

# BANK RUNS

See Doepke, Lehnert, and Sellgren (1999) Ch. 17.4

Trevor Gallen

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- ▶ So we'll introduce a model of banks (and bank runs)

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- ▶ But there will be a big problem...what?
- ▶ Because of how banks are structured, they'll be vulnerable to **bank runs**

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- ▶ We'll tell a highly stylized story about turnips now.

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7. If you're still alive, you can eat your turnip



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  - ▶ “People are have diminishing returns to consumption/are risk averse”
  - ▶ “The second type is willing to wait if it gains her anything”

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- ▶ On your own, you get expected utility:
$$\theta \cdot \log(1) + (1 - \theta) \cdot \log(1.1) = 0.5 \cdot 0 + 0.98 + 0.5 \cdot 0.095 = 0.046702$$



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- ▶ We can all be better off by using insurance to smooth our consumption across states of the world

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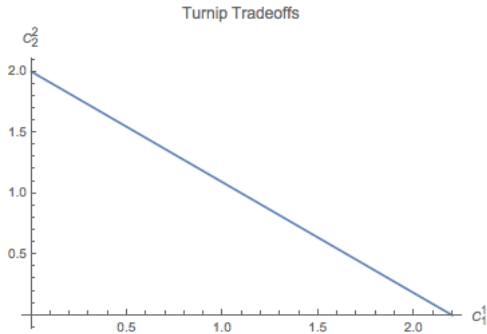
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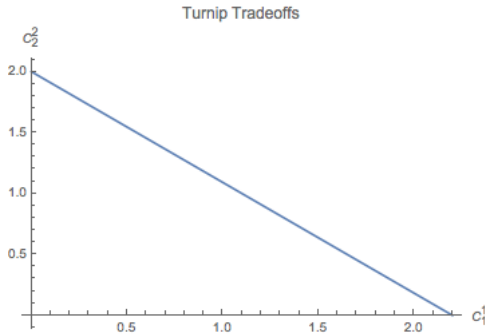
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- ▶ Let's graph this, with  $F = 1.1$  and  $\theta = 0.5$

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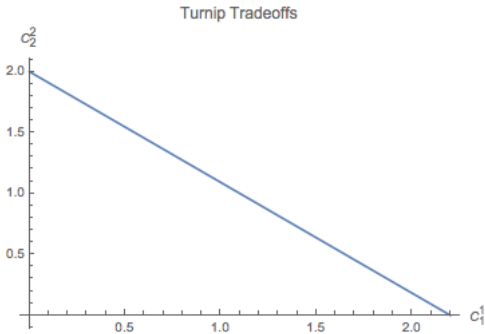


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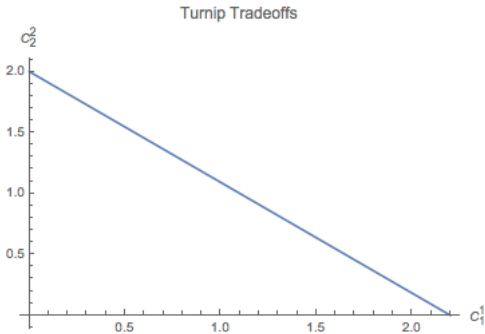
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- ▶ Or you could do something in the middle

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- ▶ Competition forces you to make the best decision for your population
- ▶ Let's write down the utility maximization problem

## INSURANCE UTILITY MAXIMIZATION

$$\mathcal{L}(c_1^1, c_2^2, \lambda) = \theta \log(c_1^1) + (1-\theta)Q \log(c_2^2) + \lambda \left( 1 - \theta c_1^1 - \frac{(1-\theta)c_2^2}{F} \right)$$

- ▶ Taking first order conditions, we get:

$$\frac{\partial \mathcal{L}}{\partial c_1^1} : \quad \frac{\theta}{c_1^1} - \lambda \theta = 0$$

$$\frac{\partial \mathcal{L}}{\partial c_2^2} : \quad Q \frac{1-\theta}{c_2^2} - \lambda \frac{1-\theta}{F} = 0$$

$$\frac{\partial \mathcal{L}}{\partial \lambda} : \quad \theta c_1^1 + \frac{(1-\theta)c_2^2}{F} = 1$$

- ▶ It's easy to solve these three equations for our three unknowns,  $c_1^1$ ,  $c_2^2$ , and  $\lambda$

## INSURANCE UTILITY SOLUTION

- Solving for  $c_1^1$ ,  $c_2^2$ , and  $\lambda$ , we get:

$$c_1^1 = \frac{1}{\theta + Q(1 - \theta)} \qquad c_2^2 = \frac{QF}{\theta + Q(1 - \theta)}$$

