

# Markov Regenerative Process - steady-state analysis

MVT exam

Stefano MARTINA

[stefano.martina@stud.unifi.it](mailto:stefano.martina@stud.unifi.it)

Tommaso PAPINI

[tommaso.papini1@stud.unifi.it](mailto:tommaso.papini1@stud.unifi.it)



UNIVERSITÀ  
DEGLI STUDI  
FIRENZE

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## Regenerative state

A state where the process loses its **memory**.

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CTMC

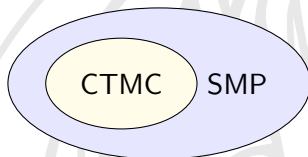
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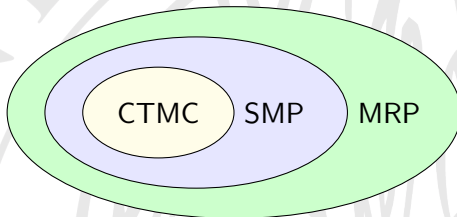
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# The steady-state problem

## Transient probabilities

The **probability** distribution that the process will be in a certain state, after given  $t$  **time**.

## Steady-state

For ergodic systems, it represents the **probability** distribution that the process will be in a certain state, as time goes to **infinity**.

- ✓ ORIS current state:
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# MRP steady-state analysis - The theory

General idea:

1. Calculate the embedded DTMC **steady-state** on the regenerative states
2. Calculate the expected **sojourn time** in each marking, after reaching a regenerative state
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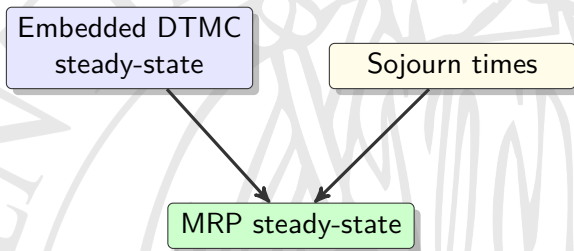
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  - written from scratch
  - calculate **embedded DTMC** steady-state
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# Steady-state of the embedded DTMC on regenerative states

## Steady-state in Discrete Time Markov Process (DTMC)

If the steady-state of a Discrete Time Markov Process (DTMC) exists and is unique (if is **ergodic**), then it's calculated by solving for  $v$  the linear system:

$$\begin{cases} v = vP \\ |v| = 1 \end{cases}$$

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## Reaching probability feature

- ✓ We add a new **reaching probability feature** to each state:  
`class ReachingProbabilityFeature`
- ✓ Inside `SteadyStateInitialStateBuilder`: set it to 1
- ✓ Inside `SteadyStatePostProcessor`: multiply the parent's reaching probability by the probability to chose a certain child

If we run a transient analysis on the Petri Net (PN) we get:

- ✓ `regenerationClasses`
- ✓ `Map<DeterministicEnablingState, Map<DeterministicEnablingState, Set<State>>>`
- ✓ sum reaching probability feature of each State to compute elements of  $P$



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$$\begin{cases} v = vP \\ |v| = 1 \end{cases} = \begin{cases} (P' - I)v' = 0 \\ \sum_i v_i = 1 \end{cases}$$

✓ **RealMatrix** & **RealVector**

✓ **QR decomposition** solver

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- DecompositionSolver solver = new QRDecomposition(coefficients).getSolver();  
- RealVector steadyState = solver.solve(constants);
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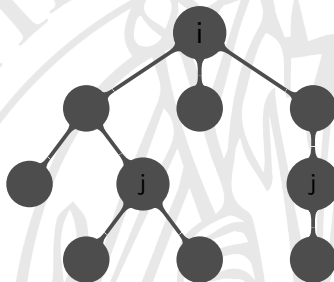
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The sojourn time  $a_{ij}$  represents the

- ✓ average time spent in the  $j$ -th marking
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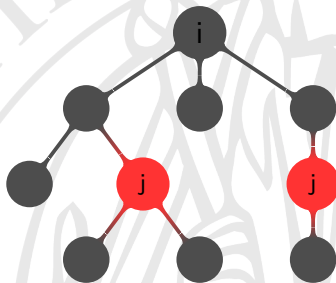


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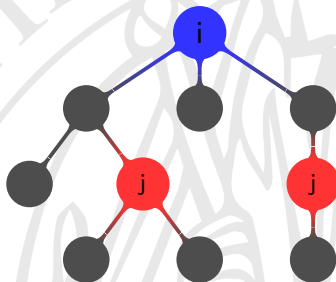


