

Binary Neutron Star Simulations: New Tools and Insights

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GW170817: Welcome to the Multi-messenger Era

Event

Object: BNS

Total mass: $2.74M_{\odot}$

Distance: 40 Mpc

GW Radiation: $0.025M_{\odot}$

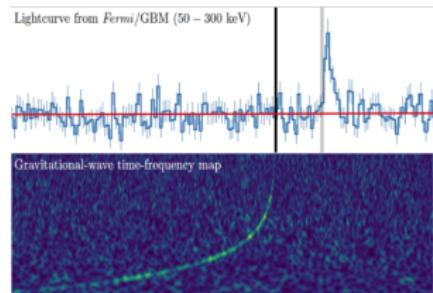
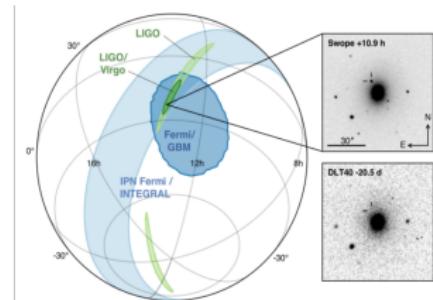
GW Duration: 100 s

Galaxy: NGC-4993

Science

- short gamma ray burst
 - kilonova (optical → radio)
 - neutrinos (none-found)
 - r-process nuclei
 - speed of gravity
 - EOS constraints
 - H_0 constraints

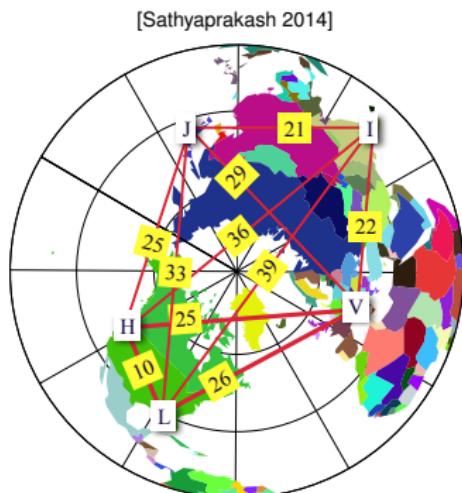
arXiv:1710.05833



Next-Generation Gravitational Wave Astronomy

Detector network by ≈ 2026

- LIGO A+ (Washington State)
 - LIGO A+ (Louisiana)
 - aVIRGO (Italy)
 - GEO-HF (Germany)
 - KAGRA (Japan)
 - LIGO-India



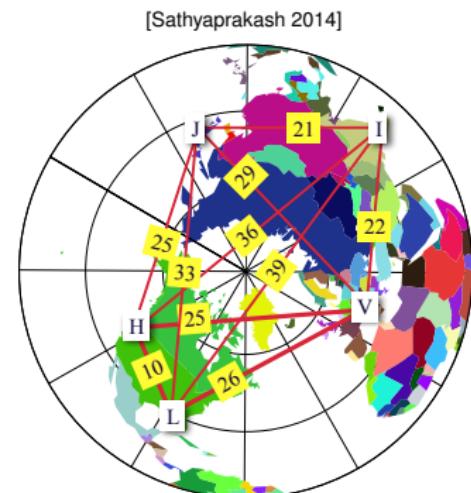
Expected NSNS Detection Rate

More than 10+ NSNS mergers detected per **week**

Numerical Relativity

Detector network by ≈ 2026

- LIGO A+ (Washington State)
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Expected NSNS Detection Rate