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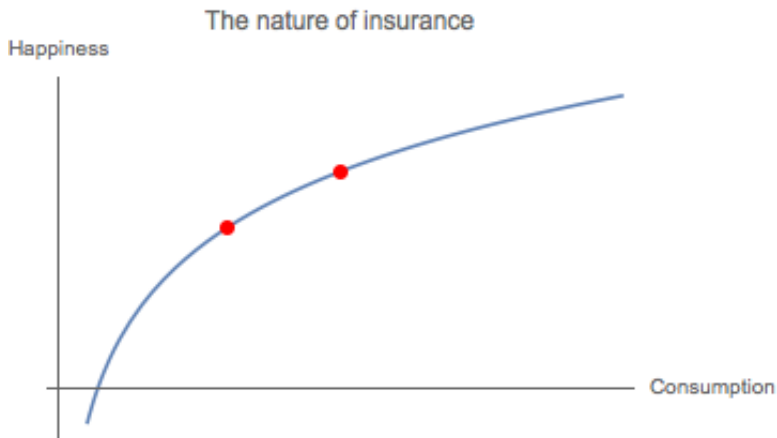
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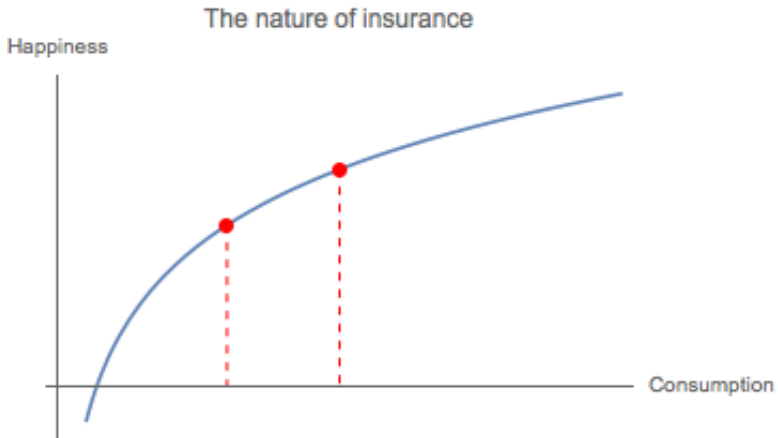
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- ▶ We did it! Improved utility slightly.

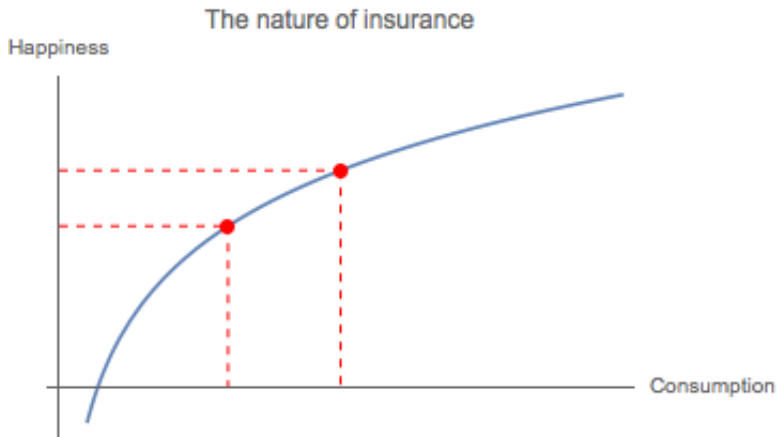
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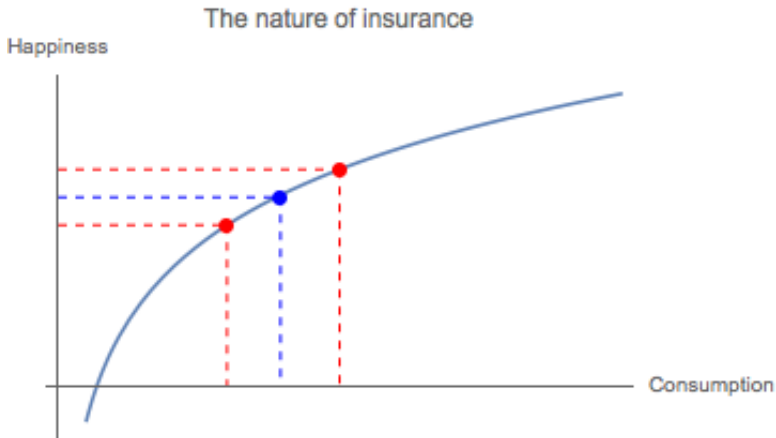
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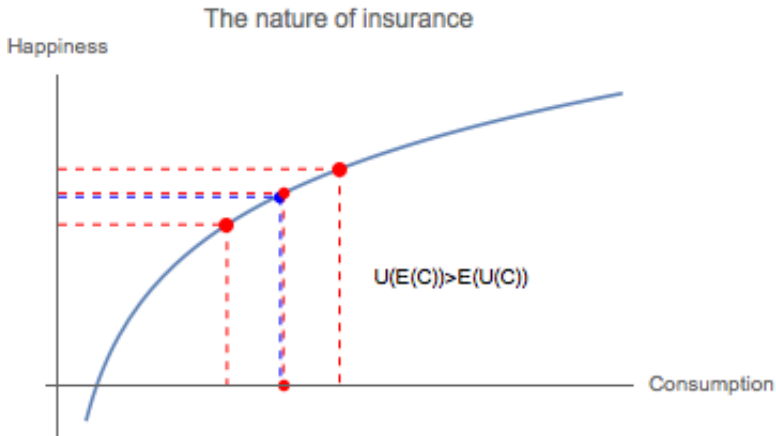
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Utility of expected consumption preferred to expectation of utility.