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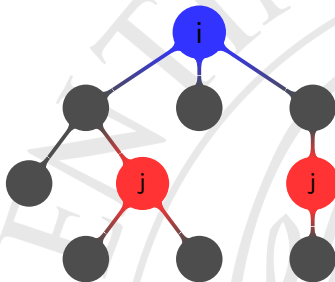
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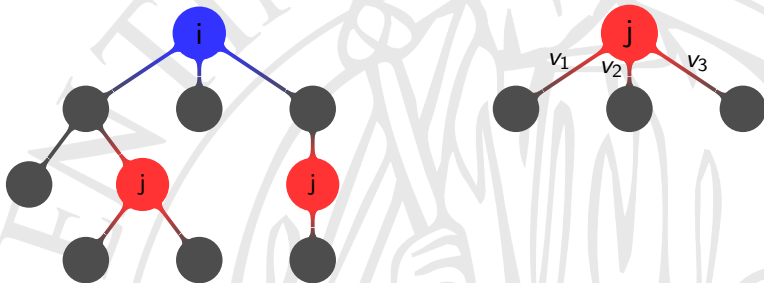
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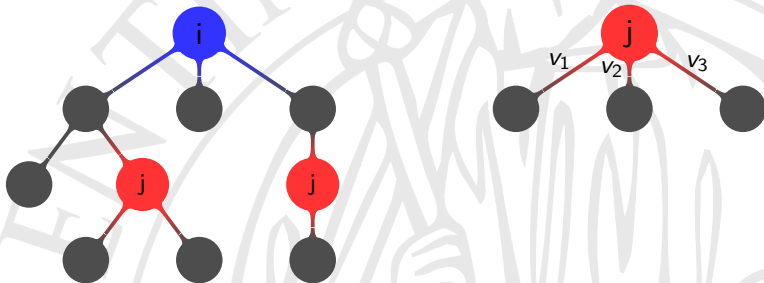
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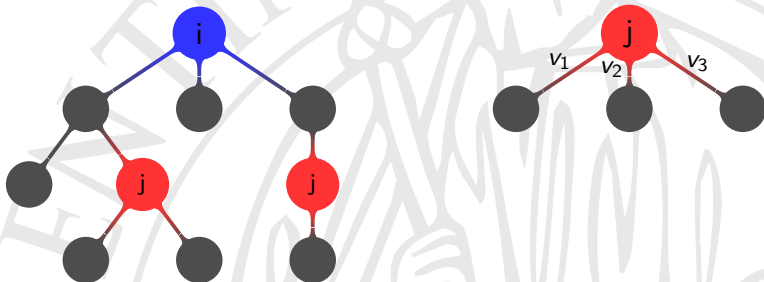




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  - regenerative state as **root**
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Let's **combine** the embedded DTMC steady-state and the sojourn times!

Formula:

