

Math 387 HW1

Trevor McCaffrey

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① Find all solutions to the system

$$\begin{cases} \textcircled{\text{I}} & x_1 + 2x_2 + 3x_3 = 8 \\ \textcircled{\text{II}} & x_1 - x_2 + 3x_3 = 5 \end{cases}$$

$$\textcircled{\text{I}} - \textcircled{\text{II}} \rightarrow 3x_2 = 3 \rightarrow x_2 = 1$$

$$\begin{cases} x_1 + 2 + 3x_3 = 8 \\ x_1 - 1 + 3x_3 = 5 \end{cases} \rightarrow \begin{cases} x_1 + 3x_3 = 6 \\ x_1 + 3x_3 = 6 \end{cases}$$

$$x_1 = 6 - 3x_3$$

$\Rightarrow$

$$x_1 = 6 - x_3$$

$$x_2 = 1$$

$$x_3 = x_3 \text{ (free)}$$