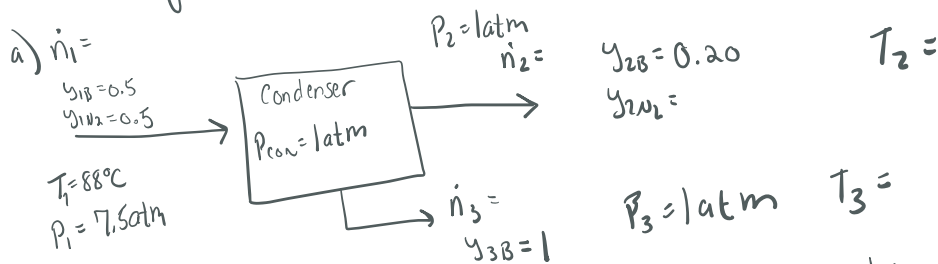


## Zippo Lighters



b) additional info:  $\dot{V}_1 = 1000 \text{ L/min}$ , the 1:1 ratio is incorporated in the PFD

Want to know:  $\dot{V}_2$ ,  $T_{\text{condenser}}$ ,  $\dot{V}_3$

- c)
- +3 unknowns ( $\dot{n}_1$ ,  $\dot{n}_2$ ,  $\dot{n}_3$ )
  - +0 chemical rxns
  - 2 independent material balances (B, N<sub>2</sub>)
  - 1 additional eq. ( $P_1 \dot{V}_1 = \dot{n}_1 R T_1 z$ )

0 DoF hooray! Can solve for all identified unknowns  $\dot{n}_1$ ,  $\dot{n}_2$ ,  $\dot{n}_3$

d) How to solve

1. Check if the inlet stream behaves ideally

$$\hat{V} = \frac{RT_1}{P} \quad \hat{V} = \frac{(0.0821 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(361 \text{ K})}{7.5 \text{ atm}} = 3.95, \quad \hat{V} < 5 \frac{\text{L}}{\text{mol}}$$

Cannot use ideal gas - must use the compressibility factor equation of state!

2. Need to read  $z$  from charts using  $T_r$ ,  $P_r$

This is a mixture so we need to calculate  $T_c'$  and  $P_c'$

$$T_r = \frac{T}{T_c}, \quad T_c' = y_{1B} T_{cB} + y_{1N_2} T_{cN_2} = 275.5 \text{ K}$$

$$P_r = \frac{P}{P_c}, \quad P_c' = y_{1B} P_{cB} + y_{1N_2} P_{cN_2} = 35.5 \text{ atm}$$

From table B.01

$$\left[ \begin{array}{l} T_{cB} = 425.17 \text{ K} \\ T_{cN_2} = 126 \text{ K} \\ P_{cB} = 37.47 \text{ atm} \\ P_{cN_2} = 33.5 \text{ atm} \end{array} \right.$$

Plugging it in ...  $T_r = \frac{361 \text{ K}}{275.5 \text{ K}}, \quad P_r = \frac{7.5 \text{ atm}}{35.5 \text{ atm}} \quad \boxed{z = 0.98}$

$T_r = 1.31, \quad P_r = 0.21$  ↗

3. After find 2, I would use  $P_1 \dot{V}_1 = z \dot{n}_1 R T_1$  to calculate  $\dot{n}_1$

Then, I would write the material balances:

$$N_2: y_{1N_2} \dot{n}_1 = \dot{n}_2 y_{2N_2} + 0$$

given

$$B: y_{1B} \dot{n}_1 = \dot{n}_2 y_{2B} + \dot{n}_3 y_{3B}$$

calculated

$$\text{total: } \dot{n}_1 = \dot{n}_2 + \dot{n}_3$$

4. solve  $N_2$  balance for  $\dot{n}_2$ .

5. solve total for  $\dot{n}_3$

6. Use  $\dot{n}_3$  to calculate  $\dot{V}_3$ . Stream 3 is a liquid, so I will use the  $\rho$  and MW.

$$\dot{V}_3 \left( \frac{L}{min} \right) = \frac{\dot{n}_3 \left( \frac{mol}{min} \right) \cdot MW_B \left( \frac{g}{mol} \right)}{\rho_{B,liq} \left( \frac{g}{L} \right)}$$

not in Table B.1,  
found it online  
from NIST chemical  
webbook

from Table  
B.1

$$MW_B = 58.12$$

$$\rho_{B,liq} = SG \cdot \rho_{H_2O}$$

$$SG = 0.60 \text{ g/mL}$$

Last - calculate  $T_{\text{condenser}}$ .

