## CS375 WK7

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Figure 1: Q01: FA

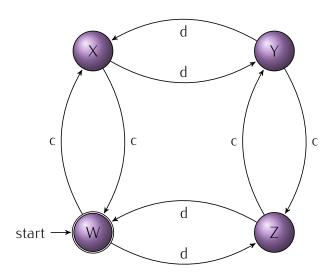


Figure 2: Q01: PDA

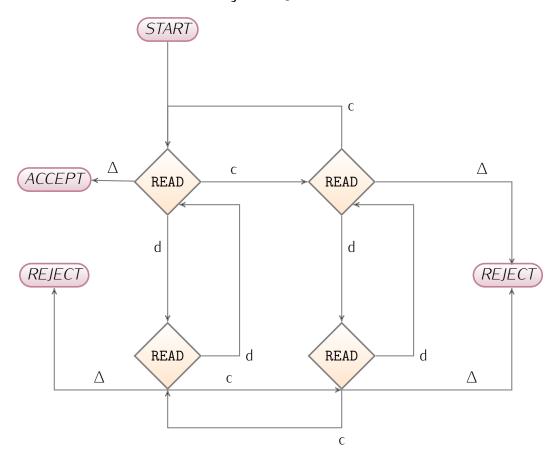
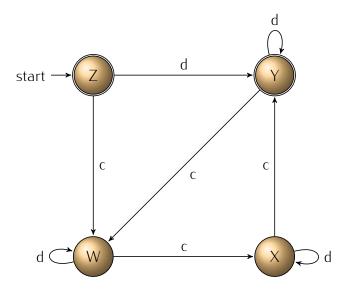


Figure 3: Q02: FA



ACCEPT d Δ START POP POP Δ d C POP d 🛦 d d READ (PUSH d) READ d C REJECT d C PUSH d PUSH d READ READ d d

Figure 4: Q02: PDA

Figure 5: Q03a: Conversion Form

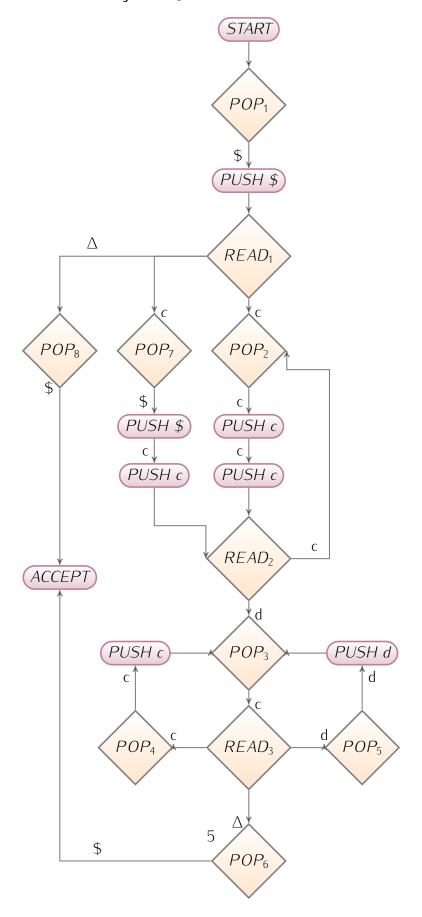


Figure 6: Q03.a Summary Table

FROM Where	To Where	READ What	POP What	PUSH What	ROW Number
START	$READ_1$	Λ	\$	\$	1
$READ_1$	ACCEPT	Λ	\$	-	2
$READ_1$	$READ_2$	С	\$	c\$	3
$READ_1$	$READ_2$	С	С	СС	4
$READ_2$	$READ_2$	С	С	СС	5
$READ_2$	$READ_3$	d	С	-	6
$READ_3$	$READ_3$	С	СС	С	7
$READ_3$	$READ_3$	d	dc	d	7
$READ_3$	ACCEPT	Λ	\$	-	8

Figure 7: Q03.a Productions

Rule 1:  $S \rightarrow Net(START, ACCEPT, \$)$ Rule 2:  $Net(READ_1, ACCEPT, \$) \rightarrow Row_2$   $Net(READ_2, READ_3, \$) \rightarrow Row_6$   $Net(READ_3, ACCEPT, \$) \rightarrow Row_8$ Rule 3:  $Row_1 \rightarrow \Lambda$   $Row_2 \rightarrow \Lambda$   $Row_3 \rightarrow c$   $Row_4 \rightarrow c$   $Row_5 \rightarrow c$   $Row_6 \rightarrow d$   $Row_7 \rightarrow c$  $Row_8 \rightarrow c$ 

