

Markov Regenerative Process steady-state analysis

MVT exam

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Markov Regenerative Processes (MRPs)

Definition

A Markov Regenerative Process (MRP) is a stochastic process that sooner or later, with probability one, will reach a **regenerative** state (will be regenerated).

Regenerative state

A state where the process loses its **memory**.

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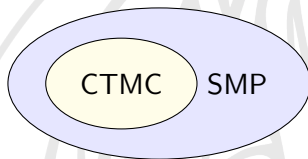
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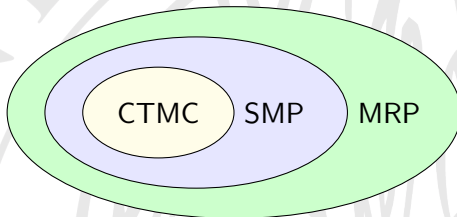
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The steady-state problem

Transient probabilities

The **probability** distribution that the process will be in a certain state, after given t **time**.

Steady-state

For ergodic systems, it represents the **probability** distribution that the process will be in a certain state, as time goes to **infinity**.

- ✓ ORIS current state:
 - **Transient** analysis for Markov Regenerative Processes (MRPs)
 - **Steady-state** analysis for Continuous Time Markov Processes (CTMCs)
- ✓ Until now! ☹
- ✓ **Warning:** we assume that the MRP is **ergodic**!

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MRP steady-state analysis - The theory

General idea:

1. Calculate the embedded DTMC **steady-state** on the regenerative states
2. Calculate the expected **sojourn time** in each marking, after reaching a regenerative state
3. **Combine** the two above in order to calculate the MRP steady-state

Embedded DTMC
steady-state

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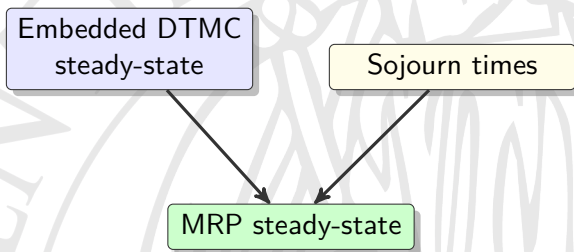
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Main classes implemented

- ✓ **class** EmbeddedDTMC
 - written from scratch
 - calculate **embedded DTMC** steady-state
- ✓ **class** RegenerativeSteadyStateAnalysis
 - based on **class** RegenerativeTransientAnalysis
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Steady-state of the embedded DTMC on regenerative states

Steady-state in Discrete Time Markov Process (DTMC)

If the steady-state of a Discrete Time Markov Process (DTMC) exists and is unique (if is **ergodic**), then it's calculated by solving for v the linear system:

$$\begin{cases} v = vP \\ |v| = 1 \end{cases}$$

- ✓ We want to calculate the **steady-state** of the embedded DTMC of the MRP in the **regenerative states**
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Reaching probability feature

- ✓ We add a new **reaching probability feature** to each state:
`class ReachingProbabilityFeature`
- ✓ Inside `SteadyStateInitialStateBuilder`: set it to 1
- ✓ Inside `SteadyStatePostProcessor`: multiply the parent's reaching probability by the probability to chose a certain child

If we run a transient analysis on the Petri Net (PN) we get:

- ✓ `regenerationClasses`
- ✓ `Map<DeterministicEnablingState, Map<DeterministicEnablingState, Set<State>>>`
- ✓ sum reaching probability feature of each State to compute elements of P

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Now we can **solve** the linear system:

$$\begin{cases} v = vP \\ |v| = 1 \end{cases} = \begin{cases} (P' - I)v' = 0 \\ \sum_i v_i = 1 \end{cases}$$

✓ RealMatrix & RealVector

✓ QR decomposition solver

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- DecompositionSolver solver = new QRDecomposition(coefficients).getSolver();  
- RealVector steadyState = solver.solve(constants);
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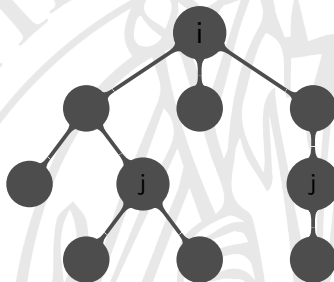
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The sojourn time a_{ij} represents the

- ✓ average time spent in the j -th marking
- ✓ after the (last) i -th regeneration.

