# Econ 690: Computational Economics/Numerical Methods

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### Fall 2023

## • Intro Matlab Files

- Lecture 2 Matlab Intro/MatlabIntro.m: Lecture file that introduces the various commands of Matlab.
- Lecture 2 Matlab Intro/GraphingExample: Lecture file that introduces three different ways to plot.
- Lecture 2 Matlab Intro/SampleFunction: Lecture file introduces an external function.

#### • Value Function Iteration

- Lecture 2 Matlab Intro/HelenofTroy: Lecture file that introduces "Helen of Troy" discrete
  choice, finite horizon stochastic Value Function Iteration. Similar to a VFI exercise on the value
  of an American Option.
- Lecture 2 Matlab Intro/CakeEating: Lecture file that introduces a "Cake Eating" problem: finite horizon deterministic problem on consuming finite natural resource.
- Lecture 2 Matlab Intro/CakeGrowth: Lecture file that introduces a "Cake Eating" problem
  with stochastic growth: finite horizon stochastic problem on consuming stochastically-growing
  natural resource.
- Lecture 4 VFI/VFI\_Intro\_Discrete: Runs the standard simple Neoclassical Growth Model value function iteration problem (discrete time, discrete choice, deterministic).
- Lecture 4 VFI/VFI\_Intro\_Continuous: Same as above, but with continuous choice.
- Lecture 4 VFI/VFI\_Cheb: Runs the standard simple Neoclassical Growth Model value function iteration problem (discrete time, discrete choice, deterministic) but using a Chebyshev Polynomial basis. Rather than using closed forms on Chebyshev nodes, it instead fits its cloud of points using least squares on a Chebyshev basis.
- Lecture 4 VFI/VFI\_polynomial.m: Runs the standard simple Neoclassical Growth Model value function iteration problem (discrete time, discrete choice, deterministic) but using a Chebyshev Polynomial basis. Rather than using closed forms on Chebyshev nodes, it instead fits its cloud of points using least squares on a Chebyshev basis.

## • Newton's Method

- Lecture 5 Newton's Method Mathematica (not Matlab) file NewtonsMethod.nb graphically shows Newton's Method on two 2-dimensional functions.
- Lecture 6 Newton's Method Applied/Lecture\_6\_NewtonsMethod\_DixitStiglitz.m
   Applies Newton's Method/derivative-based minimization (fsolve) to a "light" Dixit-Stiglitz general equilibrium model with constant elasticity of substitution aggregators.
- Lecture 6 Newton's Method Applied/Lecture\_6\_NewtonsMethod\_LinReg.m Applies
  Newton's Method/derivative-based minimization (fsolve) to a "light" Dixit-Stiglitz general equilibrium model with constant elasticity of substituion aggregators.

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- Lecture 6 - Newton's Method Applied/ZerosandMinimization.m Showcases the many equation solvers and minimizers available in matlab (including non-derivative based ones).

#### • Other Minimization Methods

- Lecture 7 Other Methods/ConjugateGradientMethod.m displays the conjugate-gradient
  method, useful when you don't want to take second derivatives but don't want to fall prey to the
  flaws of gradient descent.
- Lecture 7 Other Methods/GeneticAlgorithm.m displays Matlab's genetic algorithm, a
  "global" minimizer. Slow, but effective and can work with integer constraints, unlike most other
  methods.
- Lecture 7 Other Methods/DifferentialEvolution.m displays a differential-evolution based minimizer, comparable to the genetic algorithm.
- Lecture 7 Other Methods/NelderMead.m displays the "Nelder-Mead" simplex. Fast non-derivative based minimizer.
- Lecture 7 Other Methods/PatternSearch.m displays the "Pattern-Search" minimizer. Fast non-derivative based minimizer.
- Lecture 7 Other Methods/SimulatedAnnealing.m displays the "Simulated-Annealing" minimizer. Slow, and in my experience not great minimizer.

# • Interpolation

- Lecture 8 Interpolation/Bases.m Graphs out the first nine Monomial and Chebyshev Bases.
- Lecture 8 Interpolation/Simple\_Interpolation.m Displays simple interpolation commands and graphs them.
- Lecture 8 Interpolation/ChebyChev\_1D.m One-dimensional Chebyshev interpolation.
- Lecture 8 Interpolation/ChebyChev\_2D.m Two-dimensional Chebyshev interpolation.
- Lecture 8 Interpolation/Monom\_1D.m One-dimensional monomial/Taylor interpolation.
- Lecture 8 Interpolation/Monom\_2D.m Two-dimensional monomial/Taylor interpolation.