$$\pi_j = \frac{\sum_i v_i a_{ij}}{Z}$$

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- ✓ Three different models:
  - TestCaseSMP
  - TestCase2ParallelTasks
  - TestCaseRejuvenation
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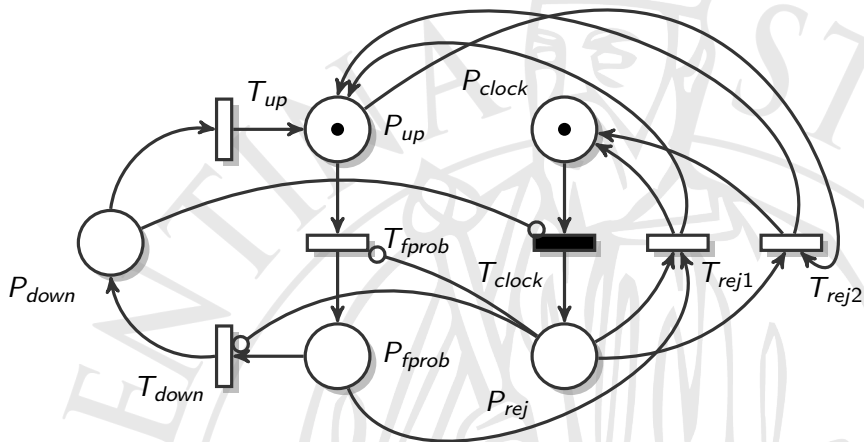
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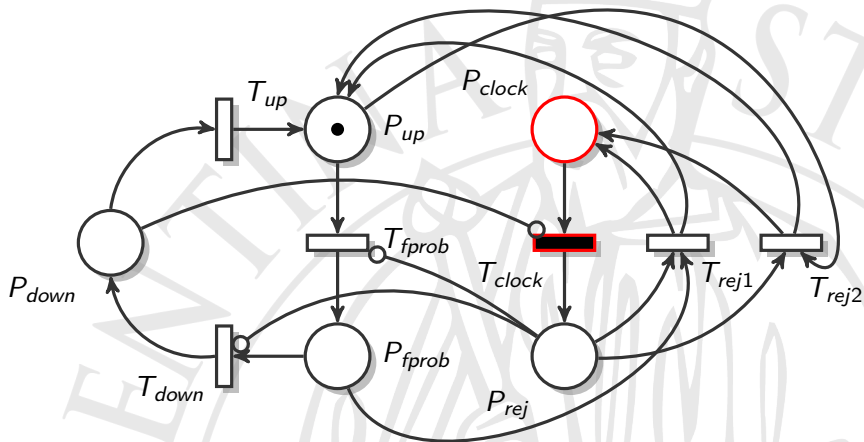
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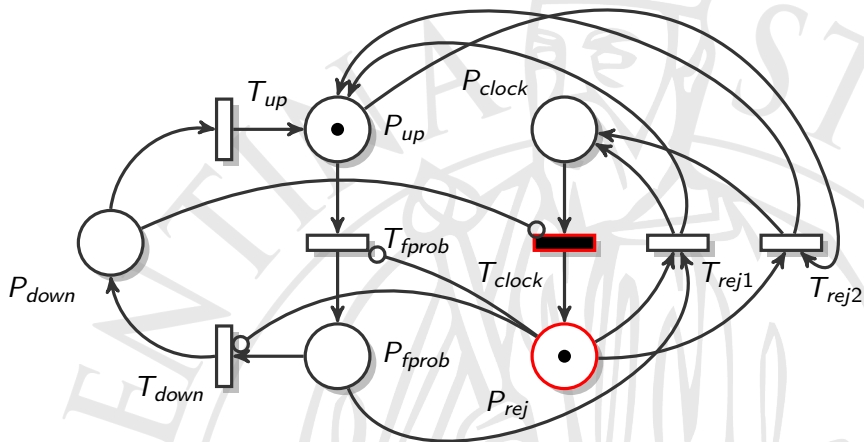
# Rejuvenation