Figure 8: Q03.b

STATE	STACK	TAPE
Start	Δ	cccddd
$Read_1$	Δ	cccddd
Push	сΔ	cccddd
$Read_2$	с∆	cccddd
Push	сс∆	cccddd
$Read_2$	сс∆	cccddd
Push	ссс∆	cccddd
$Read_2$	ссс∆	cccddd
Pop	сс∆	cccddd
$Read_3$	сс∆	cccddd
Pop	сΔ	cccddd
$Read_3$	сΔ	cccddd
Pop	Δ	cccddd
$Read_3$	Δ	cccddd
Pop	Δ	cccddd
Accept	Δ	cccddd

**Figure 9:** Q03.c

STATE	STACK	TAPE
Start	Δ	cccdcd
Read <sub>1</sub>	Δ	cccdcd
Push	сΔ	cccdcd
$Read_2$	сΔ	cccdcd
Push	сс∆	cccdcd
Read <sub>2</sub>	сс∆	cccdcd
Push	ссс∆	cccdcd
$Read_2$	ссс∆	cccdcd
Pop	сс∆	cccdcd
$Read_3$	сс∆	cccdcd
Pop	сΔ	cccdcd
$Read_3$	сΔ	cccdcd
Pop	Δ	cccdcd
$Read_3$	Δ	cccdcd
Pop	Δ	cccdcd
Accept	Δ	cccdcd

**Figure 10:** Q03.d

STATE	STACK	TAPE
Start	Δ	cccdcc
Read <sub>1</sub>	Δ	cccdcc
Push	сΔ	cccdcc
$Read_2$	сΔ	ccdcc
Push	сс∆	ccdcc
$Read_2$	сс∆	cccdcc
Push	ссс∆	cccdcc
$Read_2$	ссс∆	cccdcc
Pop	сс∆	cccdcc
Read <sub>3</sub>	сс∆	cccdcc
Pop	с∆	cccdcc
$Read_3$	сΔ	cccdcc
Pop	Δ	cccdcc
$Read_3$	Δ	cccdcc
Pop	Δ	cccdcc
Accept	Δ	cccdcc

**Figure 11:** Q03.e

STATE	STACK	TAPE
Start	Δ	cccdd
$Read_1$	Δ	cccdd
Push	сΔ	cccdd
$Read_2$	сΔ	cccdd
Push	сс∆	cccdd
$Read_2$	сс∆	ccccdd
Push	ссс∆	ccccdd
$Read_2$	ссс∆	ccccdd
Push	сссс∆	ccccdd
$Read_2$	сссс∆	ccccdd
Pop	ссс∆	cccdd
$Read_2$	ссс∆	ccccdd
Pop	сс∆	cccdd
$Read_3$	сс∆	ccccdd
Pop	сΔ	ccccdd
Reject	сΔ	cccdd