More than 10+ NSNS mergers detected per **week**

Solving Non-linear Elliptic Equations

Trevor Vincent

New Code for NB

Code Overview

Trevor Vincent

New Code for NR

Discontinuous Galerkin: Model Problem

Background

GW170817

Next Generation GW
Astronomy

Numerical Relativity

Chapter 1

New Code for NR

Test Problems

Two Punctures: Old
Code vs New Code

Two Punctures: Old
Code vs New Code

Random Three
Punctures

Future work

Chapter 2

Unequal Mass Binary
Neutron Star
Simulations

GRRHD

Ejecta Types

Dynamical Ejecta

Secular Ejecta

Velocity and Electron
Fraction

Neutrino Irradiation

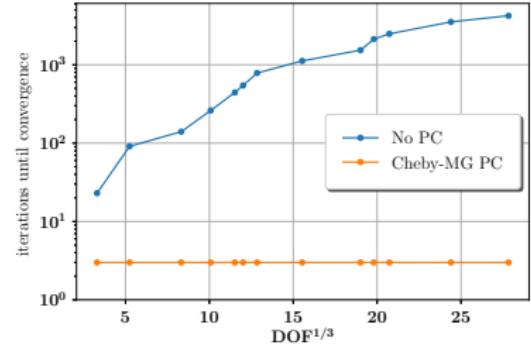
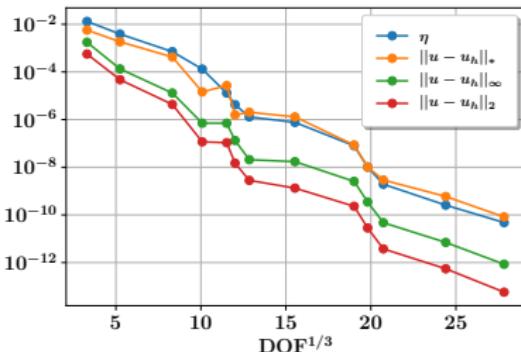
Neutrino Emission

