

CS 662
Artificial Intelligence Programming
Homework #7
Various Topics

name: yxu66

1. $D = \{(x_1, \text{'yes'}), (x_2, \text{'no'}), (x_3, \text{'yes'}), (x_4, \text{'yes'}), (x_5, \text{'no'}), (x_6, \text{'yes'})\}$

The values of the similarity function, K , for a new point x_0 are: $K(x_0, x_1)=2$, $K(x_0, x_2)=1.5$, $K(x_0, x_3)=1.8$, $K(x_0, x_4)=2.3$, $K(x_0, x_5)=2.1$, $K(x_0, x_6)=1.7$

1) What is the 1-NN classification of x_0 ?

min: $K(x_0, x_2)=1.5$, check x_2 , so the classification is no.

2) What is the 3-NN classification of x_0 ?

min: $K(x_0, x_2)=1.5$, $K(x_0, x_6)=1.7$ and $K(x_0, x_3)=1.8$

check $x_2 = \text{no}$, $x_6 = \text{yes}$, $x_3 = \text{yes}$, so the classification is yes.

2. Naïve Bayes

Given:

class A : money (4 times), finance (1 time), stock (10 times), and market (6 times)

class B : money (1 time), loss (20 times), finance (20 times), and gain (5 times)

Document: "money finance loss stock gain average"

In class A: $P(\text{money} \mid \text{categoryA}) = 4/21$,

$$\begin{aligned}P(\text{finance} \mid \text{categoryA}) &= 1/21, \\P(\text{stock} \mid \text{categoryA}) &= 10/21, \\P(\text{market} \mid \text{categoryA}) &= 6/21,\end{aligned}$$

$$\begin{aligned}\text{In class B: } P(\text{money} \mid \text{categoryB}) &= 1/46, \\P(\text{loss} \mid \text{categoryB}) &= 20/46 = 10/23, \\P(\text{finance} \mid \text{categoryB}) &= 20/46 = 10/23, \\P(\text{gain} \mid \text{categoryB}) &= 5/46,\end{aligned}$$

$$P(A) = 5/15 = 1/3$$

$$P(B) = 10/15 = 2/3$$

$$\begin{aligned}\text{So } vA &= P(A) * P(\text{money} \mid \text{categoryA}) * P(\text{finance} \mid \text{categoryA}) \\&* 1/10000 * P(\text{stock} \mid \text{categoryA}) * 1/10000 * 1/10000 \\&= 1/3 * 4/21 * 1/21 * 1/10000 * 10/21 * 1/10000 * 1/10000 \\&= 1.4397293e-15\end{aligned}$$

$$\begin{aligned}vB &= P(B) * P(\text{money} \mid \text{categoryB}) * P(\text{finance} \mid \text{categoryB}) * P(\text{loss} \\&\mid \text{categoryB}) * 1/1000 * P(\text{gain} \mid \text{categoryB}) * 1/10000 \\&= 2/3 * 1/46 * 10/23 * 10/23 * 1/10000 * 5/46 * 1/10000 \\&= 2.9778815e-12\end{aligned}$$

So the document is belong to class B.

3.

The accuracy without negation:

IntegratedCons.txt: pros -> 0.122, cons -> 0.878

IntegratedPros.txt: pros -> 0.748, cons -> 0.252

The accuracy with negation:

IntegratedCons.txt: pros -> 0.120, cons -> 0.880

IntegratedPros.txt: pros -> 0.749, cons -> 0.251

4. Utility & VPI

1) Suppose the ham:spam = 5 : 5

	spam -> spam	ham -> spam	spam -> ham
c1	85%	8%	1 - 85% = 15%
c2	70%	2%	1 - 70% = 30%
cost		\$1	\$0.05

So for c1, $\text{cost}(c1) = 1000 \cdot 50\% \cdot 8\% \cdot 1 + 1000 \cdot 50\% \cdot 15\% \cdot 0.05 = 43.75(\$)$

for c2, $\text{cost}(c2) = 1000 \cdot 50\% \cdot 2\% \cdot 1 + 1000 \cdot 50\% \cdot 30\% \cdot 0.05 = 17.50(\$)$

So c2 is better than c1.

2)

choice1: The value (utility) of buying an apartment building in good economic conditions is \$50,000 and \$30,000 in bad conditions.

choice2: The value of buying an office building in good economic conditions is \$100,000 and -\$40,000 in bad conditions.

choice3: The value of buying a warehouse in good economic conditions is \$30,000 and \$10,000 in bad conditions.

We know: The probability of being in good economic conditions is .6 and the probability of being in bad economic conditions is .4

$\text{EU}(\text{choice1}) = 50000 \cdot 0.6 + 30000 \cdot 0.4 = 42000$

$\text{EU}(\text{choice2}) = 100000 \cdot 0.6 + (-40000 \cdot 0.4) = 44000$

$\text{EU}(\text{choice3}) = 30000 \cdot 0.6 + (10000 \cdot 0.4) = 22000$

The value of knowing whether we are in good or bad economic conditions:

$= 100000 \cdot 0.6 + 30000 \cdot 0.4 - \text{EU}(\text{choice2})$

$= 28000 (\$)$

5. MDP

1)

After first step up:

1		2		3		4	
5	0.8	6		7		8	
9	0.1	10	0.1	11		12	

After second step up:

1	0.64	2		3		4	
5	0.24	6		7		8	
9	0.02	10	0.09	11	0.01	12	

After third step right:

1		2		3		4	
0.088		0.512					
5		6		7		8	
0.258				0.001			
9		10		11		12	
0.026		0.034		0.073		0.008	

After fourth step right:

1 0.088	2 0.512	3	4
5 0.258	6	7 0.001	8
9 0.026	10 0.034	11 0.073	12 0.008

After fifth step right:

1 0.02524	2 0.06224	3 0.17994	4 0.32776
5 0.18054	6	7 0.04443	8 0.014
9 0.02462	10 0.02824	11 0.02627	12 0.08672

2)

1 -0.02	2 0.35	3 0.65	+1
4 -0.02		5 0.28	-1
6 -0.02	7 0.01	8 0.02	9 0.01

Update rule:

$$U_{i+1}(s) = R(s) + \gamma \max_a \sum_s P(s|s,a) U_i(s)$$

Assume $\gamma = 0.8$

Assume time cost is -0.04: ($R(s) = -0.04$)

There are 4 directions the square 3 can take:

a. left: $0.8U(2) + 0.1U(3) + 0.1U(5) = 0.8*0.35 + 0.1*0.65 + 0.1*0.28 = 0.373$

b. right: $0.8*1 + 0.1U(3) + 0.1U(5) = 0.8*1 + 0.1*0.65 + 0.1*0.28 = 0.893$

c. down: $0.8*(5) + 0.1U(2) + 0.1*1 = 0.8*0.28 + 0.1*0.35 + 0.1*1 = 0.359$

d. up: $0.8U(3) + 0.1U(2) + 0.1*1 = 0.8*0.65 + 0.1*0.35 + 0.1*1 = 0.655$

so the max is right direction and according to the update rule:

$$U_3' = -0.04 + 0.8 * 0.893 = 0.6744$$