## • Reinforcement Learning

- Lecture 9 Reinforcement Learning/Discrete\_VFI/Discrete\_VFI.m Standard VFI, copied from the discrete choice example. Used for graphing comparison in RL.
- Lecture 9 Reinforcement Learning/Fitnet Example/Main.m Displays a neural network used for fitting (think highly flexible nonlinear least squares.)
- Lecture 9 Reinforcement Learning/NN\_Example/Simple\_5\_Main.m Shows a simple single-layer, 5 neuron network.
- Lecture 9 Reinforcement Learning/NN\_Example/Simple\_N\_Main.m Shows a simple single-layer, N-neuron network.
- Lecture 9 Reinforcement Learning/NN\_Example/Deep\_N\_Main.m Shows a deep-learning (2 layer)

N, N

-neuron network.

- Lecture 9 Reinforcement Learning/NN\_VFI/Actor\_Critic\_UpdateActor.m Shows the
  actor-critic updating algorithm (specifically, updating the actor step).
- Lecture 9 Reinforcement Learning/NN\_VFI/Main.m Uses the actor-critic algorithm to solve the standard neoclassical growth model.
- Lecture 9 Reinforcement Learning/NN\_VFI/myResetFunction.m Called by Main.m, resets the problem.

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 Lecture 9 - Reinforcement Learning/NN\_VFI/myStepFunction.m Called by Main.m, steps the problem forward in time.

- Sargent & Ljungqvist (1998)
  - Lecture 10 Sargent Ljungqvist/Sargent\_Ljungqvist.m Mostly (but not perfectly) replicates several figures in Sargent & Ljungqvist (1998).
- Neoclassical Growth Model
  - Lecture 11 NCG/NCG\_New//Main.m this file first calls the data cleaner, calibrates parameters, and solves the Neoclassical Growth Model.
  - Lecture 11 NCG/NCG\_New/focs\_NCGTrend.m. this file contains the first order conditions the Main.m file has to zero.
  - Lecture 11 NCG/NCG\_New/f\_Kstock.m this file contains two moments the initial capital stock/depreciation rate solver has to zero (calibrate initial capital stock+depreciation rate).
  - Lecture 11 NCG/NCG\_New/Data\_Preparation.m this file cleans the data and calibrates the moments.
- Computable General Equilibrium models
  - Lecture 12 CGE/HarbergerwESIdecisio.xlsx is an excel(!) file that solves the CGE model in Gallen & Mulligan 2018. Uses the Microsoft Excel derivative-based "solver" add-on.
- Generalized Method of Moments
  - Lecture 13 GMM/FittingFirmSize/Main\_Firm.m starts with a guess and calibrates the firm size model
  - Lecture 13 GMM/FittingFirmSize/Estimator\_Firm.m takes in parameter values, solves
    the general equilibrium model for firms & households (wages clear labor markets) and spits out
    moment error.
  - Lecture 13 GMM/MedicaidExample/Main\_Pref starts with a guess and calibrates the preference model
  - Lecture 13 GMM/MedicaidExample/Estimation\_Pref takes in parameter values, solves the household problem and returns moment errors.
- Simulation Estimation
- Dynamic Discrete Choice Estimation
- Markov Chain Monte Carlo
  - Lecture 16 MCMC/Metropolis\_Hastings.m
- Likelihoods and Filtering
  - Lecture 17 Likelihoods and Filtering/KalmanNew.m this file runs through a Kalman Filter and Kalman Smoother problem to filter out permanent income based on income+consumption data from a permanent income hypothesis style problem.
  - Lecture 17 Likelihoods and Filtering/Kalman.m this file straightforwardly applies the Kalman Filter to track a target whose movements are known with noise. (Basic Kalman problem)
  - Lecture 17 Likelihoods and Filtering/Kalman\_Lemma1.m this file simply shows the variance of x residual of control y  $var(x \hat{\beta}y)$  is equal to  $var(x) \frac{var(x)cov(xy)}{var(y)}$  (in matrix form). The most important fact for the Kalman filter (Kalman gain).
  - Lecture 17 Likelihoods and Filtering/Markov.m Markov Chain example with Bayesian updating.

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 Lecture 17 - Likelihoods and Filtering/Markov2.m Another Markov Chain example with Bayesian updating.

- Heterogeneous Agent Models
  - Lecture 18 Heterogeneous Agents/Krusell\_Smith.m. Application of the basic Krusell-Smith (1998) heterogeneous agents algorithm.