

## Contents

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```
%%Prelab6c
M = 0.94;
m = 0.23;
Lp = 0.3302;
r = 6.36*10^-3;
Rm = 2.6;
Kt = 7.67*10^-3;
Km = 7.67*10^-3;
Kg = 3.71;
Jm = 3.9*10^-7;
g = 9.81;

a = M*r^2*Rm + Kg^2*Jm*Rm;
b = Kg^2*Kt*Km;
c = Kg*Kt*r;
d = M + m/4;
e = M*c;
f = M*b;

a12 = 1;

a22 = -f/d/a;
a23 = -3/4*m*g/d;
b2 = e/d/a;

a34 = 1;

a42 = f/(4/3*Lp)/d/a;
a43 = 3/4*g/Lp + 3/4*m*g/d/(4/3*Lp);
b4 = -e/(4/3*Lp)/d/a;
```

```
A = [0 a12 0 0;
      0 a22 a23 0;
      0 0 0 a34;
      0 a42 a43 0];
B = [0; b2; 0; b4];
C = [1 0 0 0;
      0 0 1 0];
D = 0;
```

`evals_ref = [-2+10i -2-10i -1.6+1.3i -1.6-1.3i]; poly_ref = [1 7.2 121.05 349.8 442]; K = place(A,B,evals_ref); Ak = A-B*K; Bk = B*K;`

```
%K_lab = [-12.9796 -14.723 -47.8456 -6.5363];
```

```
P = [-10+15j -10-15j -12+17j -12-17j]; % eig of (A-LC) = eig of (A' - C'*L') I = place(A',C',P); L = I'; CL = L*C;
```

### 3.1

```
%dim Q = 4x4 because x is 4x1. dim R = 1x1 because u is 1x1
ref = [0 0 0 0];
x0 = 0.3;
a0 = 0.05;
ic = [0.3 0 0.05 0];
q2 = 0;
q4 = 0;
disp('case1: nominal');
q1 = 1;
q3 = 1;
r = 1;
q1_n = q1/x0^2;
q3_n = q3/a0^2;
r_n = r/6^2;

Q = [q1_n 0 0 0;
     0 0 0 0;
     0 0 q3_n 0;
     0 0 0 0];
R = r_n;

[K,S,E] = lqr(A,B,Q,R);
Ak = A-B*K;
Bk = B*K;
disp(['The K values are;',num2str(K)])
disp(['The eigen values/CL poles are;',num2str(E)])

%%make observer poles far from CL poles (6 times)
P = 6*E';
l = place(A',C',P);
L = l';
Cl = L*C;

sim('pl6c')

x = x';
y = C*x;
y = y';
r_x_h = r_x_h';
u = K*r_x_h;
u = u';
disp(['max position deviation is:', num2str(max(abs(y(:,1))))])
disp(['max angle deviation is:', num2str(max(abs(y(:,2))))])
disp(['max abs control is:', num2str(max(abs(u))))];

figure;
plot(t,y(:,1),t,u,'-.');
legend('position','control');
xlabel('time (s)');
title('position (m) and control (V)');
xlim([0 2]);
```