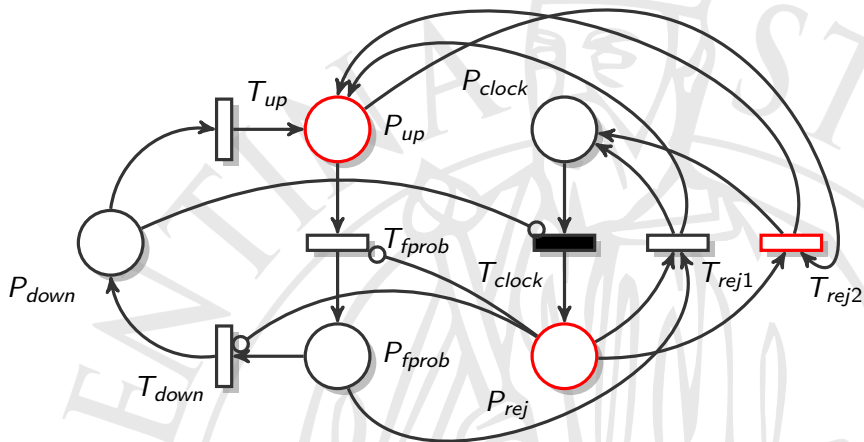
# Rejuvenation



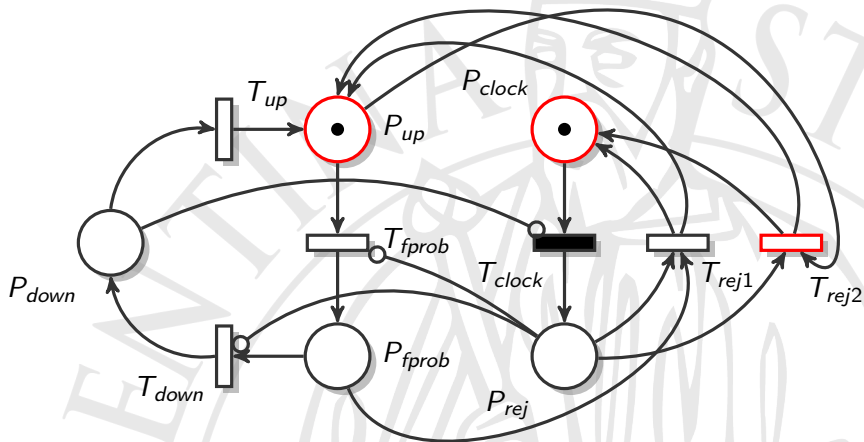
# Rejuvenation



# Rejuvenation

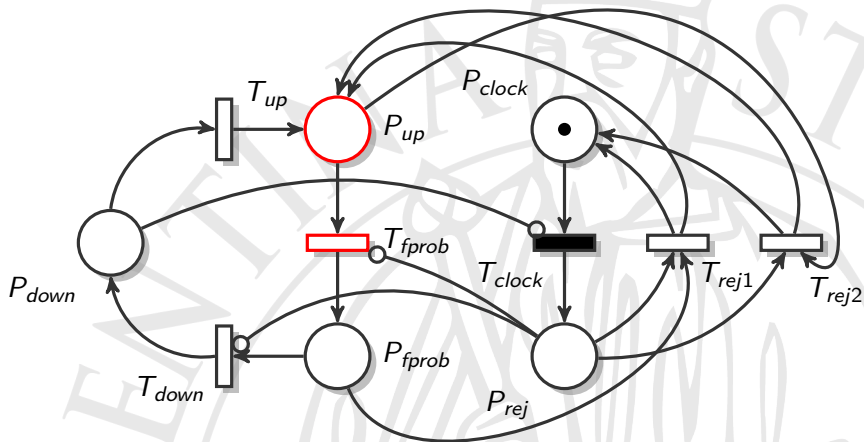


# Rejuvenation

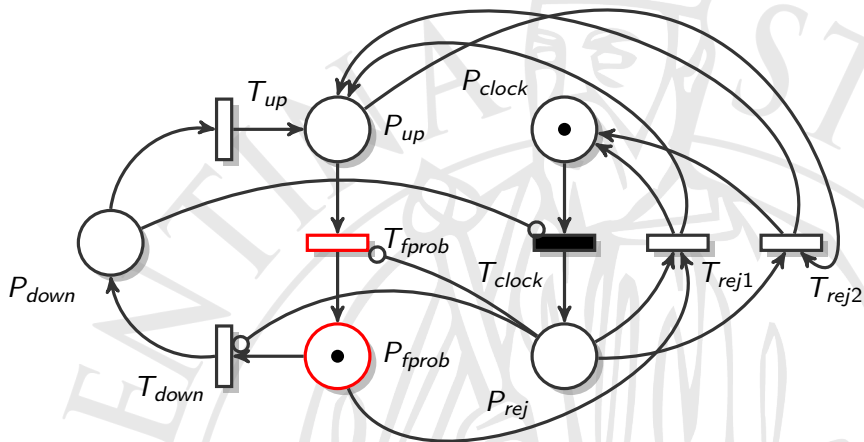




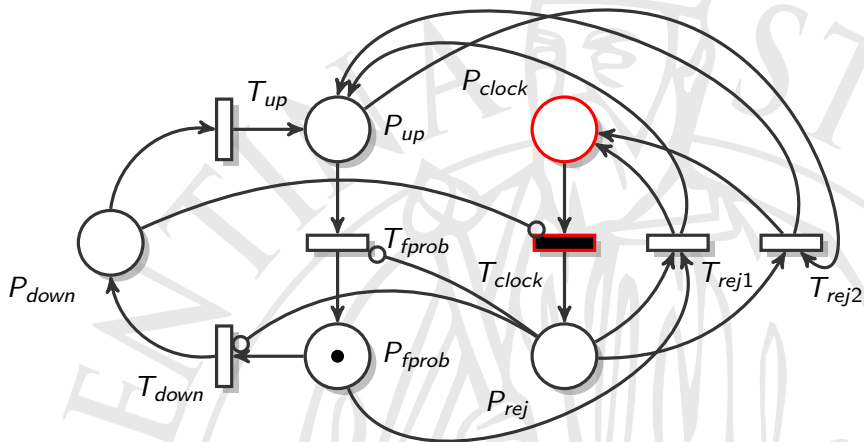
# Rejuvenation



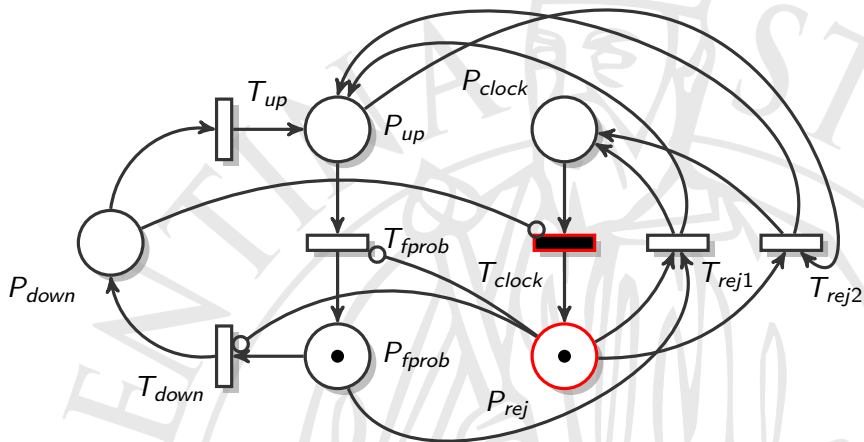