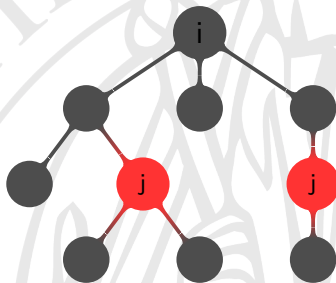


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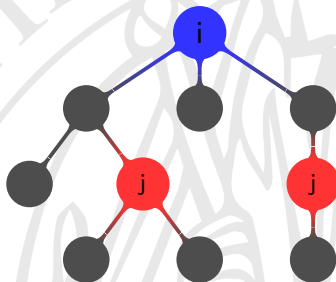


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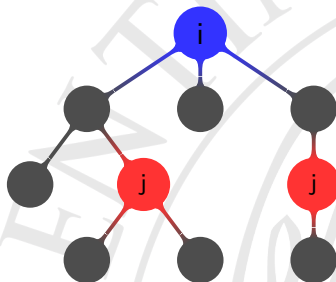
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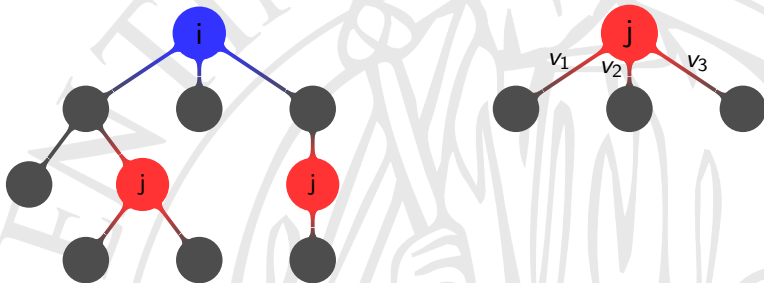
- ✓ sum of avg **time spent** in marking j occurrences
 - **sum** of avg times before each variable fires **weighted** by the probability of choosing that variable
 - ★ **condition** each variable to be the minimum (i.e. the one that fires)
 - ★ compute avg time **before** that variable fires (thanks Marco!)



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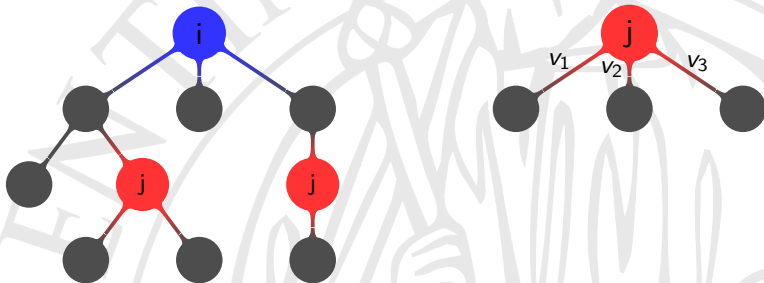
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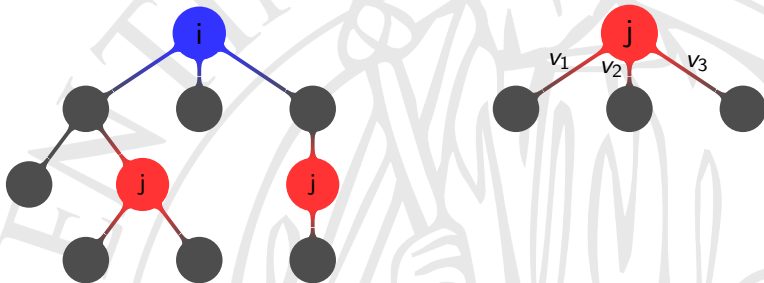
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During the transient analysis!

- ✓ transient analysis generates **succession trees** for each regenerative state
 - regenerative state as **root**
 - following regenerative states as **leaves**
 - reachable markings as inner **nodes**
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Markov Regenerative Process (MRP) steady-state

Let's **combine** the embedded DTMC steady-state and the sojourn times!