```
figure;
plot(t,y(:,2),t,u,'-.');
legend('angle','control');
xlabel('time (s)');
title('angle (rad) and control (V)');
xlim([0 2]);
```

case1: nominal

The K values are;-20          -29.39458          -155.0089          -20.4077

The eigen values/CL poles are;-15.2514-13.5564i

-15.2514+13.5564i

-0.948735-

0.84726i          -0.948735+0.84726i

L =

1.0e+03 \*

0.1058      -0.0037

2.0971      0.1145

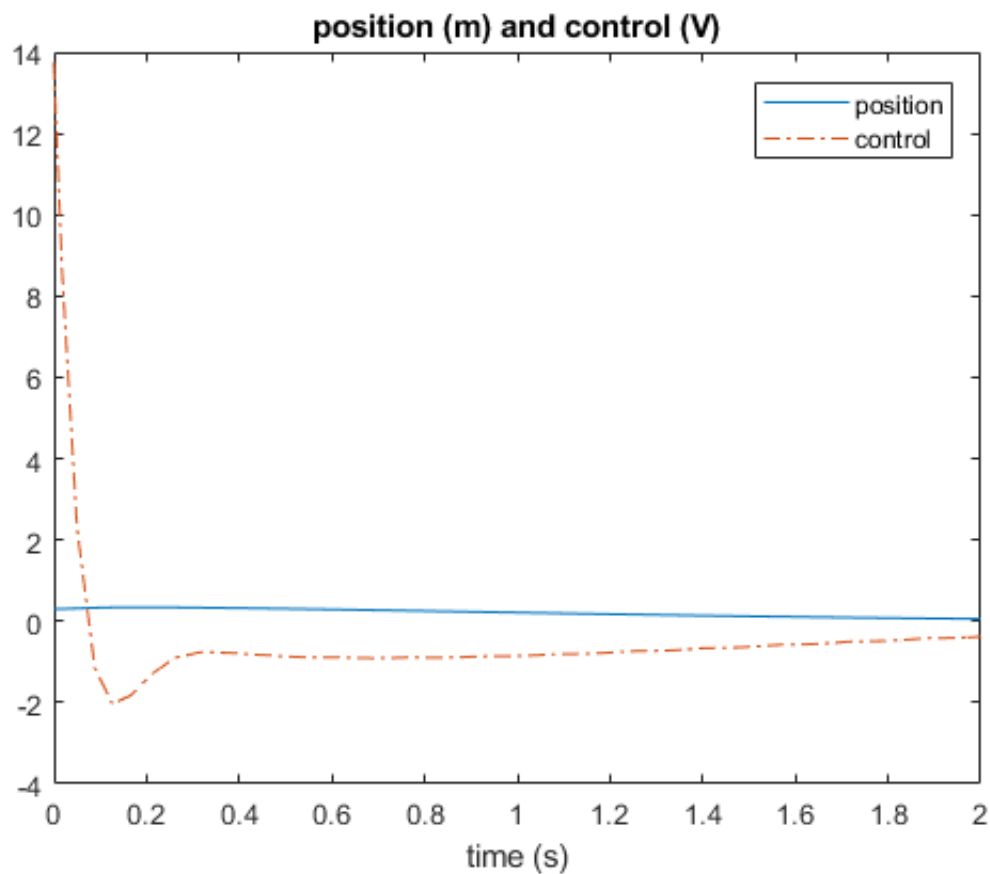
1.2833      0.0818

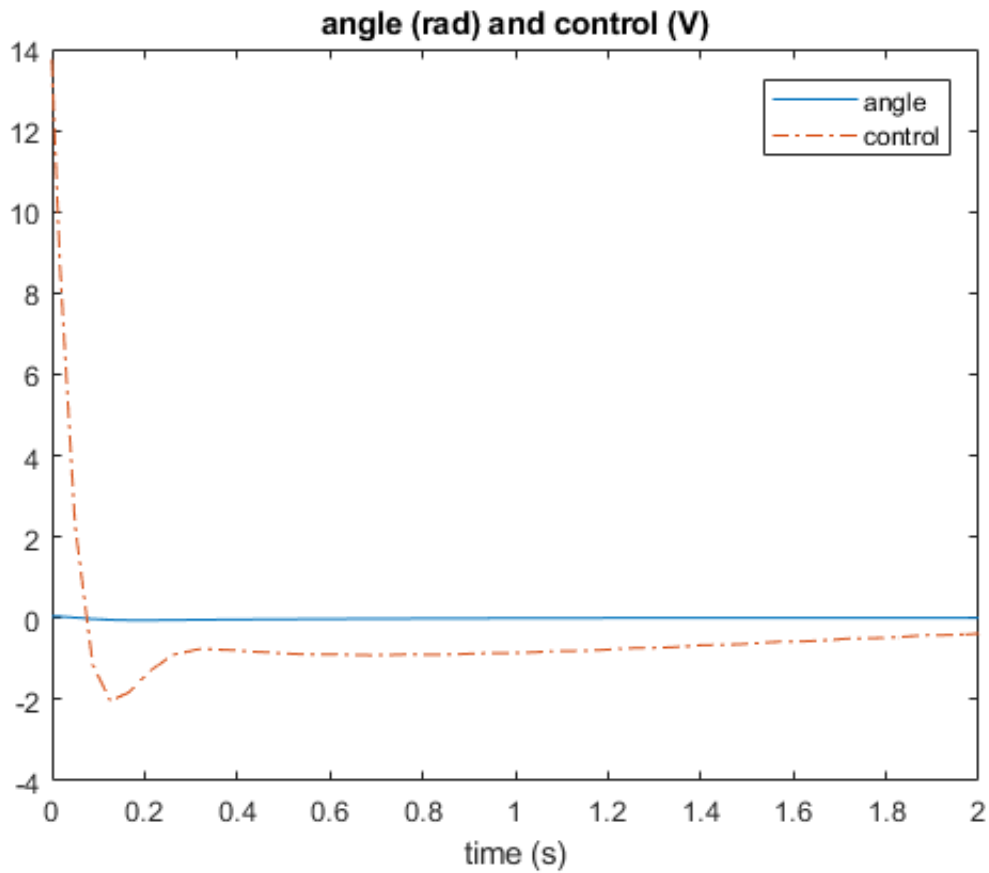
6.0063      0.4224

max position deviation is:0.34527

max angle deviation is:0.05

max abs control is:13.7504





## 3.2

```
%%case2
disp('case2: q3 = 0.01 << 1');
q1 = 1;
q3 = 0.01;
r = 1;
q1_n = q1/x0^2;
q3_n = q3/a0^2;
r_n = r/6^2;