Future work

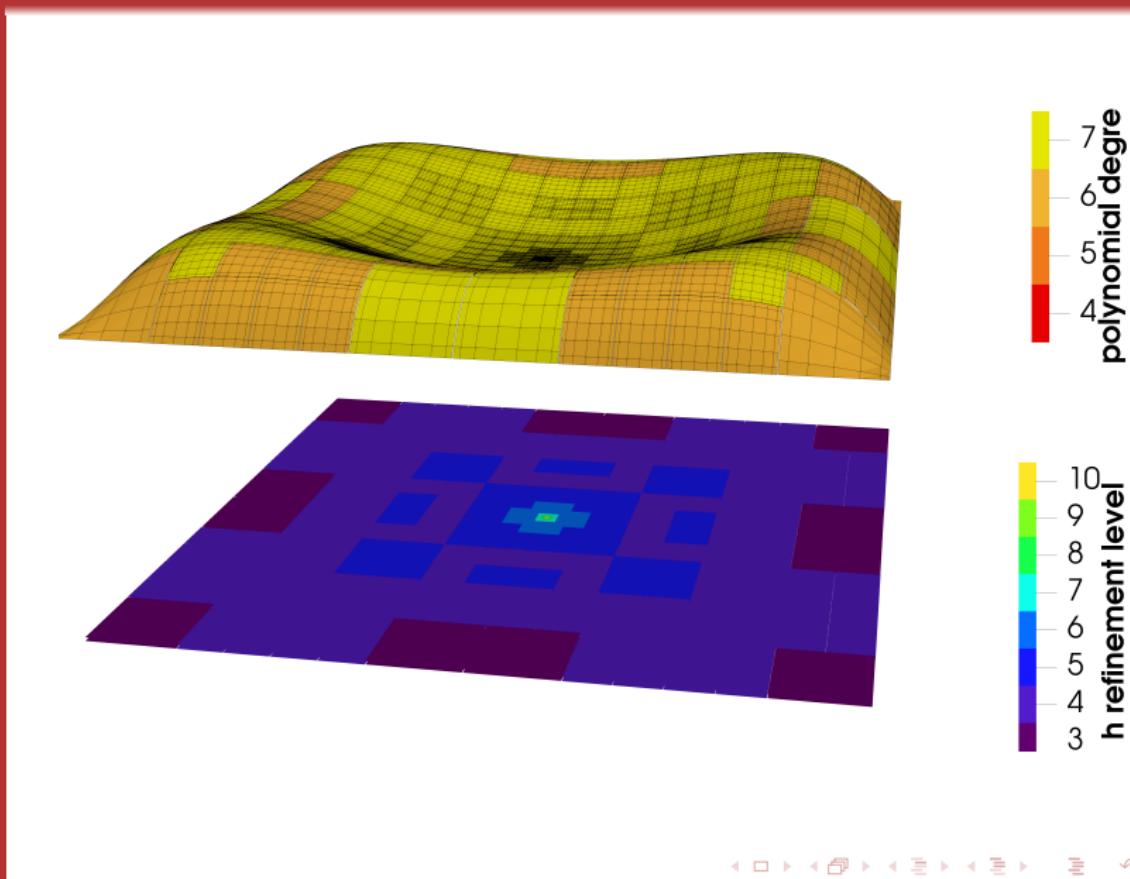
Test Problem 1: Single Non-smooth point

Test Problem Details

$$\begin{aligned} \nabla^2 u &= f \\ \Omega &= [0, 1]^2 \\ u &= 0 \quad x \in \partial\Omega \\ u &= x(1-x)y(1-y) \left[\left(x - \frac{1}{2}\right)^2 + \left(y - \frac{1}{2}\right)^2 \right]^{3/2}. \end{aligned}$$



Test Problem 1: Single Non-smooth point

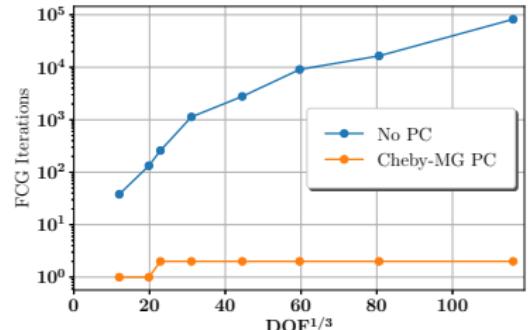
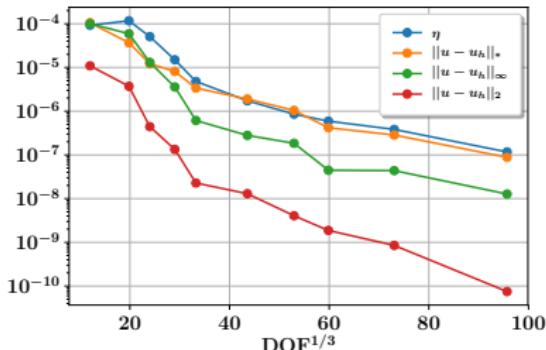


Test Problem 2: Constant Density Star

Test Problem Details

$$\nabla^2 \psi + 2\pi\rho \psi^5 = 0$$

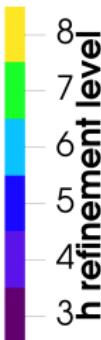
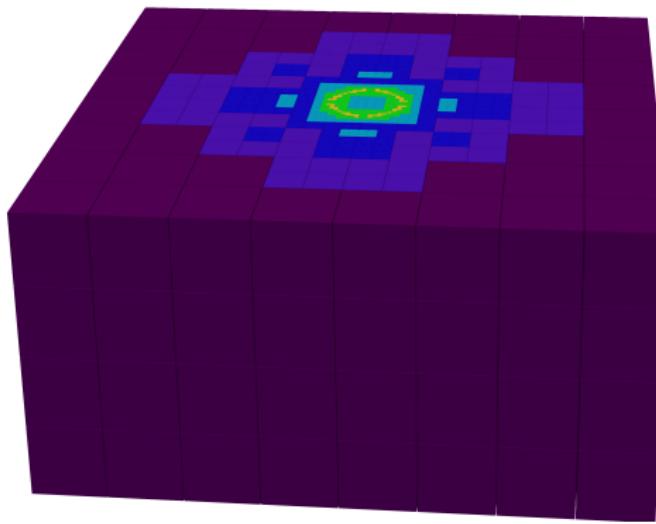
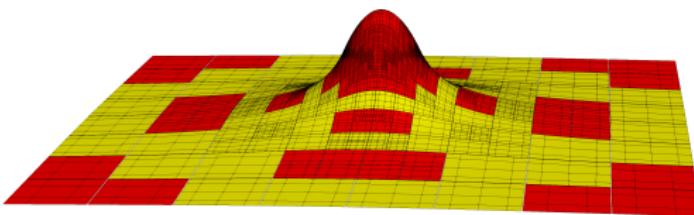
$$\rho = \begin{cases} \rho_0 & r \leq r_0 \\ 0 & r > r_0, \end{cases}$$



