Cash Flow Dispersion Model, An Application of the *Economic Order Quantity* to Personal Finance

A Preprint

Anthony Trevino
Computer Science Graduate Student, Cloud Technologist
Georgia Institute of Technology, Ant Finance LLC
trevino293@gmail.com

December 28, 2023

Abstract

This paper defines a cash flow dispersion model that minimizes liquid assets inventory whilst comfortably maintaining the ability to meet periodic demand. Migrating excess liquid asset inventory gained to long term asset inventory, thus increasing the amount of assets available to gain interest. Cumulative average estimates are used to account for variation in investment returns and cash flow habits. The resulting aggregate estimates of cash flows, liquid assets, long term assets and long term assets return percentage will be used to determine economic reorder point and order quantity. Dollars which can be considered equal to inventory will be migrated between long term and liquid asset balances based upon the economic order quantity model and policy and intuitive investment threshold. This model can be used to understand a target cash flow state, providing target account values, triggers, order quantity kickstarting progression toward confident cash flow forecasting for an individual or corporation. With the expansion of deep learning algorithms and open banking, the ability to predict and measure performance against this model may be attainable in future study.

Keywords Economic Order Quantity · Personal Finance · Asset Management, Inventory Management

1 Preface

This is my first draft and attempts to apply engineering theory and mathematics to solve a complex problem. The problem statement is defined as running out of funds in the final stages of life due to poor planning and optimization of assets. I once read a statistic stating that the median of Americans aggregate savings is $570 and on average $33,000. Whether these numbers are accurate or not is beside the problem, the range that they are in is not near an acceptable level for long term feasibility.

It is important to understand that this is my first attempt at creating a mathematically valid and acceptable model. Without in depth graduate level or higher qualifications in these subjects my attempt at the model is just that, an attempt. I understand that there will be critique and learning opportunities through development and feedback of this model, I welcome this. I have created this for fun and really couldn't get my mind away from the problem as I embark on my own personal asset management journey. Therefore I tried to write it up for more clarity, reference and validation. I hope to help others by applying this model, automated through a website, generating long term asset estimates and other financial metrics that could provide insight to potential asset positions over time.

Model Development Timeline:

Initial idea and documentation in April 2019.
Refinement for arxiv.org and peer review in December 2023.

2 Introduction

The objective is to minimize liquid assets inventory whilst comfortably maintaining ability to meet periodic demand. Additionally migrating excess liquid asset inventory gained to long term asset inventory, thus increasing the amount of assets available to gain interest. Significantly increasing the amount of savings available to gain interest through application of the economic order quantity model to aggregate liquid assets. First define an aggregate estimate of period based cash flows generating net change per period. The provided net change is added to liquid asset balance demand following the inventory demand distribution for this model. This demand distribution will be used to compute the economic order quantity Q_i to order and reorder point r_i per period.

Relating Q_i and r_i to personal asset management, liquid asset balance will be defined as inventory I_i. Liquid assets encompass credit lines, cash assets or any money that is used frequently and can be readily accessed, will not gain interest. A 0% return on investment account is influencing the liquid asset balance per period, an i period will be on the same interval as the sample net change of cash flows. The objective is to minimize inventory, migrating as much assets to long term assets balance S_i, your future self in the account that will be gaining interest. Long term assets also will have to aggregated to a single amount but in addition tied to an investment return rate i. This will be used to model the increase of long term asset balance over time.

I notice large places for variation within the model, expecting someone to give an average accurate forecast of all credits and debits per period is unlikely. Even more unlikely is trying to estimate an accurate aggregate investment return percentage with many distributed investment assets. However I believe by asking about the confidence in the ability to adhere to the estimates provided, a confidence interval of demand can be applied to model some of this variation.

3 Methodology

Adapt and apply the economic order quantity model shown in professor Ronald Askin's IEE 461 [1] production control course to generate a feasible mathematical model which minimizes aggregate liquid asset balance. An example is shown, the results will be analyzed using methods of statistical process control to gain insight and validate the results of the EOQ application.

3.1 Demand and Net Change

Aggregate liquid asset balance per period I_i will be estimated through sampling the net change to a theoretical 'master checking account' which can account for all cash flow within the period. Cash will be dispersed through spending, holding and investing money. Dispersion provides the net change per period NC_i, translating to a demand distribution of:

$$if\ NC_i < 0 \implies D_i = |NC_i|$$
$$\text{else } D_i = 0 \tag{1}$$

3.2 Investments

This distribution is based upon that when cumulative net change within a period is greater than 0 money was gained, therefore there is no impact or demand on the liquid asset balance, only surplus cash. This surplus will be addressed through investing at the end of the period if liquid asset balance surpases the reorder point plus order quantity plus investment amount or Y_i the Investment threshold. A defined target investment quantity z will be used to calculate the investment threshold.