Q = [q1_n 0 0 0;
      0 0 0 0;
      0 0 q3_n 0;
      0 0 0 0];
R = r_n;
[K,S,E] = lqr(A,B,Q,R);
Ak = A-B*K;
Bk = B*K;
disp(['The K values are;',num2str(K)])
disp(['The eigen values/CL poles are;',num2str(E')])

sim('pl6c')

x = x';
y = C*x;
y = y';
r_x_h = r_x_h';
u = K*r_x_h;
```

```

u = u';

disp(['max position deviation is:', num2str(max(abs(y(:,1))))])
disp(['max angle deviation is:', num2str(max(abs(y(:,2))))])
disp(['max abs control is:', num2str(max(abs(u))))];
%small q3 gives bigger change in x and theta but smaller control

figure;
plot(t,y(:,1),t,u,'-.');
legend('position','control');
xlabel('time (s)');
title('position (m) and control (V)');

figure;
plot(t,y(:,2),t,u,'-.');
legend('angle','control');
xlabel('time (s)');
title('angle (rad) and control (V)');

%%case3
disp('case3: q3 = 100 >> 1');
q1 = 1;
q3 = 100;
r = 1;
q1_n = q1/x0^2;
q3_n = q3/a0^2;
r_n = r/6^2;

Q = [q1_n 0 0 0;
      0 0 0 0;
      0 0 q3_n 0;
      0 0 0 0];
R = r_n;
[K,S,E] = lqr(A,B,Q,R);
Ak = A-B*K;
Bk = B*K;
disp(['The K values are:',num2str(K)])
disp(['The eigen values/CL poles are:',num2str(E)])

sim('pl6c')

x = x';
y = C*x;
y = y';
r_x_h = r_x_h';
u = K*r_x_h;
u = u';

disp(['max position deviation is:', num2str(max(abs(y(:,1))))])
disp(['max angle deviation is:', num2str(max(abs(y(:,2))))])
disp(['max abs control is:', num2str(max(abs(u))))];
%big q3 gives smaller change in x and same in theta but bigger control

figure;
plot(t,y(:,1),t,u,'-.');
legend('position','control');
xlabel('time (s)');

```

```

title('position (m) and control (V)');

figure;
plot(t,y(:,2),t,u,'-.');
legend('angle','control');
xlabel('time (s)');
title('angle (rad) and control (V)');

%%case4
disp('case4: r = 0.01 << 1');
q1 = 1;
q3 = 1;
r = 0.01;
q1_n = q1/x0^2;
q3_n = q3/a0^2;
r_n = r/6^2;

Q = [q1_n 0 0 0;
      0 0 0 0;
      0 0 q3_n 0;
      0 0 0 0];
R = r_n;
[K,S,E] = lqr(A,B,Q,R);
Ak = A-B*K;
Bk = B*K;
disp(['The K values are;',num2str(K)])
disp(['The eigen values/CL poles are;',num2str(E)])

sim('pl6c')

x = x';
y = C*x;
y = y';
r_x_h = r_x_h';
u = K*r_x_h;
u = u';

disp(['max position deviation is:', num2str(max(abs(y(:,1))))])
disp(['max angle deviation is:', num2str(max(abs(y(:,2))))])
disp(['max abs control is:', num2str(max(abs(u))))];
%small r gives slightly smaller change in x and slightly bigger change in theta but bigger co
ntrol

figure;
plot(t,y(:,1),t,u,'-.');
legend('position','control');
xlabel('time (s)');
title('position (m) and control (V)');

figure;
plot(t,y(:,2),t,u,'-.');
legend('angle','control');
xlabel('time (s)');
title('angle (rad) and control (V)');

%%case5
disp('case5: r = 100 >> 1');

```

```

q1 = 1;
q3 = 1;
r = 100;
q1_n = q1/x0^2;
q3_n = q3/a0^2;
r_n = r/6^2;

Q = [q1_n 0 0 0;
      0 0 0 0;
      0 0 q3_n 0;
      0 0 0 0];
R = r_n;
[K,S,E] = lqr(A,B,Q,R);
Ak = A-B*K;
Bk = B*K;
disp(['The K values are;',num2str(K)])
disp(['The eigen values/CL poles are;',num2str(E')])

sim('pl6c')

x = x';
y = C*x;
y = y';
r_x_h = r_x_h';
u = K*r_x_h;
u = u';

disp(['max position deviation is:', num2str(max(abs(y(:,1))))])
disp(['max angle deviation is:', num2str(max(abs(y(:,2))))])
disp(['max abs control is:', num2str(max(abs(u))))];
%big r gives slightly smaller change in x and same theta but smaller control

figure;
plot(t,y(:,1),t,u,'-.');
legend('position','control');
xlabel('time (s)');
title('position (m) and control (V)');

figure;
plot(t,y(:,2),t,u,'-.');
legend('angle','control');
xlabel('time (s)');
title('angle (rad) and control (V)');

```