Test Problem 2: Constant Density Star

BNS simulations

Test Problems

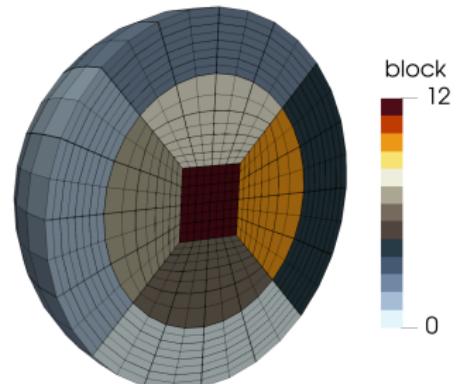
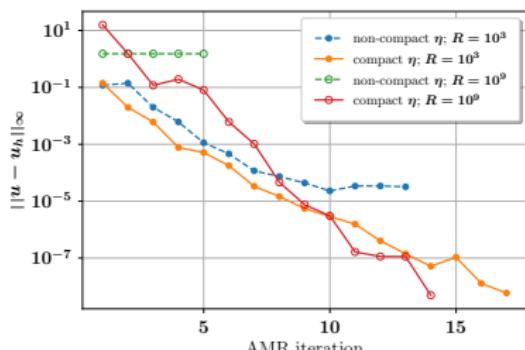


Test Problem 3: Cubed-spheres and Compactified grid

Lorentzian

$$-\nabla^2 u = f$$

$$u =$$

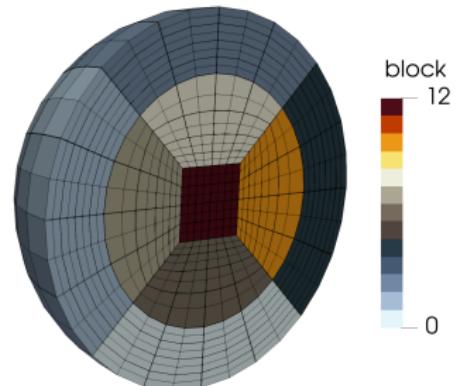
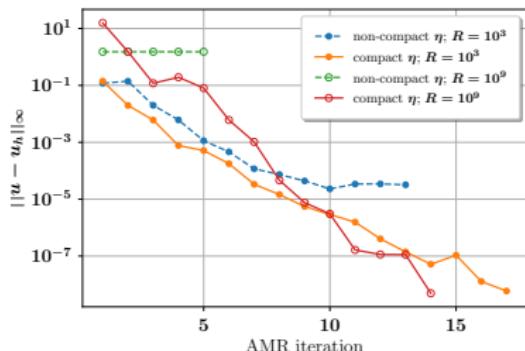
Mesh: Cubed Sphere with $R = 1000$ 

Test Problem 3: Cubed-spheres and Compactified grid

Lorentzian

$$-\nabla^2 u = f$$

$$u =$$

Mesh: Cubed Sphere with $R = 1000$ 

Two Punctures: Old Code vs New Code

Equal Mass Binary Black Hole Initial Data

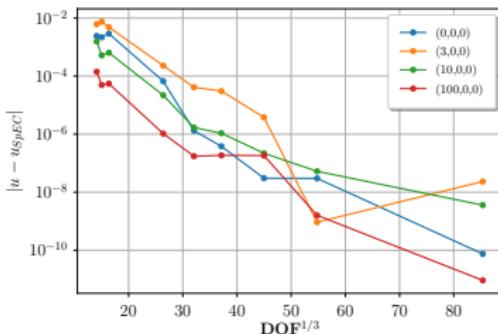
$$-\nabla^2 u = \frac{1}{8} \bar{A}^{ij} \bar{A}_{ij} \psi^{-7}$$

$$u = 0 \quad r = \infty$$

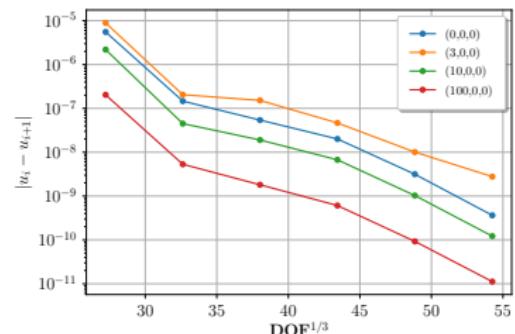
$$\vec{x}_\pm = (\pm 3, 0, 0) \quad \vec{P}_\pm = (0, \pm 2, 0)$$