# Rejuvenation



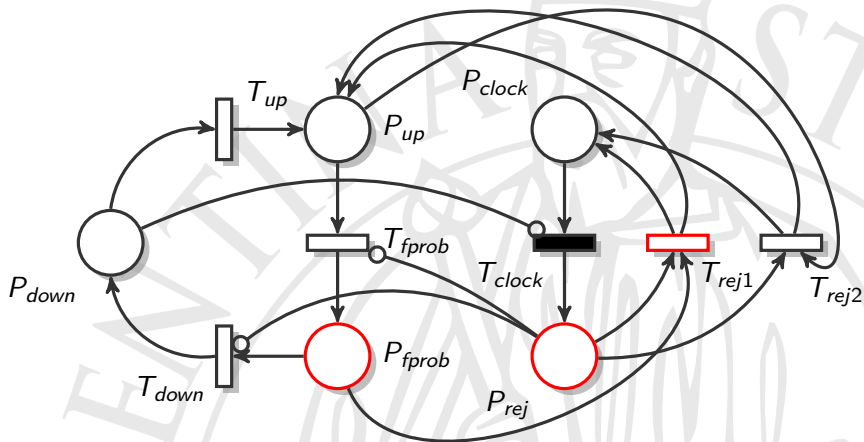
# Rejuvenation



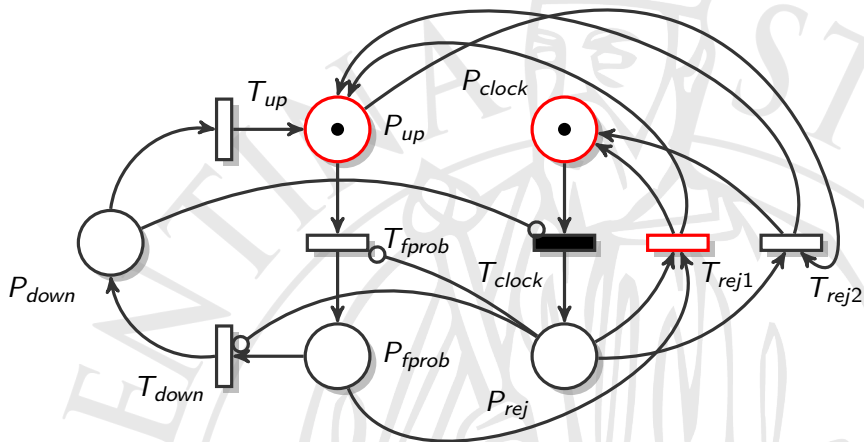
# Rejuvenation



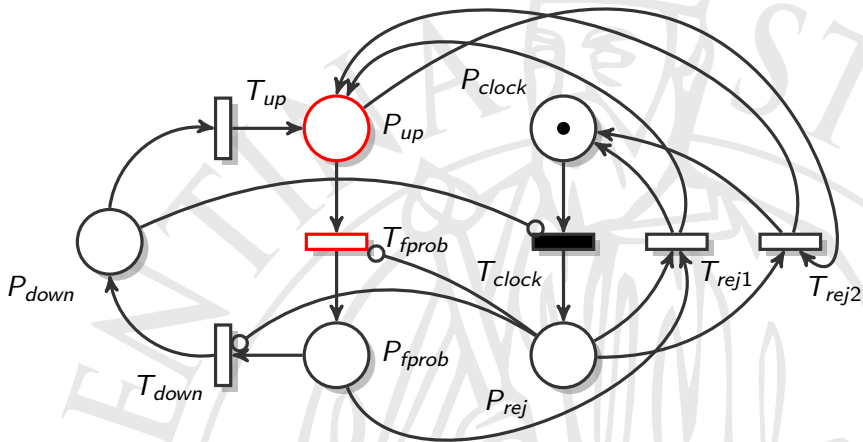
# Rejuvenation



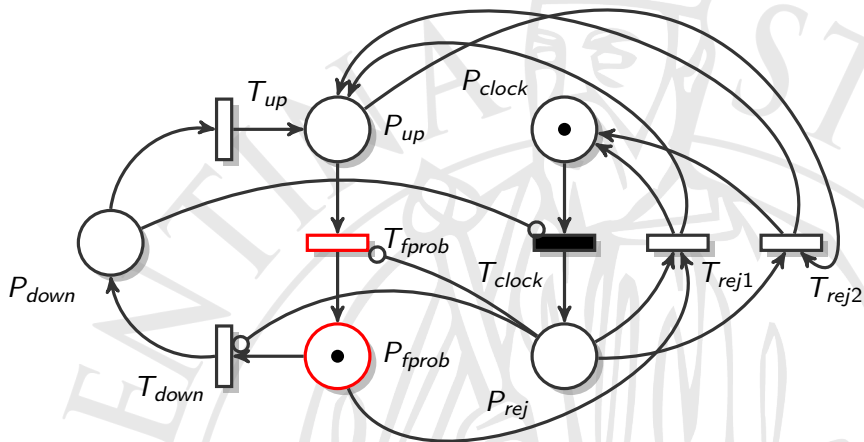
# Rejuvenation



## Rejuvenation

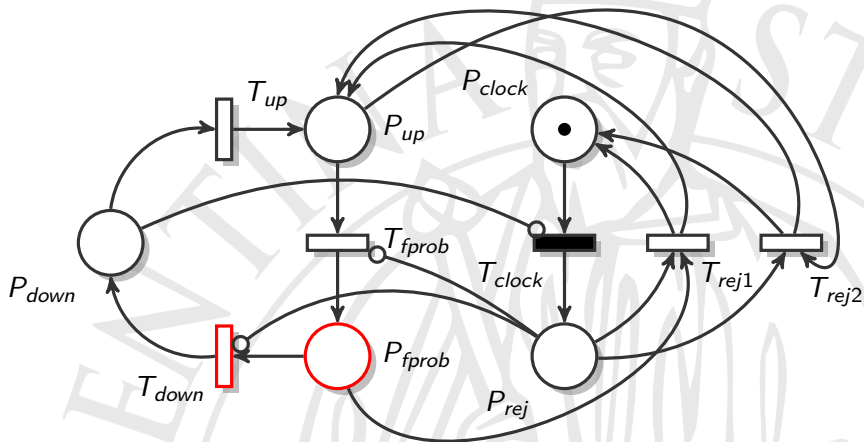


# Rejuvenation

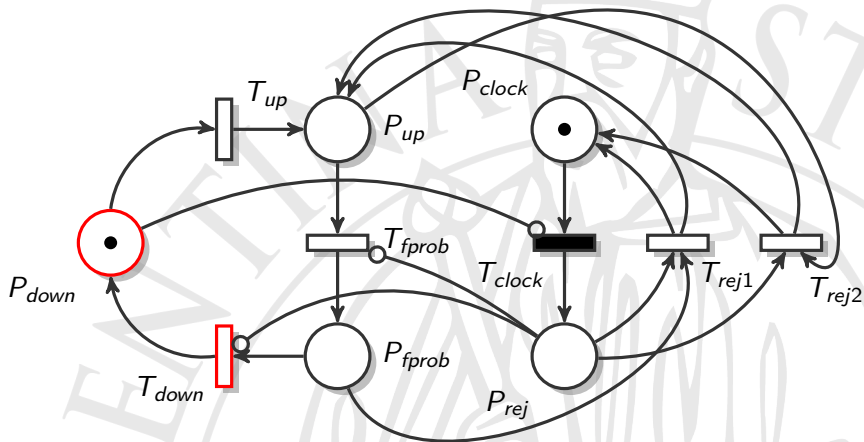




