

# Validating Plate Boundary Observatory borehole strainmeter data with GNSS derived strain

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## 1 Introduction

The Plate Boundary Observatory maintains 82 borehole strain meters (BSMs), most of which are installed along the Western United States. BSMs are able to detect geophysical processes such as coseismic and postseismic deformation (e.g., Langbein et al., 2006; Langbein, 2015), slow slip events (e.g., Dragert and Wang, 2011), and seismic wave propagation (Barbour and Crowell, 2017). BSMs are intended for measuring deformation over timescales of minutes to months. At longer timescales, BSM data is contaminated by factors such as borehole relaxation (Gladwin et al., 1987). Slow slip events and postseismic deformation occur on timescales that near the upper limit of what BSMs can be expected to resolve. Another complication with BSM data is that the strain measured at the borehole may deviate from the regional strain due to local topographic or geologic features (Berger and Beaumont, 1976). Due to these sources of noise, it can be difficult to use BSM data quantitatively in, for example, geophysical inverse problems.

In this study, we assess the ability of BSMs to measure strain resulting from slow slip events (SSEs) on the Cascadia subduction zone. This is done by comparing BSM data to strain derived from GNSS data. There are about forty BSMs in the Pacific Northwest and only five of them, B003, B004, B005, B007, and B018, record noticeable deformation from SSEs. Of these stations B005 and B007 are collocated. We show that only station B004 produces strain that is in reasonable agreement with GNSS derived strain rates. Station B018 records shear strains with opposite polarity as the GNSS derived strains. This discrepancy can be explained by an  $25^\circ$  error in the recorded orientation of the instrument.

GNSS derived strains are computed with Gaussian process regression using the method described in (Hines and Hetland, 2017).

## 2 Data

Each of the PBO BSMs are Gladwin tensor strain meters, which contain four extensometers, or gauges, oriented  $60^\circ$ ,  $60^\circ$ , and  $30^\circ$  apart from each other. We denote the extension measured at gauge  $i$  as  $e_i$ , and the strain tensor components as  $\varepsilon_{xx}$ ,  $\varepsilon_{yy}$ , and  $\varepsilon_{xy}$ , where  $x$  and  $y$  indicate the east and north direction, respectively. The extensions measured at BSMs are traditionally converted into areal strain,  $\varepsilon_a = \varepsilon_{xx} + \varepsilon_{yy}$ , differential strain  $\varepsilon_d = \varepsilon_{xx} - \varepsilon_{yy}$ , and engineering shear strain,  $\varepsilon_s = 2\varepsilon_{xy}$ . If gauge 0 is oriented along direction  $\theta_0$ , measured in degrees north of east, then the strain components can be expressed in terms of the gauge measurements through the equation

$$\begin{bmatrix} \varepsilon_a \\ \varepsilon_d \\ \varepsilon_s \end{bmatrix} = 2\mathbf{K}^{-1} \begin{bmatrix} 1 & \cos(2\theta_0) & \sin(2\theta_0) \\ 1 & \cos(2(\theta_0 + 60)) & \sin(2(\theta_0 + 60)) \\ 1 & \cos(2(\theta_0 + 120)) & \sin(2(\theta_0 + 120)) \\ 1 & \cos(2(\theta_0 + 150)) & \sin(2(\theta_0 + 150)) \end{bmatrix}^+ \begin{bmatrix} e_0 \\ e_1 \\ e_2 \\ e_3 \end{bmatrix}, \quad (1)$$

where “+” indicates the Moore-Penrose pseudoinverse and  $\mathbf{K}$  is a coupling matrix describing how instrument strains relate to the crustal strains (Hart et al., 1996). In this paper  $\varepsilon_a$ ,  $\varepsilon_d$ , and  $\varepsilon_s$  are ideally intended to represent crustal strains. We assume that BSMs are installed in homogeneous, isotropic rock, allowing us to write the coupling matrix as

$$\mathbf{K} = \begin{bmatrix} c & 0 & 0 \\ 0 & d & 0 \\ 0 & 0 & d \end{bmatrix}, \quad (2)$$

where  $c$ , and  $d$  are response factors that depend on the elastic properties of the instrument, the grout, and surrounding rock (Gladwin and Hart, 1985). Based on the analysis of Gladwin and Hart (1985), we use  $c = 1.5$  and  $d = 3.0$ . UNAVCO, the organization responsible for maintaining the PBO BSMs and disseminating their data, use these same response factors for their final data products.