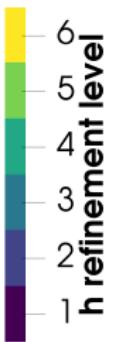
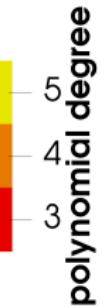
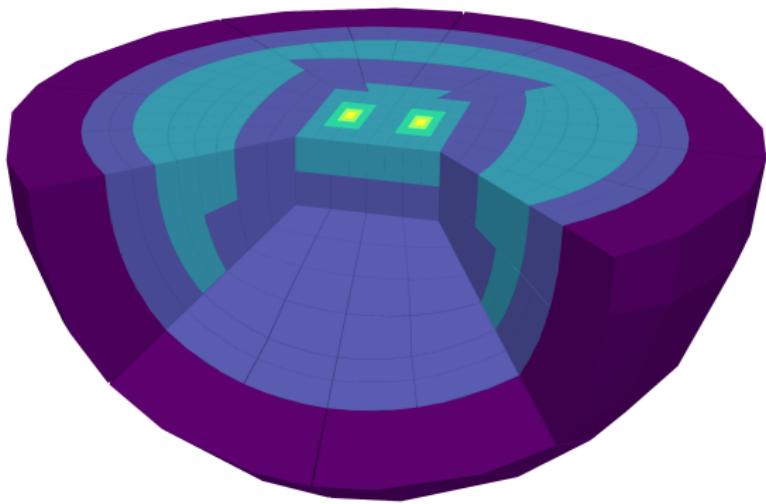
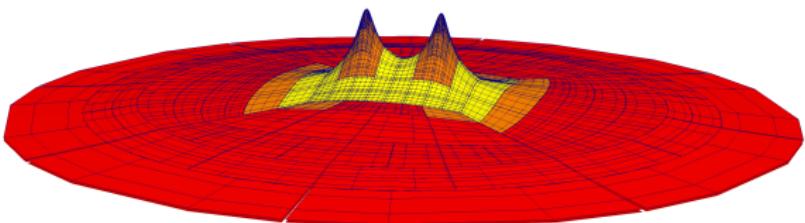
Mesh: Cubed Sphere with $R = 10^{11}$

[r4G]



[SpEC]





Random Three Punctures: New Code only

Background

GW170817

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New Code for NR

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Two Punctures: Old
Code vs New CodeTwo Punctures: Old
Code vs New CodeRandom Three
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Ejecta Types

Dynamical Ejecta

Secular Ejecta

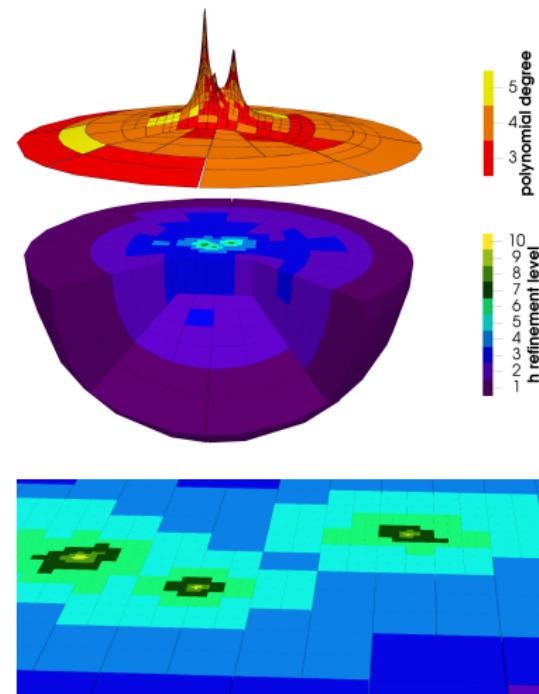
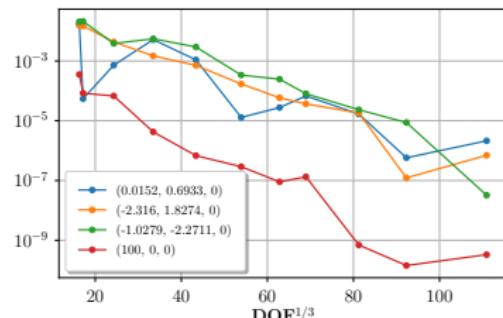
Velocity and Electron
Fraction