Formula:

$$\pi_j = \frac{\sum_i v_i a_{ij}}{Z}$$

- ✓ We **multiply** the **sojourn** time in the marking **j** after the regeneration **i** by the **probability** of reaching the **i**-th regeneration
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Unit test

- ✓ Class SteadyStateTest with JUnit tests
- ✓ Three different models:
 - TestCaseSMP
 - TestCase2ParallelTasks
 - TestCaseRejuvenation
- ✓ For each test:
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 2. check if the result is comparable to the expected value (with a tolerance)

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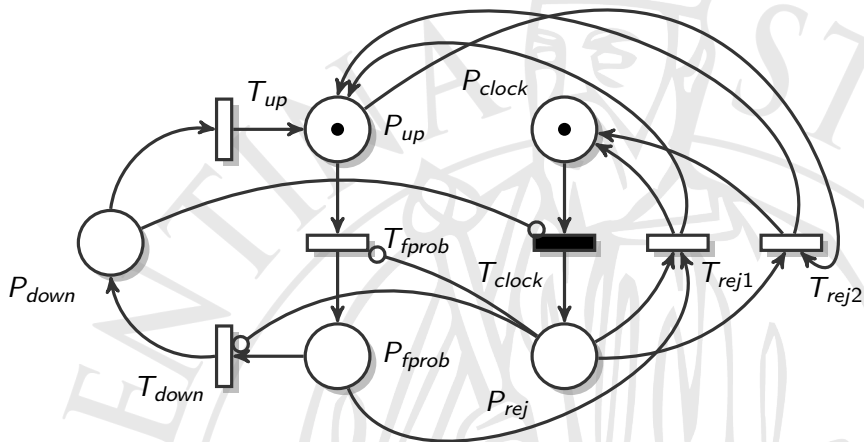
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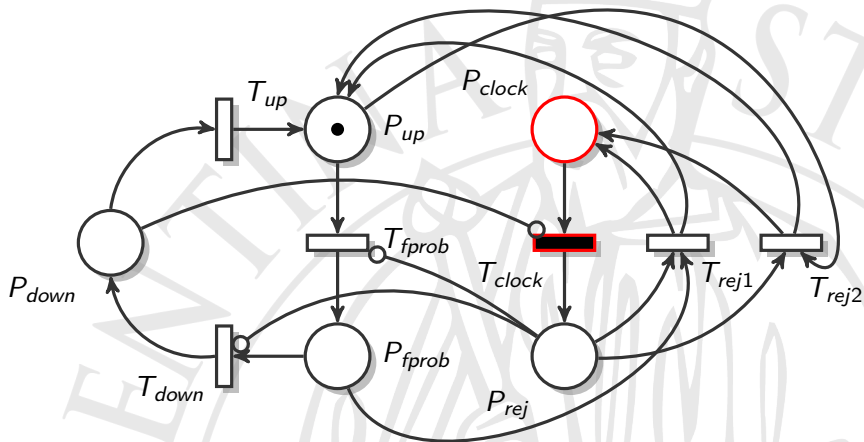
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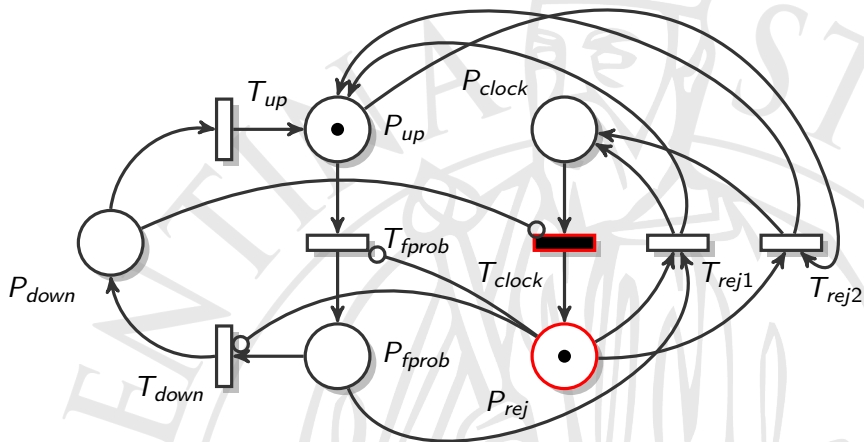