Localize topographic or geologic features can cause  $\mathbf{K}$  to have non-zero off diagonal elements. If possible, the components of  $\mathbf{K}$  should be determined in-situ by calibrating the BSM data with a well known strain source, such as diurnal and semi-diurnal tides (Hart et al., 1996; Roeloffs, 2010; Hodgkinson et al., 2013). Hart et al. (1996) calibrated a BSM at Pinyon Flat, using the tidal strains recorded at a collocated laser strain meter. This calibration method is, of course, not possible for most PBO BSMs. Roeloffs (2010) and Hodgkinson et al. (2013) calibrated PBO BSMs using theoretical predictions of tidal strains (e.g., Agnew, 1997). This approach is still not adequate for BSMs near large local bodies of water, which can make it difficult to form an accurate theoretical estimate of tidal strains. As determined by Roeloffs (2010), the five BSM stations considered in this paper are too close to the Strait of Juan de Fuca to be accurately calibrated with tidal strains. Since in-situ calibration is not possible, we acknowledge that our choice for  $\mathbf{K}$  is likely to be a significant source of error in BSM data. Another source of error is orientation.

While eq. 2 with  $c = 1.5$  and  $d = 3.0$  is our best guess for an appropriate coupling matrix, this assumption is likely to be a significant source of error.

our best choice for to assume the coupling matrix from eq. 2.

complicate it can difficult to accurately account for local bodies of water in theoretical predictions of tidal strains, and the BSM can be prone to error at BSMs near large local bodies of water. It is not possible not a calibration strategy It is not always possible, or at least advisable, to calibrate BSMs with theoretical predictions of tides

which Coupling matrices should be determined in-situ for each

If possible, the coupling matrix should be determined in-situ, the can also be determined

If possible, the coupling matrix should be determined in-situ, by finding the components  $\mathbf{K}$  that are calibrating the BSM with some

the areal, differential, and engineering shear strain measured by the instrument relate to those strain

Assuming that the first gauge is oriented along  $\theta$ , then the extensional strains measured at each gauge,  $[e_0, e_1, e_2, e_3]$ , can be converted to the traditionally used areal strain,  $\varepsilon_a$ , differential strain,  $\varepsilon_d$ , and engineering shear strain,  $\varepsilon_s$ , by

These BSMs can measure the full horizontal strain tensor with

that record extension along four azimuths In this study we use the level2 PBO BSM data provided by UNAVCO at [www.unavco.org](http://www.unavco.org).

foo Hines and Hetland (2017)

### 3 Method

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## References

- Agnew, D. C. (1997). NLOADF: A program for computing ocean-tide loading. *Journal of Geophysical Research*, 102:5109–5110.
- Barbour, A. J. and Crowell, B. W. (2017). Dynamic Strains for Earthquake Source Characterization. *Seismological Research Letters*, 88(2A):354–370.
- Berger, J. and Beaumont, C. (1976). An analysis of tidal strain observations from the United States of America II. The inhomogeneous tide. *Bulletin of the Seismological Society of America*, 66(6):1821–1846.
- Dragert, H. and Wang, K. (2011). Temporal evolution of an episodic tremor and slip event along the northern Cascadia margin. *Journal of Geophysical Research: Solid Earth*, 116(12):1–12.
- Gladwin, M. T., Gwyther, R. L., Hart, R., Francis, M., and Johnston, M. J. S. (1987). Borehole tensor strain measurements in California. *Journal of Geophysical Research: Solid Earth*, 92(B8):7981–7988.
- Gladwin, M. T. and Hart, R. (1985). Design parameters for borehole strain instrumentation. *Pure and Applied Geophysics*, 123(1):59–80.
- Hart, R. H. G., Gladwin, M. T., Gwyther, R. L., Agnew, D. C., and Wyatt, F. K. (1996). Tidal calibration of borehole strain meters: Removing the effects of small-scale inhomogeneity. *Journal of Geophysical Research*, 101(96).
- Hines, T. T. and Hetland, E. A. (2017). Unbiased characterization of noise in geodetic data. *submitted to Journal of Geodesy*.