```

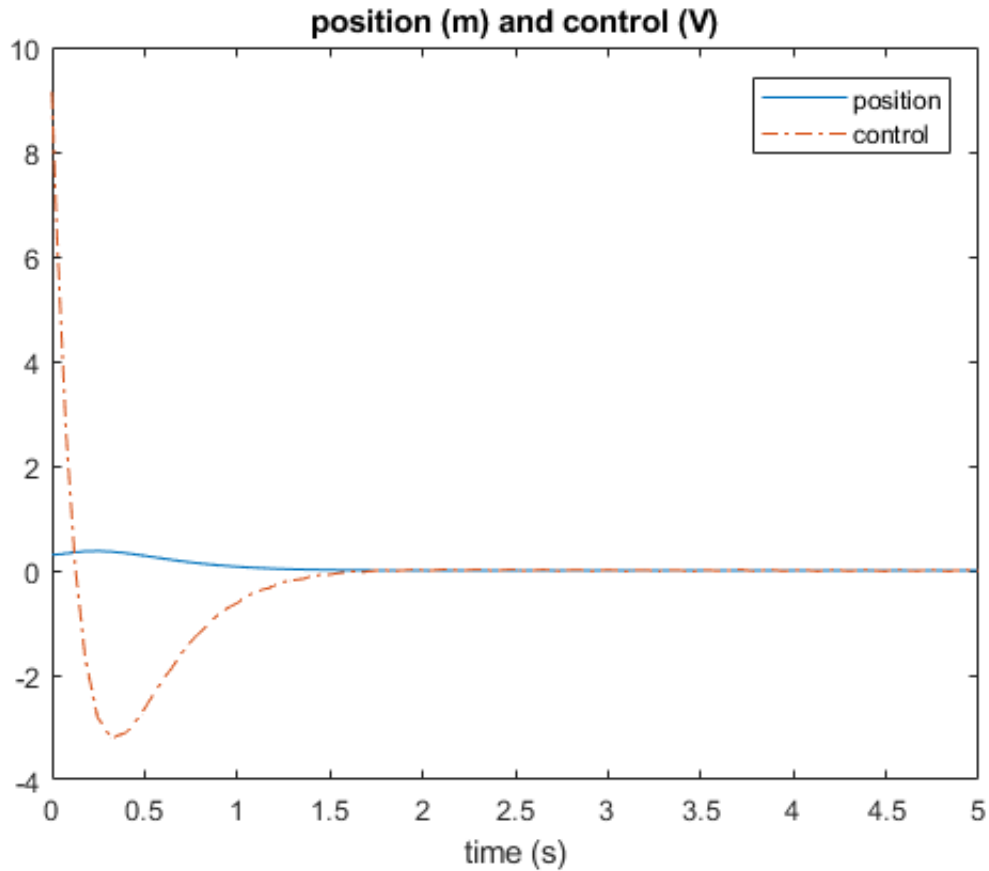
case2: q3 = 0.01 << 1
The K values are;-20      -20.1536      -62.9958      -12.8567
The eigen values/CL poles are;-7.2972-3.2902i      -7.2972+3.2902i      -2.9239-1.401
6i      -2.9239+1.4016i
max position deviation is:0.3718
max angle deviation is:0.11963