VLE and an ideal vapor in stream 2 (low pressure)  $\rightarrow$  Raoult's Law

$$y_{2B} P = x_{2B} P_B^{\text{sat}} \quad \text{and} \quad P_B^{\text{sat}} = 10^{\left[ A - \frac{B}{T+C} \right]}$$

$$\text{where } A = 6.82485$$

$$B = 943.453$$

$$C = 239.711$$

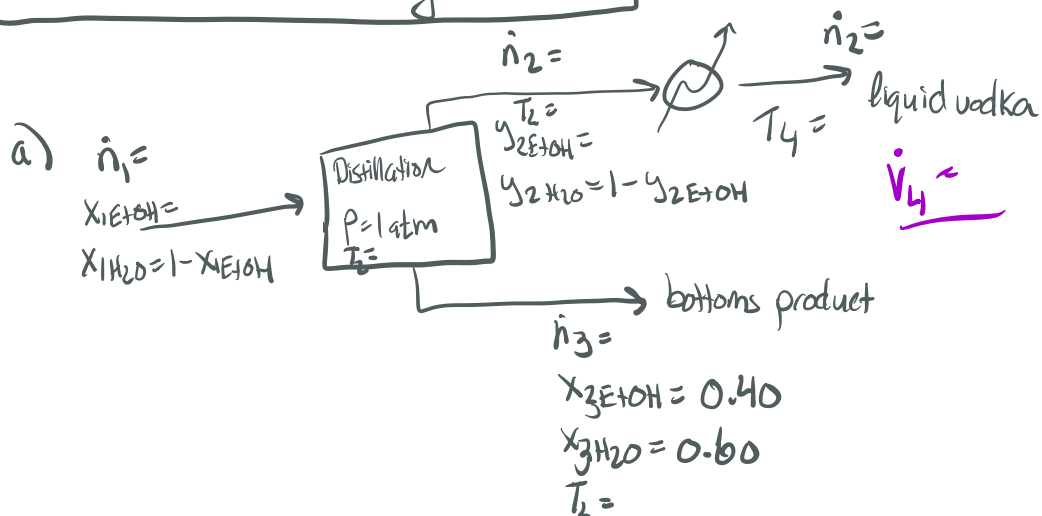
Table B.4

$$7. \text{ Convert } \frac{P_B^{\text{sat}} = 1 \text{ atm} \mid 760 \text{ mm Hg}}{1 \text{ atm}}$$

8. Plug  $P_B^{\text{sat}}$  into Antoine—solve for  $T_{\text{condenser}} (^{\circ}\text{C})$ .

Done! ☺

# Quantitative: Distilling Vodka



b)  $T_{\text{bub}}$  can be read directly from the  $T_{xy}$  diagram.

x-axis is  $x_{\text{H}_2\text{O}}, y_{\text{H}_2\text{O}}$

at  $x_{2\text{H}_2\text{O}} = 0.60$ ,  $T_{\text{bub}} = 81^\circ\text{C}$

at  $T = 81^\circ\text{C}$ ,  $y_{2\text{H}_2\text{O}} = 0.4$   
 $y_{2\text{EtOH}} = 0.6$

see  $T_{xy}$  diagram  
 below

c) at 90°C, what is the ABV?

$$ABV = \frac{V_{\text{ethanol}}}{V_{\text{vodka}}} = \frac{V_{\text{ethanol}}}{V_{\text{ethanol}} + V_{\text{H}_2\text{O}}} =$$

In order to calculate the  $V_{\text{ethanol}}$  and  $V_{\text{H}_2\text{O}}$  in the liquid condensate, we need to first know  $n_{\text{ethanol}}$  and  $n_{\text{H}_2\text{O}}$  for Stream 2. Just like we do for converting between mass and mole fractions, we can assume a basis:

$$\begin{array}{l} \text{calc mol EtOH} \rightarrow \text{g EtOH} \rightarrow V_{\text{EtOH}} \\ \text{calc mol H}_2\text{O} \rightarrow \text{g H}_2\text{O} \rightarrow V_{\text{H}_2\text{O}} \end{array} \quad \text{then} \quad \frac{V_{\text{EtOH}}}{V_{\text{H}_2\text{O}} + V_{\text{EtOH}}}$$