Figure 12: Q05-07: Conversion Form

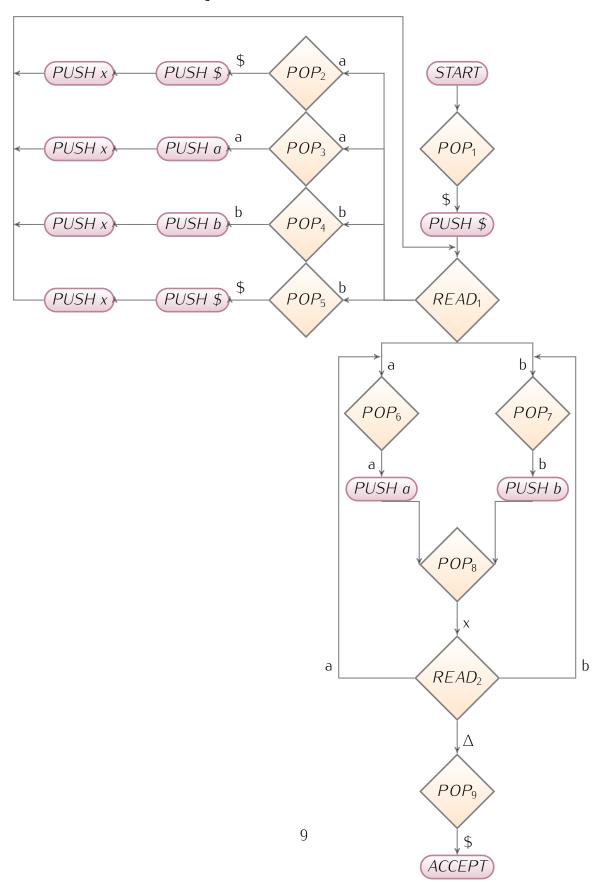


Figure 13: Q05-07: Summary Table

FROM Where	To Where	READ What	POP What	PUSH What	ROW Number
START	$READ_1$	Λ	\$	\$	1
$READ_1$	$READ_1$	a	\$	x\$	2
$READ_1$	$READ_1$	a	a	xa	3
$READ_1$	$READ_1$	b	b	xb	4
$READ_1$	$READ_1$	b	\$	x\$	5
$READ_1$	$READ_2$	a	ax	a	6
$READ_1$	$READ_2$	b	bx	b	7
$READ_2$	$READ_2$	a	ax	a	8
$READ_2$	$READ_2$	b	bx	b	9
$READ_2$	ACCEPT	Δ	\$	-	10

Figure 14: Q05

 $Net(READ_1, READ_1, a)Row2$  $Net(READ_1, READ_2, b)Row7$  $Net(READ_2, ACCEPT, \Delta)Row10$ 

STATE	STACK	TAPE
Start	Δ	ab
Read <sub>1</sub>	Δ	a b
$Push_x$	хΔ	a b
Read <sub>1</sub>	xΔ	ab
Pop	Δ	аЪ
Read <sub>2</sub>	Δ	ab
Pop	Δ	a b
Accept	Δ	ab

Figure 15: Q06

 $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_2, a)Row6$   $Net(READ_2, ACCEPT, \Delta)Row10$ Example with Tape

Example with Tape				
STATE	STACK	TAPE		
Start	Δ	bbba		
$Read_1$	Δ	bbba		
$Push_x$	xΔ	bbba		
Read <sub>1</sub>	xΔ	b b b a		
$Push_x$	xxΔ	b b b a		
$Read_1$	xxΔ	bbba		
Pop	xΔ	bbba		
$Read_2$	xΔ	bbba		
Pop	Δ	bbba		
$Read_2$	Δ	bbba		
Pop	Δ	bbba		
Accept	Δ	bbba		

Figure 16: Q08-11: Conversion Form

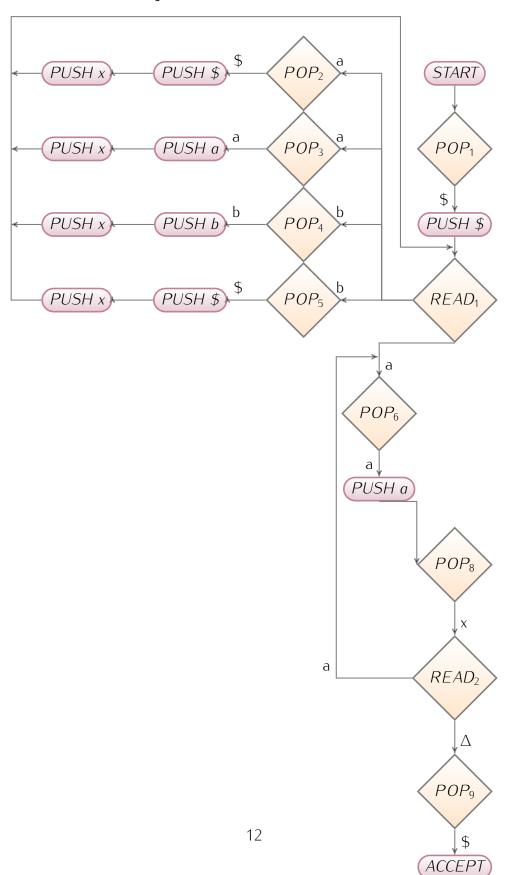


Figure 17: Q08-11: Summary Table

FROM Where	To Where	READ What	POP What	PUSH What	ROW Number
START	$READ_1$	Λ	\$	\$	1
$READ_1$	$READ_1$	a	\$	x\$	2
$READ_1$	$READ_1$	a	a	xa	3
$READ_1$	$READ_1$	b	b	xb	4
$READ_1$	$READ_1$	b	\$	x\$	5
$READ_1$	$READ_2$	a	ax	a	6
$READ_2$	$READ_2$	a	ax	a	8
$READ_2$	ACCEPT	Δ	\$	-	10