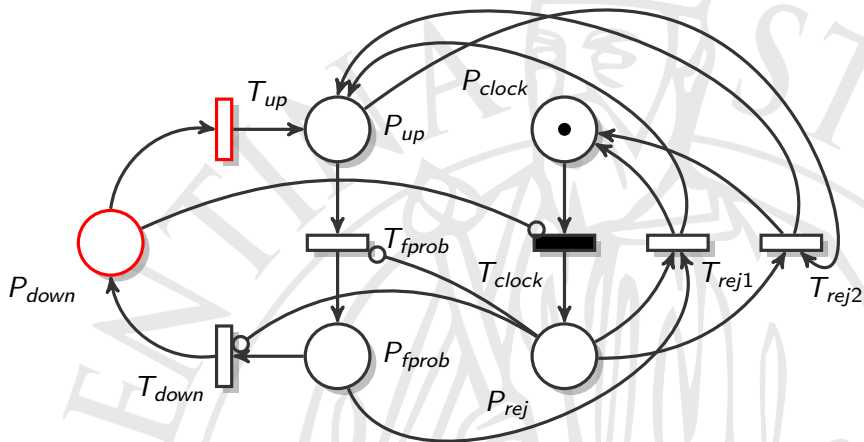
# Rejuvenation



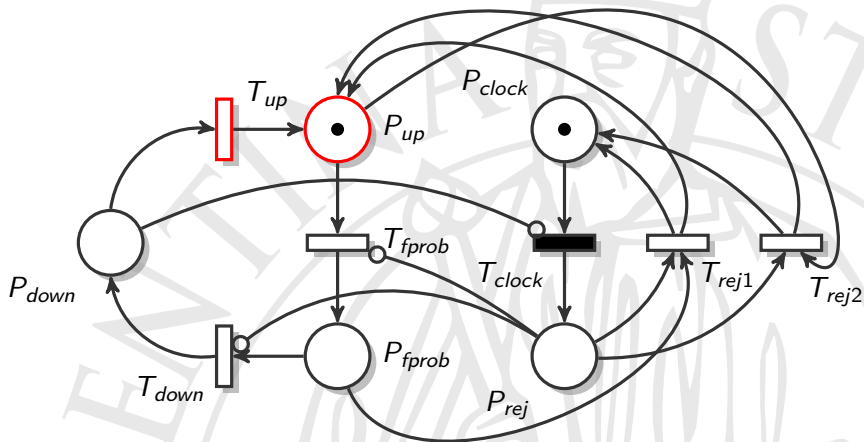
# Rejuvenation



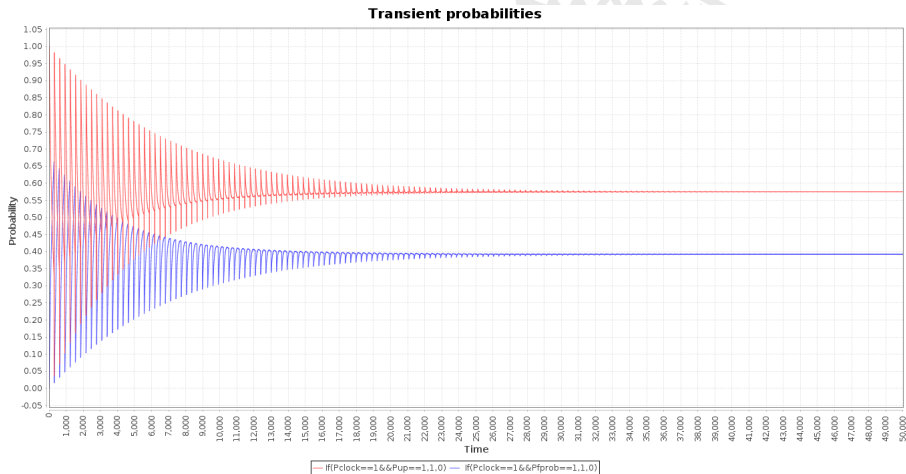
# Rejuvenation



# Rejuvenation



# Transient analysis

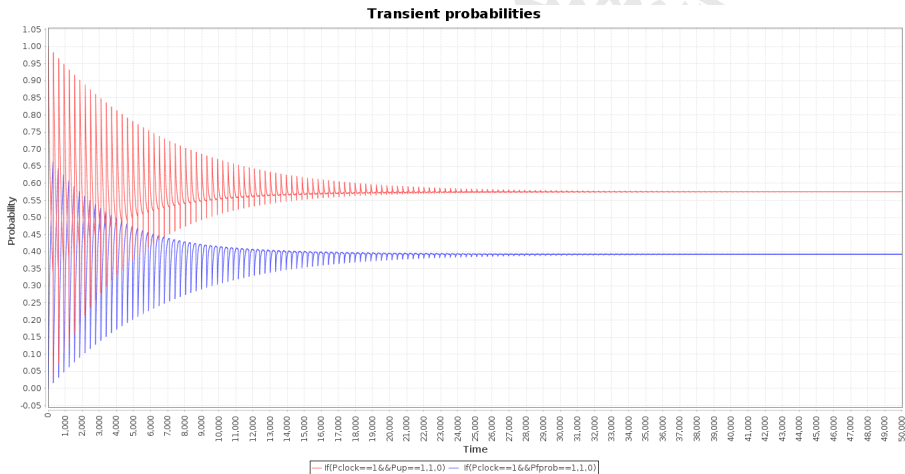


✓ Steady-state estimation using **transient** analysis:

-  $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{up}} = 1) \approx 0.58$

-  $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{fprob}} = 1) \approx 0.40$

# Transient analysis



✓ Steady-state estimation using **transient** analysis:

- $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{up}} = 1) \approx 0.58$
- $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{fprob}} = 1) \approx 0.40$