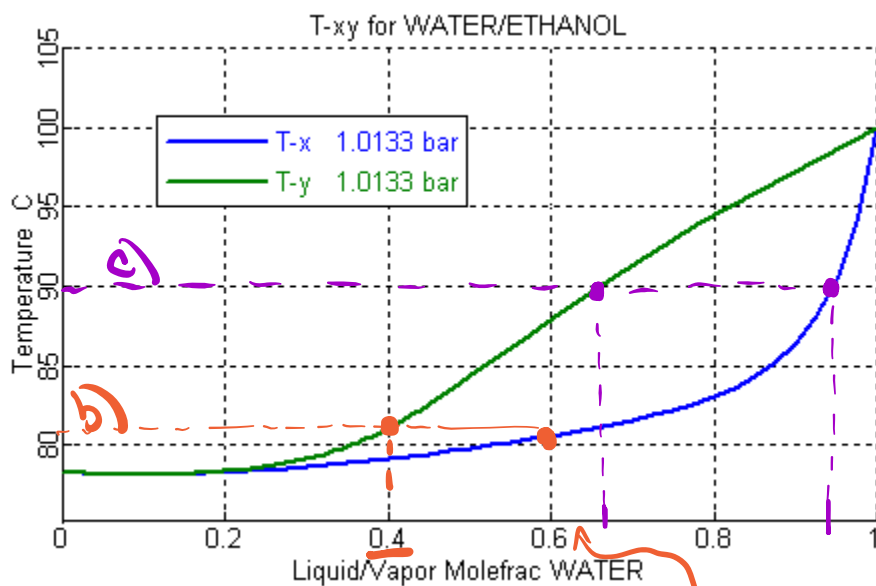
$$\begin{array}{c|c|c|c} 100 \text{ mol} & 0.35 \text{ mol EtOH} & 46.07 \text{ g} & \text{L EtOH} \\ \hline & \text{mol} & 1 \text{ mol EtOH} & 789 \text{ g EtOH} \end{array} = 2.3 \text{ L EtOH}$$

$$\begin{array}{c|c|c|c} 100 \text{ mol} & 0.65 \text{ mol H}_2\text{O} & 18.02 \text{ g} & \text{L H}_2\text{O} \\ \hline & \text{mol} & 1 \text{ mol H}_2\text{O} & 1800 \text{ g H}_2\text{O} \end{array} = 1.08 \text{ L H}_2\text{O}$$

$$ABV = \frac{2.3 \text{ L}}{2.3 \text{ L} + 1.08 \text{ L}}$$

$$ABV = 0.54$$

for context - this is  
54% alcohol, so 100  
proof vodka,  
ChemE in action!



$$x_{2\text{H}_2\text{O}} = 1 - x_{2\text{EtOH}} = 1 - 0.4 = 0.60$$

$$\text{and } y_{2\text{H}_2\text{O}} = 0.4$$

Q) If  $T = 90^{\circ}\text{C}$  and  $\dot{V}_y = 1 \text{ L/hour}$ . How much feed solution do you need?  
 $P_2 = 1 \text{ atm}$

According to Txy ...  $y_{2\text{H}_2\text{O}} = 0.65$   $x_{3\text{H}_2\text{O}} = 0.95$   
 \* can use  $\dot{n}_2$  to calculate  $\dot{V}_y$  (moles of liq  $\rightarrow$  volume),  $\rho_{\text{EtOH}} =$   
 $MW_{\text{EtOH}} =$

3 unknowns ( $\dot{n}_1$ ,  $x_{1\text{EtOH}}$ ,  $\dot{n}_3$ )

- 2 independent material balances (EtOH, H<sub>2</sub>O)

0 additional equations

1 DOF

\* Not enough info to solve! We already used Raoult's law (via Txy diagram). Need  $\dot{n}_1$ ,  $\dot{n}_2$