Neutrino Irradiation

Neutrino Emission

Future work

	Puncture 1	Puncture 2	Puncture 3
m	0.2691	0.4063	0.3245
x	0.0152	-2.316	-1.0279
y	-0.6933	1.8274	-2.2711
P_x	0.0585	-0.0284	0.1640
P_y	0.0082	-0.1497	0.0515
S_z	-0.0134	-0.0332	-0.0708



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General Relativistic Radiation-Hydrodynamics

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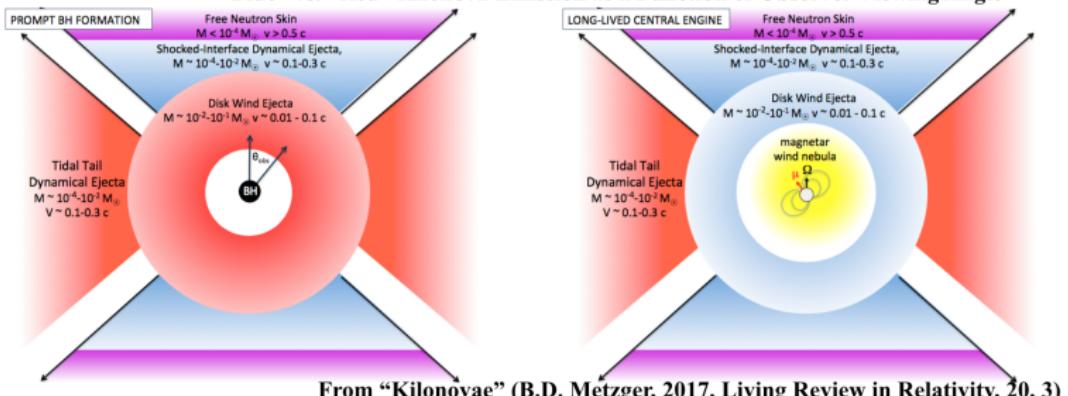
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Ejecta Types

“Blue” vs. “Red” Kilonova Emission as a Function of Observer Viewing Angle



From “Kilonovae” (B.D. Metzger, 2017, Living Review in Relativity, 20, 3)

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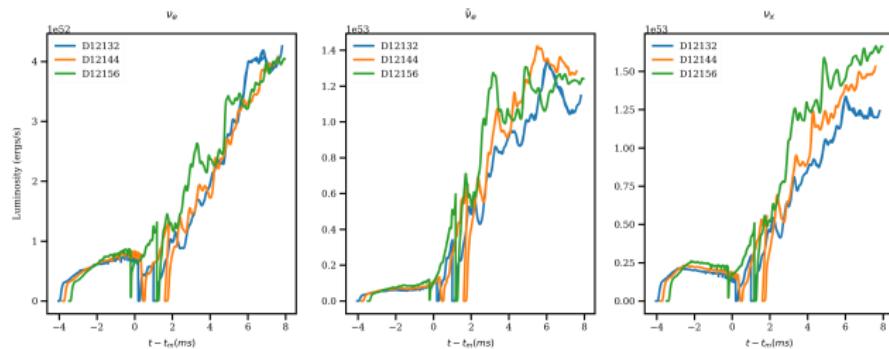
Neutrino Emission

Future work

Neutrino Emission

<divBNSNSNS!Simulations

Neutrino Emission



Future work

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