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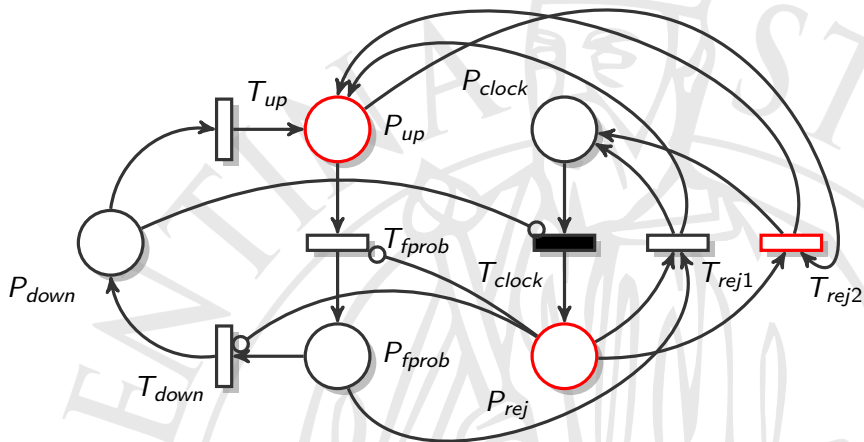
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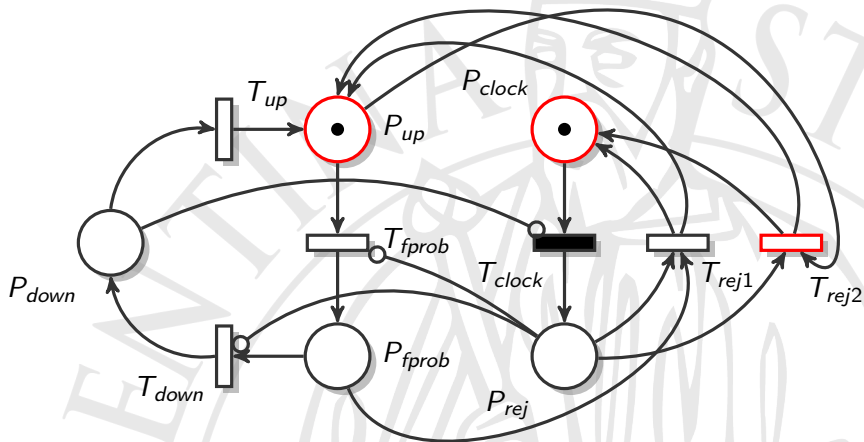
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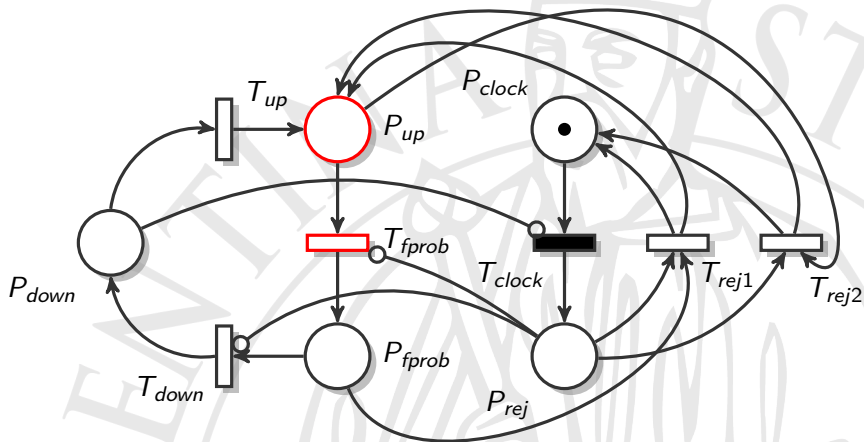
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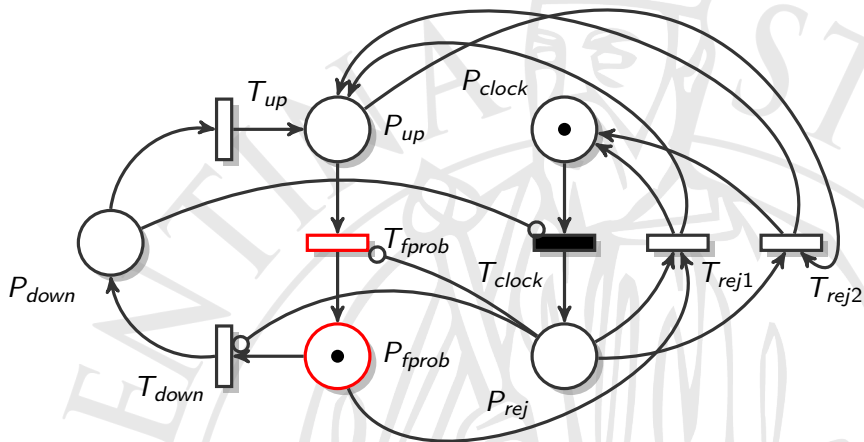
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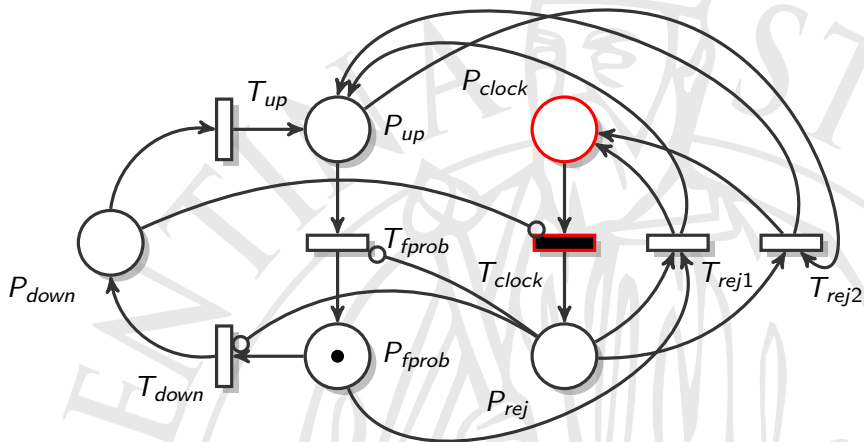
Rejuvenation