# Steady state analysis

```
1 Map<String, Integer> tmpPlacesMarking = new HashMap<  
    ↪ String, Integer>();  
2 tmpPlacesMarking.put("Pup", Integer.parseInt("1"));  
3 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
4 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.58"));  
5  
6 tmpPlacesMarking = new HashMap<String, Integer>();  
7 tmpPlacesMarking.put("Pfprob", Integer.parseInt("1"));  
8 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
9 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.40"));
```

Test  
Passed

# Steady state analysis

```
1 Map<String, Integer> tmpPlacesMarking = new HashMap<  
    ↪ String, Integer>();  
2 tmpPlacesMarking.put("Pup", Integer.parseInt("1"));  
3 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
4 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.58"));  
5  
6 tmpPlacesMarking = new HashMap<String, Integer>();  
7 tmpPlacesMarking.put("Pfprob", Integer.parseInt("1"));  
8 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
9 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.40"));
```



Test  
Passed



<<Java Class>>

### RegenerativeSteadyStateAnalysis<R>

it.unifi.oris.oris.sirio.models.stpn

- reachableMarkings: Set<Marking>
- alwaysRegenerativeMarkings: Set<Marking>
- neverRegenerativeMarkings: Set<Marking>
- regenerativeAndNotRegenerativeMarkings: Set<Marking>
- sojournMap: Map<R, Map<Marking, BigDecimal>>
- steadyState: Map<Marking, BigDecimal>
- initialRegeneration: R
- petriNet: PetriNet
- truncationPolicy: EnumerationPolicy
- absorbingCondition: MarkingCondition
- absorbingMarkings: Set<Marking>
- localClasses: Map<R, Map<Marking, Set<State>>>
- regenerationClasses: Map<R, Map<R, Set<State>>>
- regenerations: Set<R>

- getDTMC(): EmbeddedDTMC<R>
- getSojournMap(): Map<R, Map<Marking, BigDecimal>>
- getSteadyState(): Map<Marking, BigDecimal>
- getReachableMarkings(): Set<Marking>
- getAlwaysRegenerativeMarkings(): Set<Marking>
- getNeverRegenerativeMarkings(): Set<Marking>
- getRegenerativeAndNotRegenerativeMarkings(): Set<Marking>
- getInitialRegeneration()
- getRegenerations(): Set<R>
- getPetriNet(): PetriNet
- getTruncationPolicy(): EnumerationPolicy
- getAbsorbingCondition(): MarkingCondition
- getAbsorbingMarkings(): Set<Marking>
- getLocalClasses(): Map<R, Map<Marking, Set<State>>>
- getRegenerationClasses(): Map<R, Map<R, Set<State>>>
- RegenerativeSteadyStateAnalysis()
- canAnalyze(PetriNet, ValidationMessageCollector) boolean
- calculateSteadyState(RegenerativeSteadyStateAnalysis<R>): Map<Marking, BigDecimal>
- compute(PetriNet, R, StateBuilder<R>, SuccessionProcessor, EnumerationPolicy, MarkingCo...

<<Java Class>>

### EmbeddedDTMC<R>

it.unifi.oris.oris.sirio.models.stpn

- reachingProbabilities: Map<R, Map<R, BigDecimal>>
- steadyState: Map<R, BigDecimal>
- EmbeddedDTMC()
- compute(Set<R>, Map<R, Map<R, Set<State>>>): EmbeddedDTMC<R>
- mapRegenerativeStates(Set<R>): Map<R, Integer>
- computeReachingProbabilities(Map<R, Integer>, Map<R, Map<R, Set<State>>>): RealMatrix
- computeSteadyState(Map<R, Integer>, RealMatrix): RealVector
- getReachingProbabilities(): Map<R, Map<R, BigDecimal>>
- getSteadyState(): Map<R, BigDecimal>

-eDTMC 0..1



<<Java Class>>

### ReachingProbabilityFeature

it.unifi.oris.oris.sirio.models.stpn

- reachingProbability: BigDecimal
- ReachingProbabilityFeature(BigDecimal)
- getValue(): BigDecimal
- toString(): String

<<Java Class>>

### SteadyStateInitialStateBuilder

it.unifi.oris.oris.sirio.models.stpn

- sb: DeterministicEnablingStateBuilder
- SteadyStateInitialStateBuilder(PetriNet)
- build(DeterministicEnablingState): State

<<Java Class>>

### SteadyStatePostProcessor

it.unifi.oris.oris.sirio.models.stpn

- es: EnablingSyncsEvaluator
- SteadyStatePostProcessor()
- process(Succession): Succession



*The End.*

*Questions? Thank you!*

*The End.*



*Questions? Thank you!*

*The End.*



*Questions? Thank you!*