

Question: Is set of odd numbers with binary operations (+), i.e.  $\langle O, + \rangle$  an abelian group?

$\Rightarrow$  solution:  $O = \{ \dots, -3, -1, 1, 3, 5, 7, 9, 11, 13, 15, \dots \}$

1. closure: if  $a, b \in O$  then  $a+b \in O$ .

Let  $a=3, b=5$ ; then  $3+5=8 \notin O$   
so, condition fails this requirement

2. Identity element: 0 is even number so, in  $e+a \in O$  is work out.

3. Associative: ~~at~~ if  $\forall a, b, c \in O$  then  
 $a+(b+c) = (a+b)+c \in O$ .

Let,  $a=3, b=5, c=-3$

then,  $3+(5-3) = (3+5)-3 = 5 \in O$

so, here condition is satisfy.

4. Inverse Element: if  $a \in O, a' \in O$   
and  $(a+a') = e \in O$ .

Let  $a=3; a'=-3; 3-3=0 \in O$



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this  $\emptyset$  pass this requirement.

5. commutative: if  $\forall a, b \in \emptyset$  then

$$(a+b) = b+a \in \emptyset$$

so let  $a=5, b=7$ ;  $5+7 = 7+5 = 12 \notin \emptyset$   
this condition not satisfy.

hence given odd number set is not  
an abelian because it is not ~~to~~ pass  
all the con of condition of abelian.