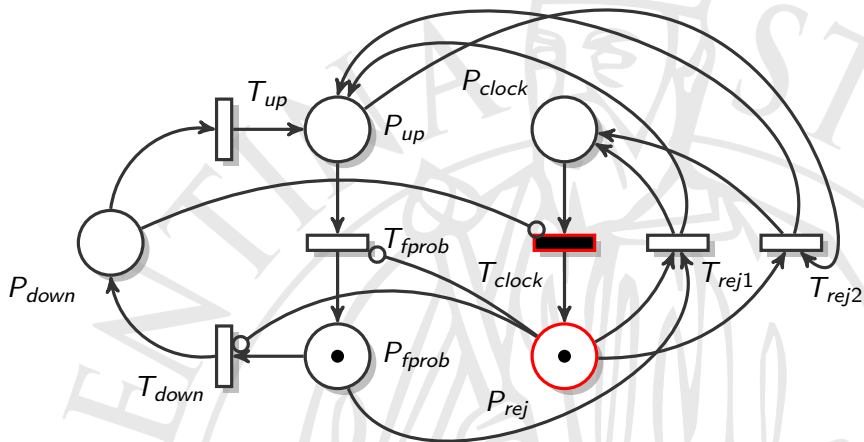
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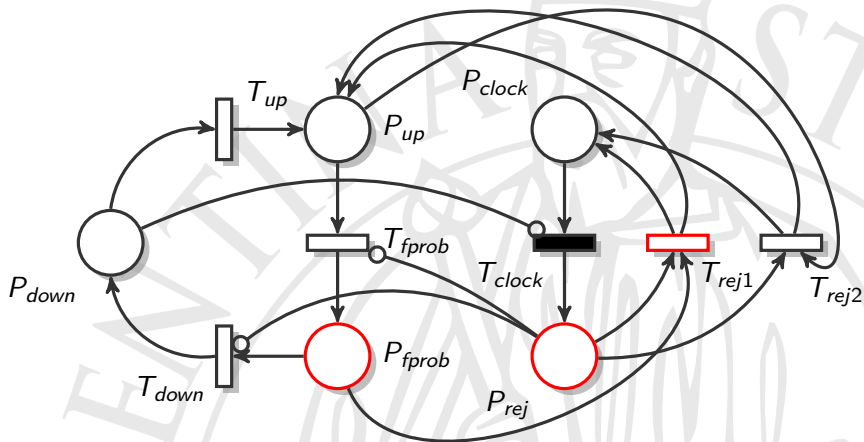
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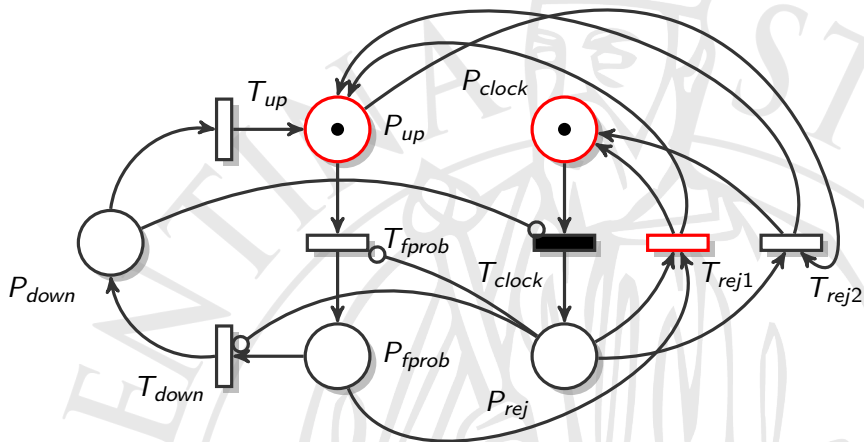
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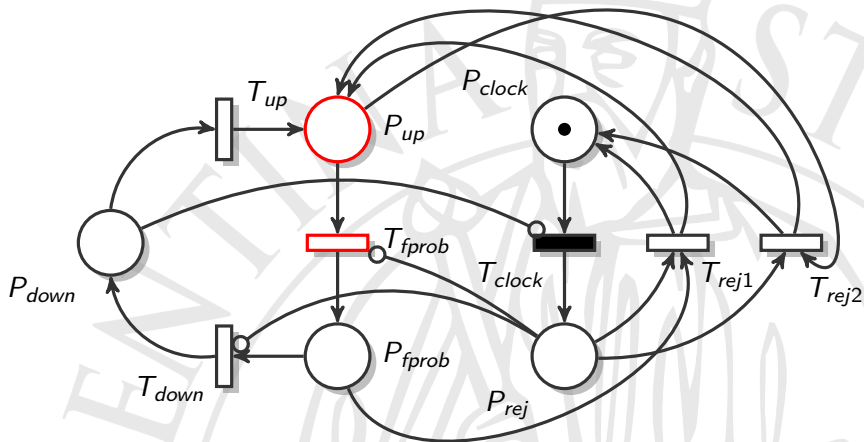
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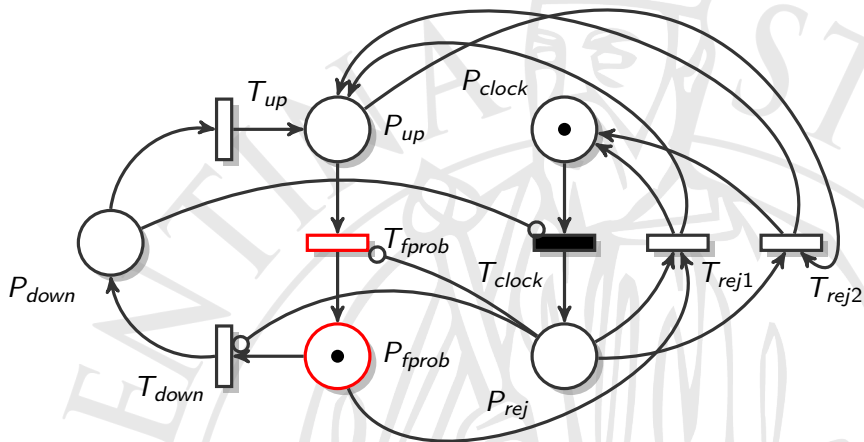