max abs control is:9.1498
case3: q3 = 100 >> 1
The K values are;-20      -75.269428      -1231.8874      -57.932371
The eigen values/CL poles are;-45.6609-45.121i      -45.6609+45.121i      -0.287533-0.
284266i      -0.287533+0.284266i

```

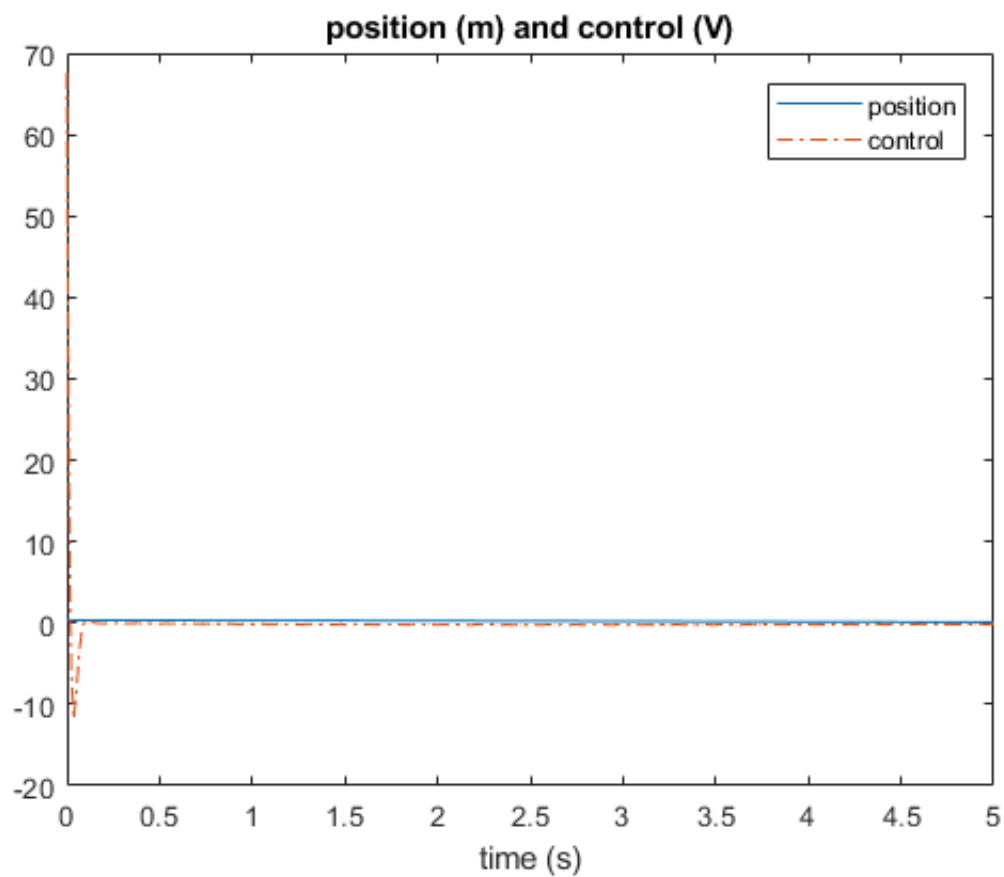
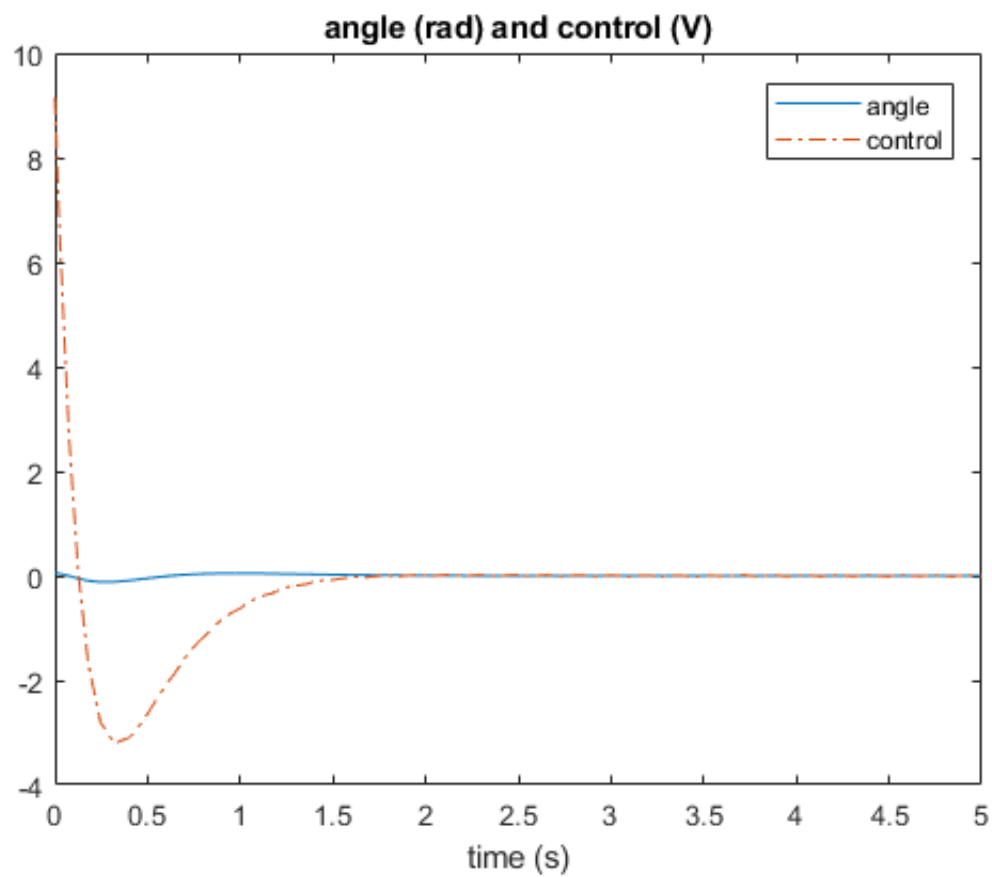
```

