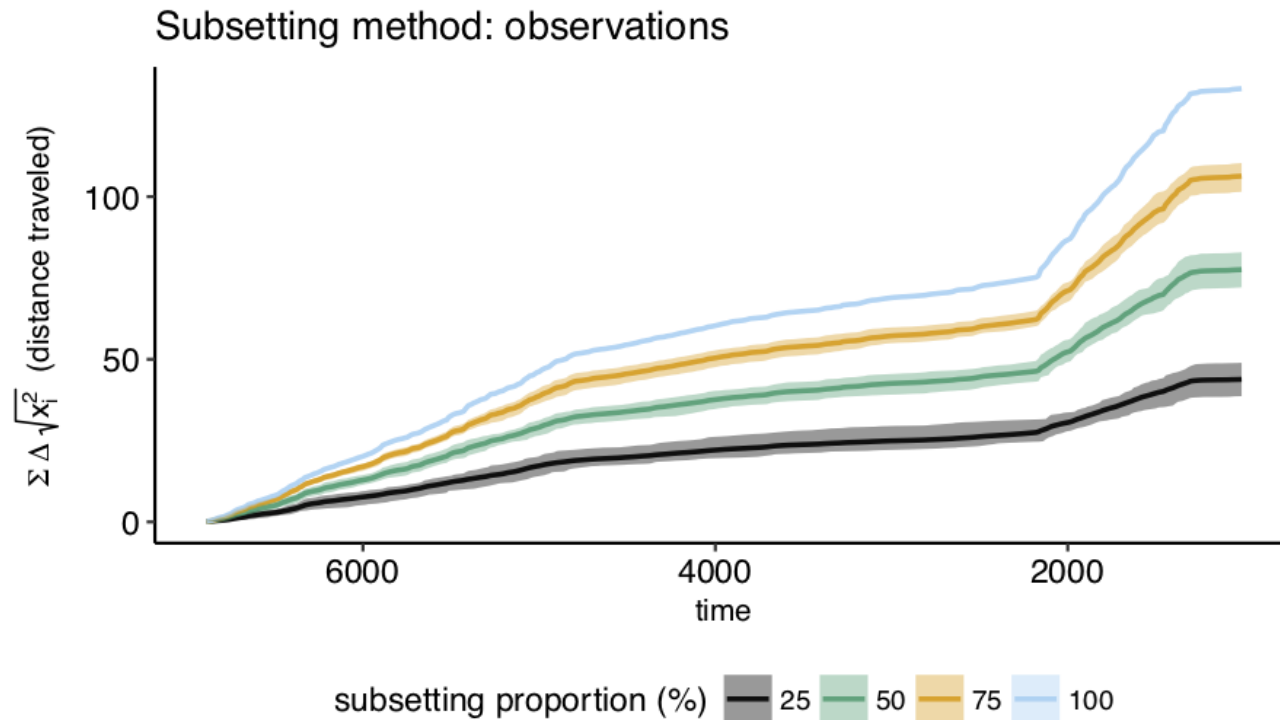
Total Variation Regularized Numerical Differentiation to smooth the original data



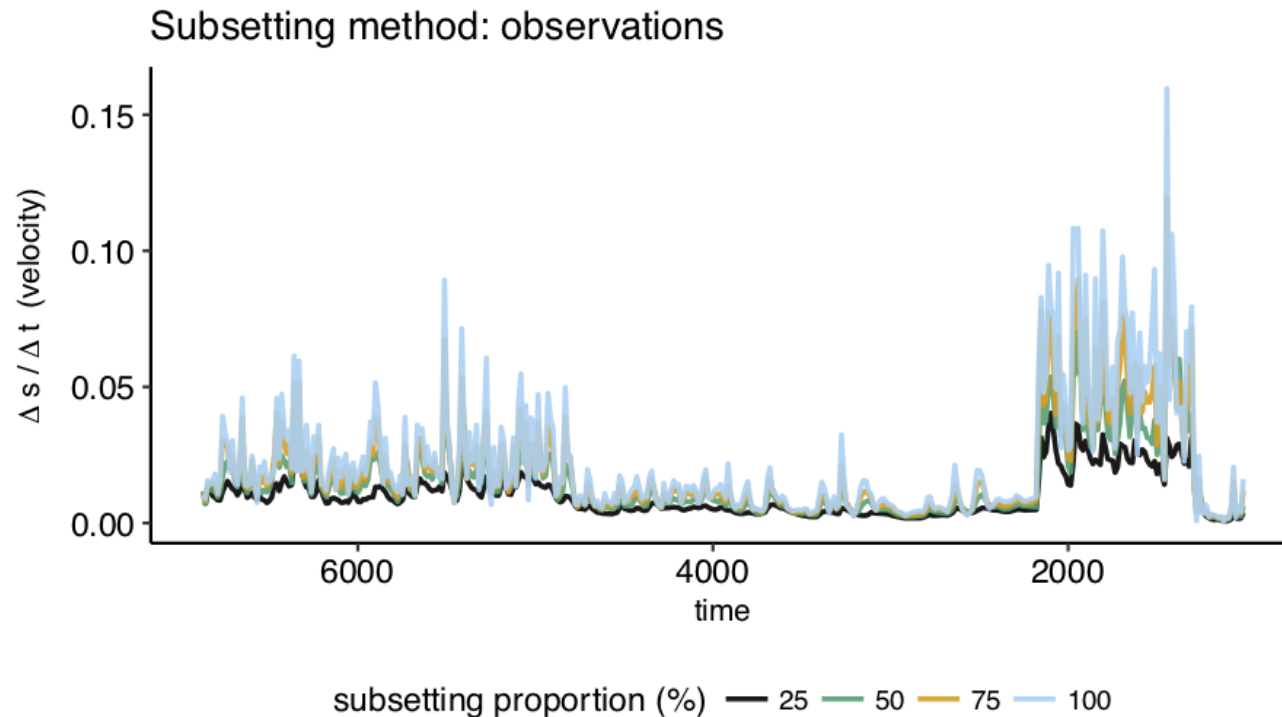
Velocity (v) Identifies Previously Unknown Periodicities



s and v Robust to Data Quality & Quantity Issues



s and v Robust to Data Quality & Quantity Issues



Conclusions

Simply calculation, relative to other regime detection methods

Handles noisy and sparse data

Less sensitive to data quality issues common in ecology

Velocity is best when $\text{mean} > \text{variance}$

Next Steps

Numerical identification of exact change points

Compare to distance-based metrics

Compare to ordination techniques

Identify out-of-sample predictive capacity

Relevant R Packages:

- **distanceTravelled** calculate velocity
- **regimeDetectionMeasures** calculate various metrics
- **bbsRDM** application to Breeding Bird Survey
- **tvdiff** regularized differentiation noisy data

More Information

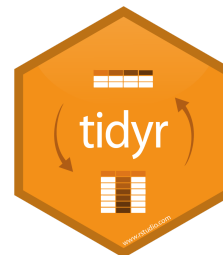
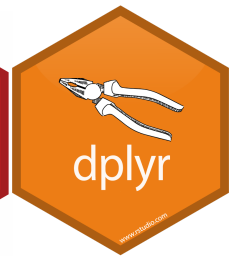
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Analysis & Presentation



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