The investment threshold value $Y_i = r_i + Q_i + z$ is a first instinct to me as when I would feel comfortable to invest. My inventory or liquid assets would have more than the entire amount to be invested plus one economic order quantity plus the economic reorder point. A substantial buffer of inventory left after the investment is removed. Additionally the actual amount invested will be the current inventory minus the investment threshold, minus demand or $I_i - Y_i - D_i$ I believe this will give strong resistance to changes in demand and allow the inventory to remain positive over time, reducing the exposure to negative assets, debt.

$$\text{Invest if } I_i > r_i + Q_i + z \text{ and } I_i - (I_i - r_i - Q_i - z) - D_i > 0$$
$$\text{Investment threshold } Y_i = r_i + Q_i + z \tag{2}$$

3.3 Liquid Assets

The economic order quantity or Q_i asssets will be removed from long term assets to meet demand when the liquid assets inventory falls below the re-order point r_i.

$$if\ I_i > Y_i \implies \Delta_{i|+} = I_i - Y_i$$
$$if\ I_i < 0 \implies \Delta_{i|-} = |I_i|$$

$$\text{Net Change } = NC_i = Q_i - (\Delta_{i-1|+} + D_i) + \Delta_{i-1|-}$$
$$\implies I_i = I_{I-1} + NC_i$$

3.4 Long Term Assets Distribution

Aggregate long term assets per period S_i is an estimated value of all long term saving methods. Aggregate investment return i is an estimated average return percentage of all long term saving methods. This balance will be gaining investments $\Delta_{i|+}$, interest at i and losing economic order quantities Q_i. The resulting long term assets distribusion is defined by the following.

$$if\ I_i > Y_i \text{ and } I_i - \Delta_{i|+} - D_i > 0 \implies \quad S_i = S_i(1 + i_i) + (\Delta_{i|+} - D_i)$$
$$if\ 0 < I_i < r_i \implies \quad S_i = S_i(1 + i_i) - Q_i$$
$$if\ I_i < 0 \implies \quad S_i = S_i(1 + i_i) - Q_i - \Delta_{i|-}$$

4 Example Problem

The following section will be an example and explanation of each parameter within the economic order quantity model relating to this application. These are an adaptation of the parameters defined to build the economic order quantity model which were shown in the course applied to inventory management rather than asset flow.

4.1 Variable Definiton

• **Holding Costs:** $i\,C\,\overline{I}$

• **Return:** i = estimate return on long term assets

• **Cost per Unit:** $C = 1\$ = 1\ Unit$

• **Average Inventory, Liquid Assets:** $\overline{I} \implies \overline{I}_i = \frac{1}{i}\sum_{i=0}^{i} I_i$

• **Opportunity Cost:** $h_i = i\,C\,\overline{I}_i$

• **Setup Cost:** $= \frac{AD}{Q}$

• **Income:** $= A_i$ = Approximate cash generated per period

• **Net Change:** = Sum of all Cash flows in period $= NC_i = CF_i^+ - CF_i^-$

• **Demand:** = Sum of all Cash flows in period $= NC_i = CF_i^+ - CF_i^-$

$$\xi_{ij}(t) = P(x_t = i, x_{t+1} = j | y, v, w; \theta) = \frac{\alpha_i(t)a_{ij}^{w_t}\beta_j(t+1)b_j^{v_{t+1}}(y_{t+1})}{\sum_{i=1}^{N}\sum_{j=1}^{N}\alpha_i(t)a_{ij}^{w_t}\beta_j(t+1)b_j^{v_{t+1}}(y_{t+1})} \tag{3}$$

4.1.1 Headings: third level

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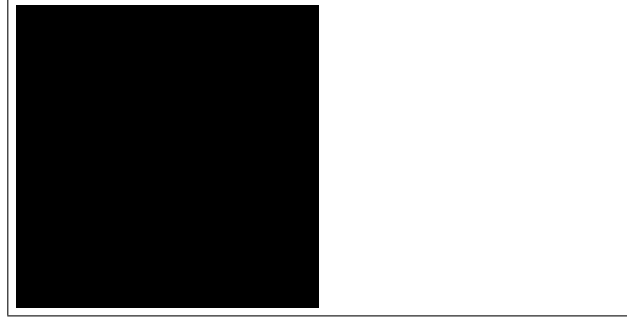
Figure 1: Sample figure caption.

Table 1: Sample table title

	Part	
Name	Description	Size (μm)
Dendrite	Input terminal	$\sim$100
Axon	Output terminal	$\sim$10
Soma	Cell body	up to 10^6

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Paragraph   Sed commodo posuere pede. Mauris ut est. Ut quis purus. Sed ac odio. Sed vehicula hendrerit sem. Duis non odio. Morbi ut dui. Sed accumsan risus eget odio. In hac habitasse platea dictumst. Pellentesque non elit. Fusce sed justo eu urna porta tincidunt. Mauris felis odio, sollicitudin sed, volutpat a, ornare ac, erat. Morbi quis dolor. Donec pellentesque, erat ac sagittis semper, nunc dui lobortis purus, quis congue purus metus ultricies tellus. Proin et quam. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos hymenaeos. Praesent sapien turpis, fermentum vel, eleifend faucibus, vehicula eu, lacus.

5   Examples of citations, figures, tables, references

5.1   Figures

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5.2   Tables

See awesome Table 1.

5.3   Lists

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- consectetur adipiscing elit.

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[1]Sample of the first footnote.

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References

[1] Ronald Askin (2019) *Chapter 6, Inventory Management and the EOQ*, Lecture 5 IEE 461, Arizona State University.