**Figure 18:** Q08

 $Net(READ_1, READ_1, a)Row2$  $Net(READ_1, READ_2, a)Row6$  $Net(READ_2, ACCEPT, \Delta)Row10$ 

	1	
STATE	STACK	TAPE
Start	Δ	ab
Read <sub>1</sub>	Δ	a b
Push	xΔ	a b
Read <sub>1</sub>	хΔ	a b
Pop	Δ	a b
Read <sub>2</sub>	Δ	ab
Pop	Δ	ab
Accept	Δ	a b

**Figure 19**: Q09

 $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_1, a)Row2$   $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_2, a)Row6$   $Net(READ_2, READ_2, a)Row8$   $Net(READ_2, READ_2, a)Row8$  $Net(READ_2, ACCEPT, \Delta)Row10$ 

STATE	STACK	TAPE
Start	Δ	babaaa
Read <sub>1</sub>	Δ	aabaaa
Push	xΔ	aabaaa
Read <sub>1</sub>	хΔ	a a b a a a
Push	xxΔ	a a b a a a
$Read_1$	xxΔ	a a a a a
Push	xxxΔ	a a a a a
Read <sub>1</sub>	xxxΔ	a a a a a a
Pop	xxΔ	a a a a a a
$Read_2$	xxΔ	aaaaaa
Pop	хΔ	aaaaaa
$Read_2$	xΔ	aaaaab
Pop	Δ	aaaaab
Read <sub>2</sub>	Δ	aaaaab
Pop	Δ	aaaaab
Accept	Δ	aaaaab

Figure 20: Q10

The PDA for 8-11 is an EVENPALINDROME therefore it is impossible to balance the amount of readable tape with the stack if not even as shown below. If instead of the below example we were to remain in READ 1 an additional cycle then we would have to many x's on the Stack and the tape would complete too soon. In this case the tape completes too late.

 $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_1, a)Row2$   $Net(READ_1, READ_1, b)Row5$   $Net(READ_1, READ_2, a)Row6$   $Net(READ_2, READ_2, a)Row8$   $Net(READ_2, READ_2, b)Row8$ CRASH

STATE	STACK	TAPE
Start	Δ	babaaab
$Read_1$	Δ	aabaaab
Push	хΔ	аарааар
Read <sub>1</sub>	хΔ	aabaaab
Push	xxΔ	aabaaab
$Read_1$	xxΔ	a a a a a b
Push	xxx∆	aaaaab
Read <sub>1</sub>	xxxΔ	a a a a a b
Pop	xxΔ	a a a a a b
Read <sub>2</sub>	xxΔ	a a a a a b
Pop	xΔ	a a a a a b
$Read_2$	xΔ	a a a a a a b
Pop	Δ	a a a a a a b
$Read_2$	Δ	aaaaab
Pop	Δ	aaaaab

Figure 21: Q11

Once again the PDA for 8-11 is an EVENPALINDROME therefore it is impossible to balance the amount of readable tape with the stack if not even as shown below. If instead of the below example we were to remain in READ 1 an additional cycle then we would have to many x's on the Stack and the tape would complete too soon. In this case the tape completes too late. This example is identical to the falure shown above with the exception of the extra character on the string being a 'a'

Net(READ<sub>1</sub>, READ<sub>1</sub>, b)Row5 Net(READ<sub>1</sub>, READ<sub>1</sub>, a)Row2 Net(READ<sub>1</sub>, READ<sub>1</sub>, b)Row5 Net(READ<sub>1</sub>, READ<sub>2</sub>, a)Row6 Net(READ<sub>2</sub>, READ<sub>2</sub>, a)Row8 Net(READ<sub>2</sub>, READ<sub>2</sub>, a)Row8 CRASH

STATE	STACK	TAPE
Start	Δ	babaaaa
$Read_1$	Δ	aabaaaa
Push	хΔ	aabaaaa
Read <sub>1</sub>	хΔ	a a b a a a a
Push	xxΔ	aabaaaa
Read <sub>1</sub>	xxΔ	a a a a a a
Push	xxxΔ	aaaaaa
Read <sub>1</sub>	xxxΔ	a a a a a a
Pop	xxΔ	a a a a a a
$Read_2$	xxΔ	a a a a a a
Pop	xΔ	a a a a a a
Read <sub>2</sub>	хΔ	a a a a a a
Pop	Δ	a a a a a a
Read <sub>2</sub>	Δ	aaaaaab
Pop	Δ	aaaaaab