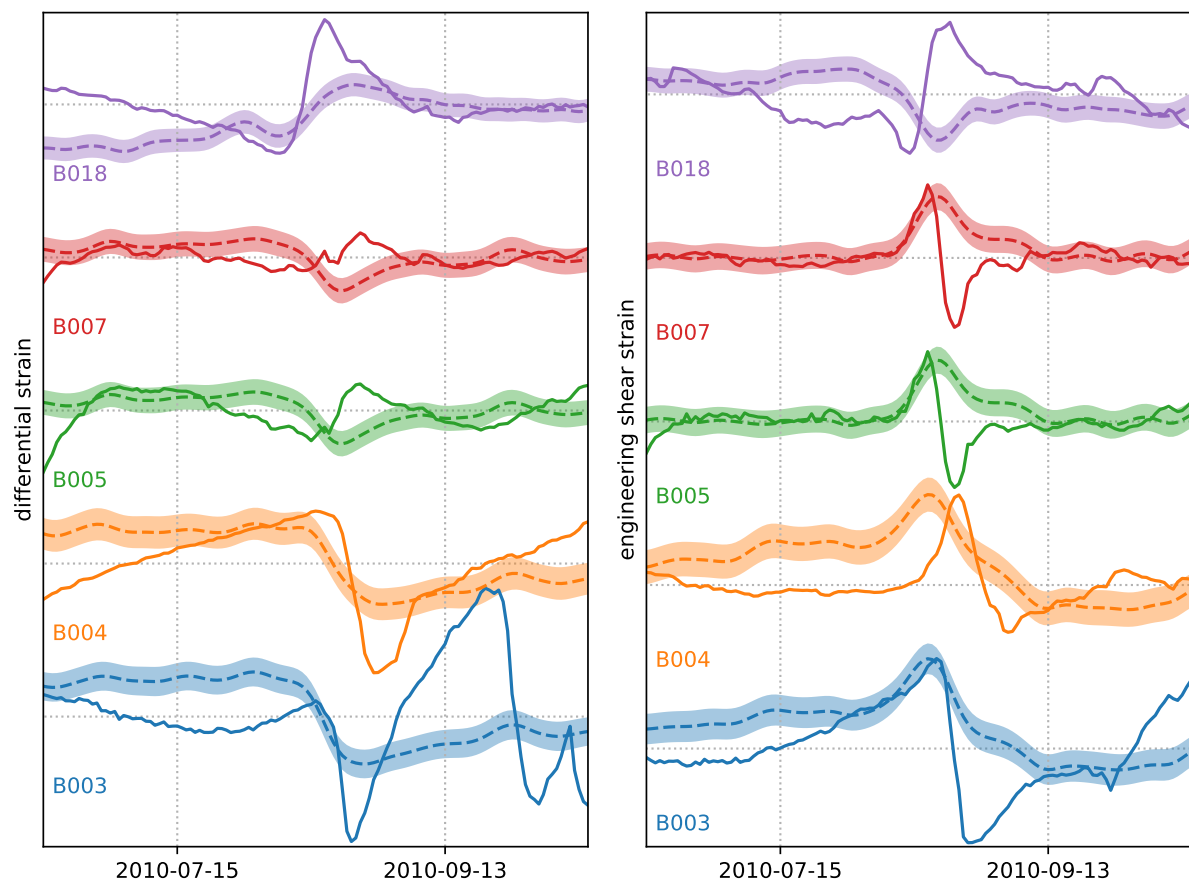


Figure 1: foo

- Hodgkinson, K., Agnew, D., and Roeloffs, E. (2013). Working With Strainmeter Data. *Eos, Transactions American Geophysical Union*, 94(9):91–91.
- Langbein, J. (2015). Borehole strainmeter measurements spanning the 2014 Mw6.0 South Napa Earthquake, California: The effect from instrument calibration. *Journal of Geophysical Research B: Solid Earth*, 120(10):7190–7202.
- Langbein, J., Murray, J. R., and Snyder, H. A. (2006). Coseismic and initial postseismic deformation from the 2004 Parkfield, California, earthquake, observed by global positioning system, electronic distance meter, creepmeters, and borehole strainmeters. *Bulletin of the Seismological Society of America*, 96(4 B):304–320.
- Roeloffs, E. (2010). Tidal calibration of Plate Boundary Observatory borehole strainmeters: Roles of vertical and shear coupling. *Journal of Geophysical Research: Solid Earth*, 115(6):1–25.