## INSURANCE PROBLEM: SUMMARY

- ▶ We have a problem in which people can invest and earn interest
- ▶ But sometimes some people want their money now
- ▶ Think of mortgages like planted turnips
- ▶ Banks will allow people to withdraw whenever
- ▶ People can benefit by participating in this “insurance” system, where we’re insuring your liquidity needs
- ▶ Now we’ll reframe this as a bank problem, but with one difference (what?)
  - ▶ People can withdraw at any time! (No proof of type)

## BANK PROBLEM

- ▶ Banks have the same problem as insurance companies, with a small twist:
  1. They'll make promises in period 0 about how much you can receive if you withdraw in period 1 or period 2
  2. They then have to keep those promises no matter how many people actually do withdraw in period 1
- ▶ The point:
  - ▶ If too many people withdrew in period 1, then there would be nothing left in period 2!
  - ▶ If I fear too many people are going to withdraw in period 1, then I'll withdraw in period 1 even if I'm of type 2
- ▶ Bank run!



## BANK PROBLEM

- ▶ Banks face the same basic problem: choose an interest rate  $r_1$  for type 1 and then whoever withdraws in period 2 gets the rest:

$$c_1^1 = 1 + r_1$$
$$c_2^2 = F \frac{1 - \theta(1 + r_1)}{1 - \theta}$$

- ▶ If for some reason  $\theta$ , the proportion that withdraw in period 1, is very high, then  $c_2^2$  goes down.
- ▶ If  $c_2^2$  ever slips below  $c_1^1$ , then all the type 2's should run on the bank.
- ▶ How should a bank choose  $r_1$ ?
- ▶ Maximize utility

## BANK MAXIMIZATION PROBLEM

- ▶ Banks must maximize consumer expected utility, plugging in for  $c_2^2$ :

$$\theta \log(1 + r_1) + (1 - \theta)Q \log \left( F \frac{1 - \theta(1 + r)}{1 - \theta} \right)$$

- ▶ You can notice that this is the exact same problem as the insurance company faced, with  $1 + r_1 = c_1$  and the budget constraint plugged in:
- ▶ Consequently, it has the same maximization solutions:

$$1 + r_1 = \frac{1}{\theta + Q(1 - \theta)}$$

- ▶ The bank chose the interest rate so everything is exactly the same as the insurance problem.
- ▶ If all goes according to plan, type 1 will get  $1.0\bar{1}$  and type 2 will get  $1.0\bar{8}$
- ▶ Type 2's won't want to run on the bank if nobody else is

## BANK RUNS

- ▶ What if for some reason I fear that too many people are withdrawing?
- ▶ Bank pays them out and I get the residual. I should get  $1.0\bar{8}$  if 50% of population withdraws
- ▶ What if 80% withdraws? Then I only get

$$c_2^2 = F \frac{1 - \theta(1 + r)}{1 - \theta} = 1.1 \frac{1 - 0.6 \cdot 1.0\bar{1}}{1 - 0.6} = 1.05$$

- ▶ Then I don't want to run
- ▶ What if 89% withdraws? Then I get:

$$c_2^2 = F \frac{1 - \theta(1 + r)}{1 - \theta} = 1.1 \frac{1 - 0.89 \cdot 1.0\bar{1}}{1 - 0.89} = 1.001$$

- ▶ If I fear that 89% of the population should withdraw, then I'll withdraw too!
- ▶ That means that (say) 90% of the population is withdrawing, the heat is turned up for others who aren't withdrawing
- ▶ Self-fulfilling Bank run!

## BANK RUNS: THE STORY

- ▶ If everyone is doing what they're supposed to, then there's no problem, everyone is happier and the economy is better than if there were no banks
- ▶ But if I *fear* too many people are withdrawing at once, then I should withdraw, creating a self-fulfilling bank run
- ▶ This happens because banks make promises that they are able to keep only when people think they're able to keep them
- ▶ Pro and con of banks:
  - ▶ On the one hand, they improve utility
  - ▶ On the other hand, they're vulnerable to bank runs
- ▶ Is there a way to avoid bank runs?

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  2. Deposit insurance
  3. Mutual funds
  4. Lender of last resort
- ▶ Let's talk about each in turn

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- ▶ This method fails if you don’t know  $\theta$  in advance! It would be a bad day for many of the type 1’s if the government declared that only 25% of the population can withdraw!

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- ▶ This method can be expensive, because it insures both *illiquid* and *insolvent* banks!

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- ▶ This method works, unless you decide that mutual funds really have promised implicitly (which is what happened in the financial crisis to MMMF's)



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- ▶ The possibility that they'll do this makes a run not happen
- ▶ This is called **Bagehot's Rule**: in times of crisis, lend without limit, to solvent firms, against good collateral, at high rates.

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- ▶ After 1913, we've had 2 (1 every  $\sim 50$  years)
- ▶ We know how to solve! Flood the system with liquidity.