

1. (a) **Tradeoffs between copper and optical:** Optical cabling is more expensive than copper, but allows to transfer data significantly faster (higher bandwidth), over longer distances, and is immune to Electromagnetic Interference and Radio Frequency Interference due to close proximity to other electronic devices. Fibre optical cable is also smaller in diameter and weighs less, which is desirable for cabling solutions. Because a lot of technology was built on copper before fibre optics, it may be easier to build copper infrastructures and it is also cheaper, as no additional and expensive electronics are usually necessary.

(b) **(Extra-credit) Different protocols:**

(c) **(Extra-credit) Delayed release and early release:**

2. (a) **Output Signal-to-Noise Ratio:**

Output power level P_2 is unknown

$$-20 \text{ (dB)} = 10 \times \log_{10} \left(\frac{P_2}{0.5 \text{ (W)}} \right) \text{ (Negative because it's a loss)}$$

$$\Rightarrow P_2 = 0.005 \text{ (W)}$$

$$SNR_{dB} = 10 \log_{10} \frac{0.005 \text{ (W)}}{8 \times 10^{-6} \text{ (W)}} = 10 \log_{10} 625 = 27.9588 \text{ (dB)}$$

(b) **Capacity with a frequency range of 100-1000 Hz:**

$$(\text{Bandwidth}) B = 1000 - 100 = 900 \text{ (Hz)}$$

$$\frac{S}{N} = 625$$

$$\begin{aligned} (\text{Channel Capacity}) C &= B \times \log_2 \left(1 + \frac{S}{N} \right) \\ &= 900 \text{ (Hz)} \times \log_2 626 \\ &= 8361.02 \text{ (bps)} = 8.36102 \text{ (kbps)} \end{aligned}$$

(c) **Length of phone line before requiring a repeater:**

$$\text{Attenuation Rate} = 2 \text{ (dB/km)}$$

$$SNR = 10 \log_{10} \left(\frac{0.00025 \text{ (W)}}{0.5 \text{ (W)}} \right) = -33.01 \text{ (dB)}$$

$$\text{Max Phone Line Length} = \frac{33.01}{2} = 16.505 \text{ (km)}$$

3. 4B/5B encoding and NRZI signals (See next page for NRZI signals)

(a) **1110 0101 0000 0011**

4B/5B Encoding: 11100 01011 11110 10101

(b) **1101 1110 1010 1101 1011 1110 1110 1111**

4B/5B Encoding: 11011 11100 10110 11011 10111 11100 11100 11101

6. (a) **Probability of a collision in the i th round, q_i :** For a collision to happen in the i th round, both nodes must choose the same slot out of the 2^{i-1} slots for that round. Each slot is equally likely, so the probability for A and B to pick any specific slot is $1/2^{i-1}$. Therefore:

$$q_i = \sum_{n=0}^{2^{i-1}-1} \frac{1}{2^{i-1}} \times \frac{1}{2^{i-1}} = \frac{1}{2^{i-1}}$$

- (b) **Probability p_i that exactly i rounds are needed for success:** To reach i th round, there must have been $i - 1$ conflicts, one at every round before. In order to finish on the i th round, we must not have a conflict at the last round. Therefore:

$$p_i = \left(\prod_{n=1}^{i-1} q_n \right) \times (1 - q_i)$$

$$p_1 = 1$$

$$p_2 = 1 - \frac{1}{2} = \frac{1}{2}$$

$$p_3 = \frac{1}{2} \times \left(1 - \frac{1}{4} \right) = \frac{3}{8}$$

$$p_4 = \frac{1}{2} \times \frac{1}{4} \times \left(1 - \frac{1}{8} \right) = \frac{7}{64}$$

- (c) **Probability A wins again =**

$$1 - 2 \times \frac{1}{2} \times \frac{1}{4} = \frac{3}{4}$$

- (d) **Probability that A captures the network for the next 5 frames, given A won the first round:** At every round A must pick a time slot with value strictly smaller than B 's. Assuming after A wins round 1, its counter is 1 and B 's counter is 2:

$$P(\text{win}_2 | \text{win}_1) = \frac{1}{2} \times \frac{3}{4} + \frac{1}{2} \times \frac{2}{4} = \frac{5}{8}$$

$$P(\text{win}_3 | \text{win}_2, \text{win}_1) = \frac{1}{2} \times \frac{7}{8} + \frac{1}{2} \times \frac{6}{8} = \frac{13}{16}$$

$$P(\text{win}_4 | \text{win}_3, \text{win}_2, \text{win}_1) = \frac{1}{2} \times \frac{15}{16} + \frac{1}{2} \times \frac{14}{16} = \frac{29}{32}$$

$$P(\text{win}_5 | \text{win}_4, \text{win}_3, \text{win}_2, \text{win}_1) = \frac{1}{2} \times \frac{31}{32} + \frac{1}{2} \times \frac{30}{32} = \frac{61}{64}$$

$$P(\text{win}_2 \wedge \text{win}_3 \wedge \text{win}_4 \wedge \text{win}_5 | \text{win}_1) = \frac{5}{8} \times \frac{13}{16} \times \frac{29}{32} \times \frac{61}{64} = 0.4386$$

7. (a) **Efficiency of the network:**

Efficiency is defined as the ration between the time the network is being utilized and the total time. There is only one station sending data in this network so:

$$Efficiency = \frac{THT}{RingLatency + THT}$$

(b) **Optimall setting for THT:**

Since there is only one station working, the longer the single active station gets to hold on to the token the more efficient this network is. In fact, most optimal setting would be to never release the token.

(c) **Upper bound on Token Rotation Time, TRT:**

Maximum TRT would occur when each station holds on to the token for the duration of it's THT . Therefore:

$$TRT \leq RingLatency + N \times THT$$