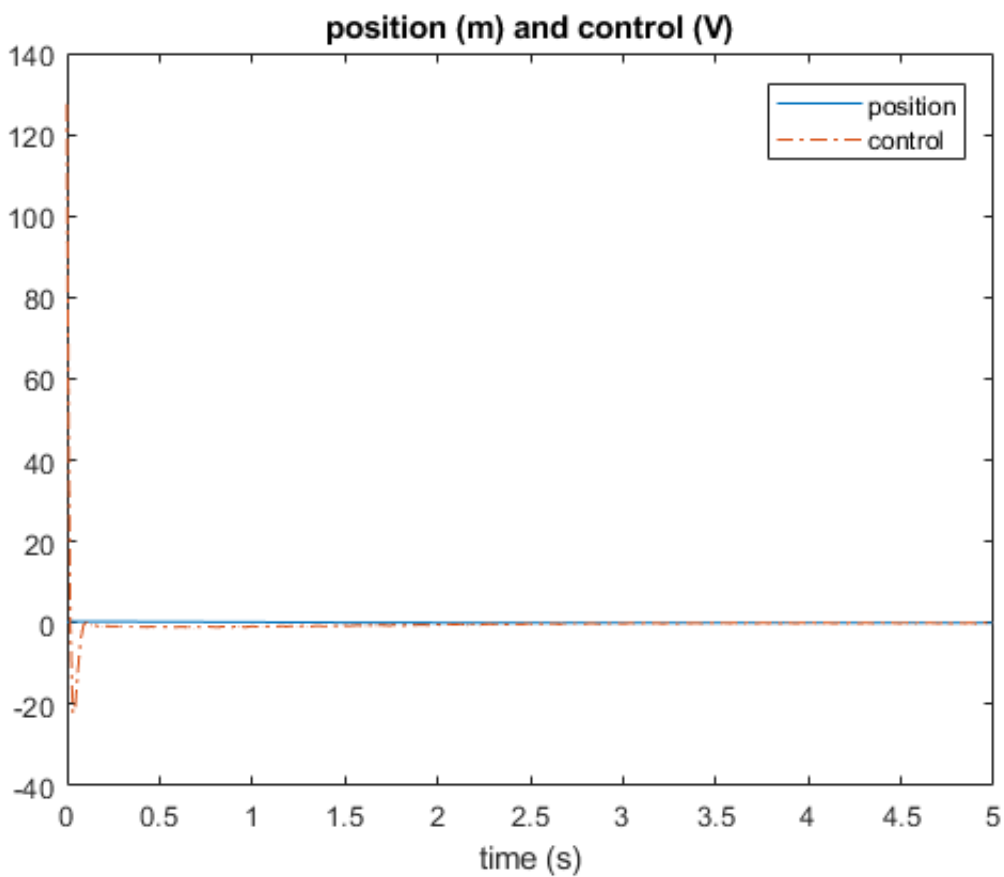
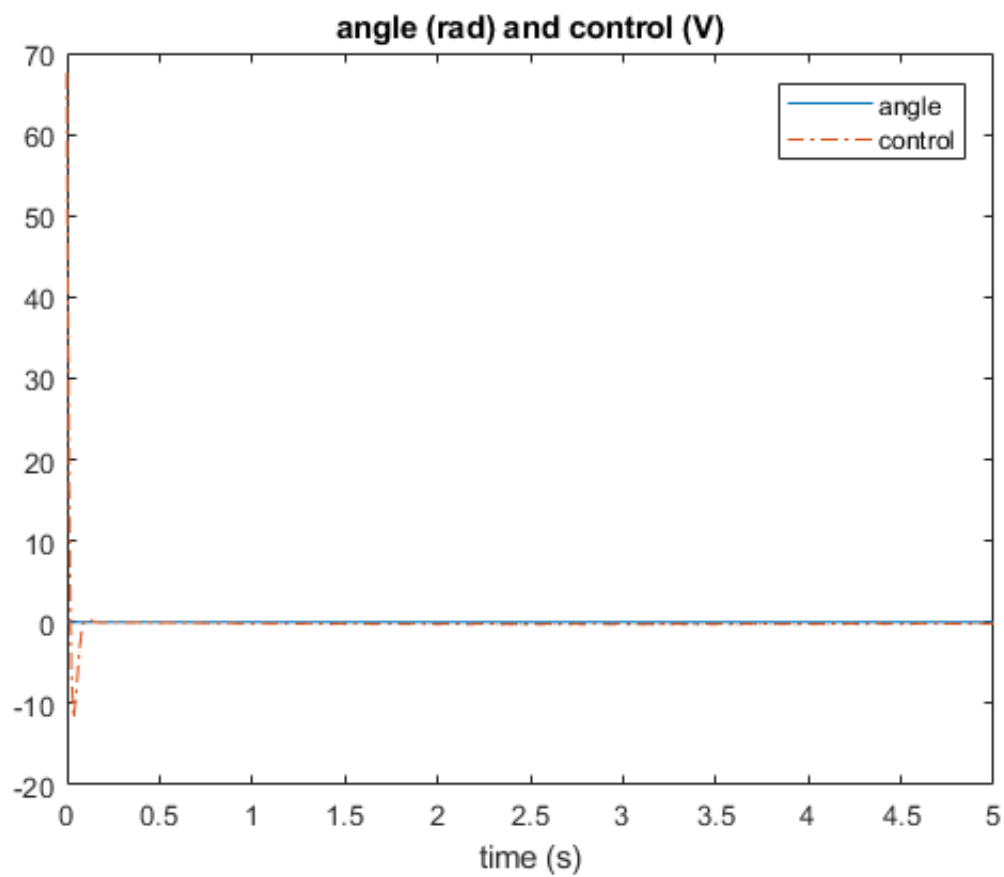
max position deviation is:0.32615
max angle deviation is:0.05
max abs control is:67.5944
case4: r = 0.01 << 1
The K values are;-200      -238.4112      -1349.2888      -130.17026
The eigen values/CL poles are;-45.7202-45.1824i      -45.7202+45.1824i      -0.935536-0
.869056i      -0.935536+0.869056i
max position deviation is:0.34633
max angle deviation is:0.054905
max abs control is:127.4644
case5: r = 100 >> 1
The K values are;-2      -10.208      -39.1463      -7.63995
The eigen values/CL poles are;-7.3602-2.851i      -7.3602+2.851i      -2.3926+0
i      -0.45194+0i
max position deviation is:0.34989
max angle deviation is:0.05
max abs control is:2.5573

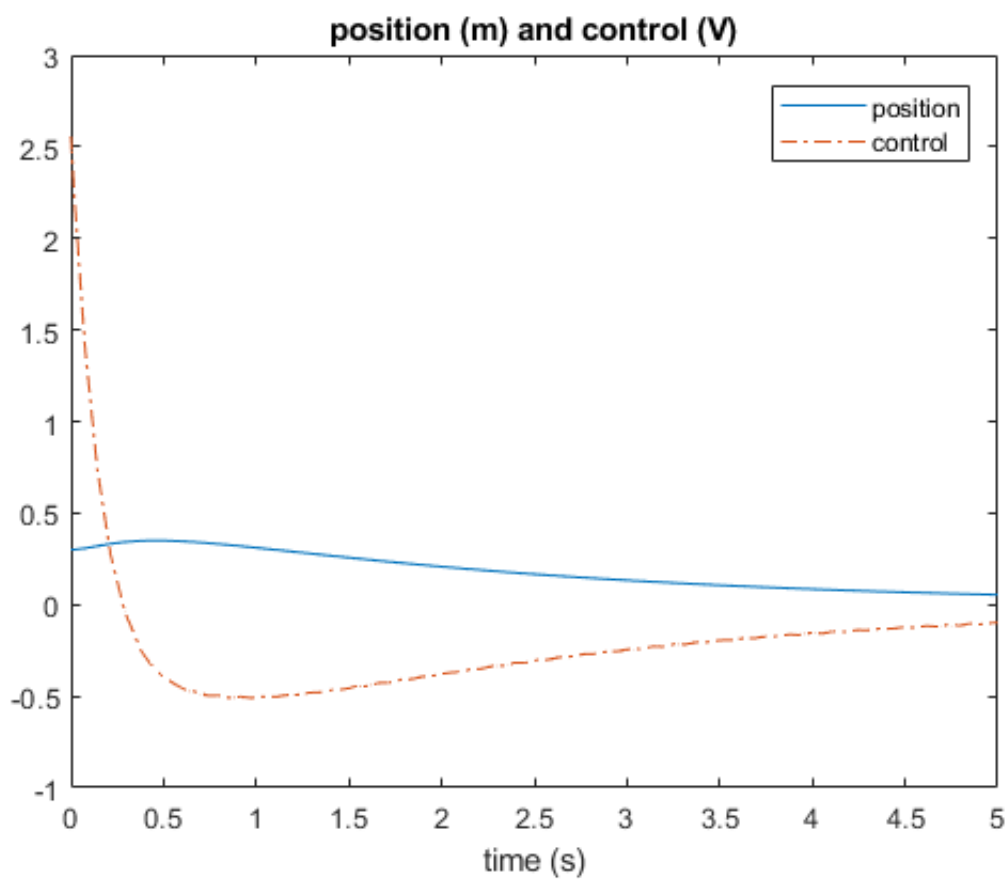
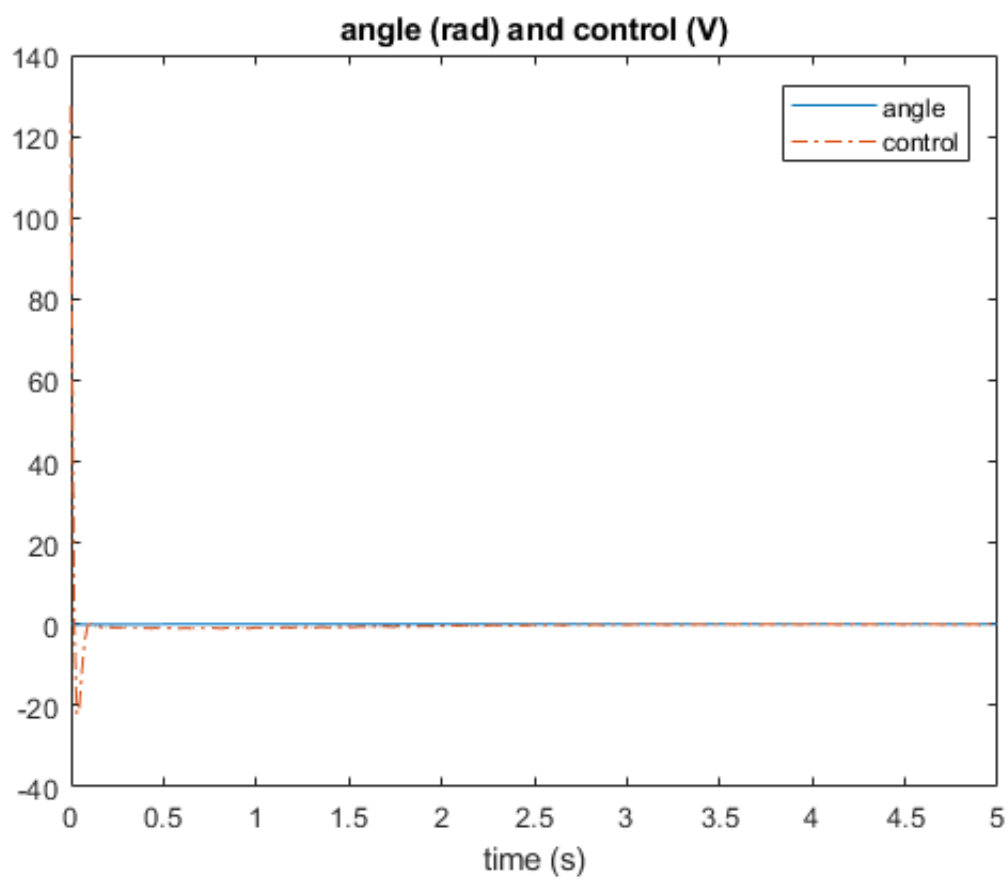
```

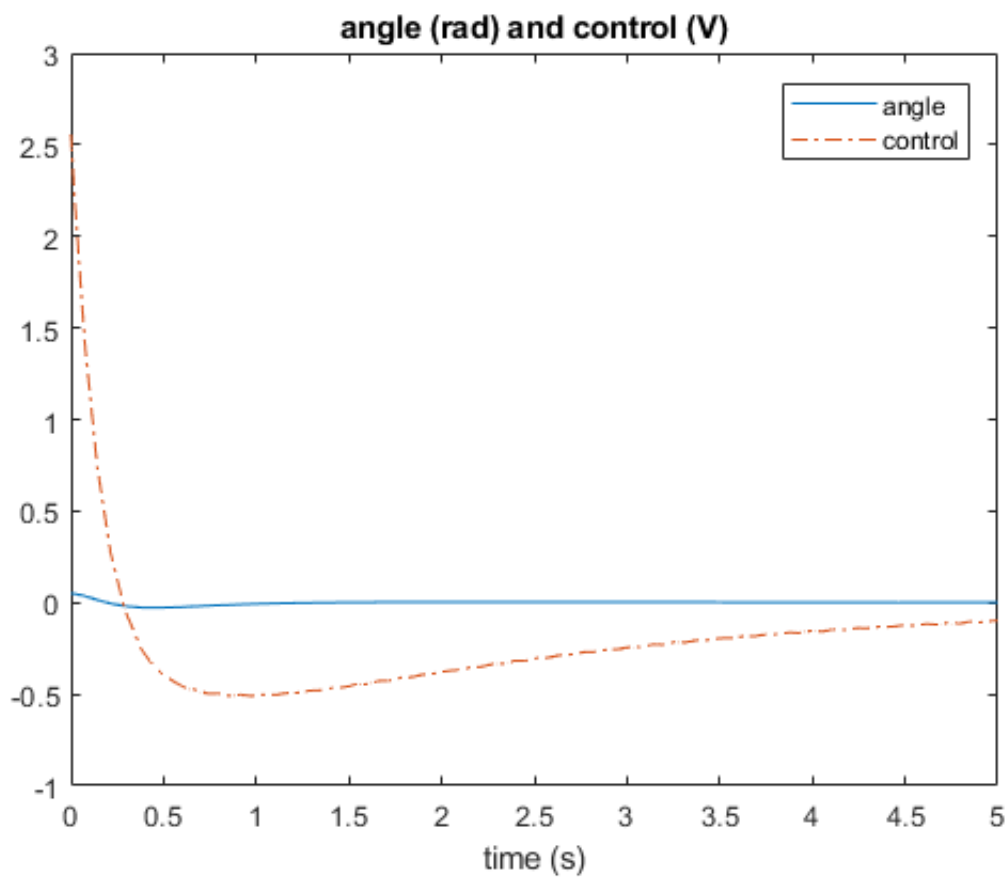












### 3.3

```
%position will first increase before converging to zero shows that the cart  
%is moving to swing the angle closer to 0
```