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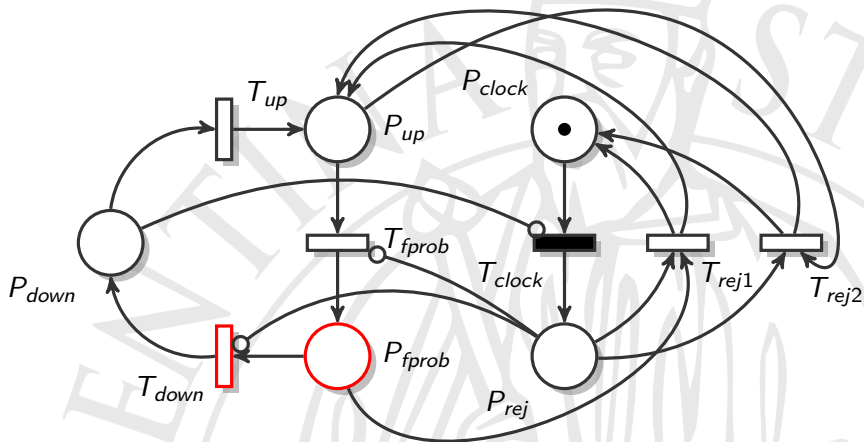
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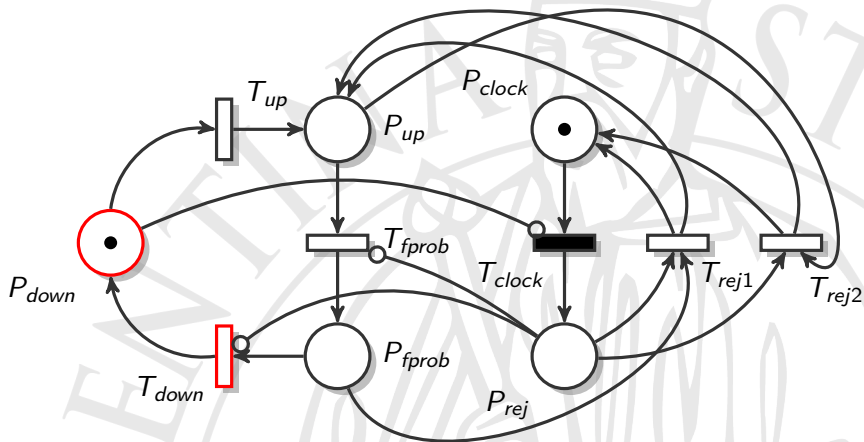
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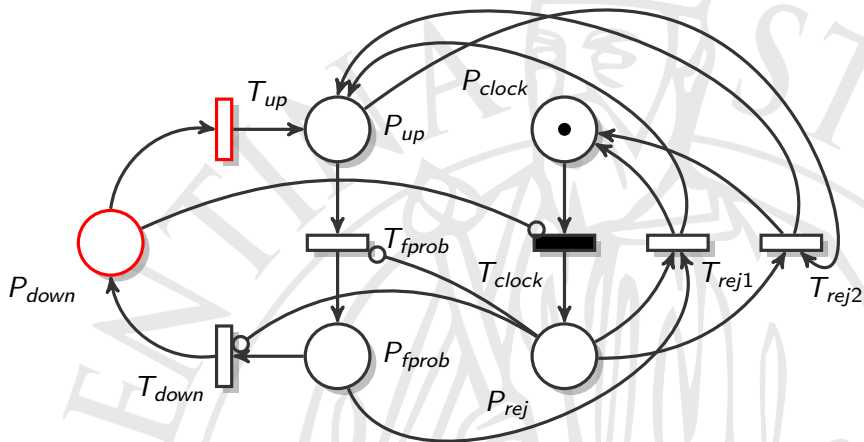
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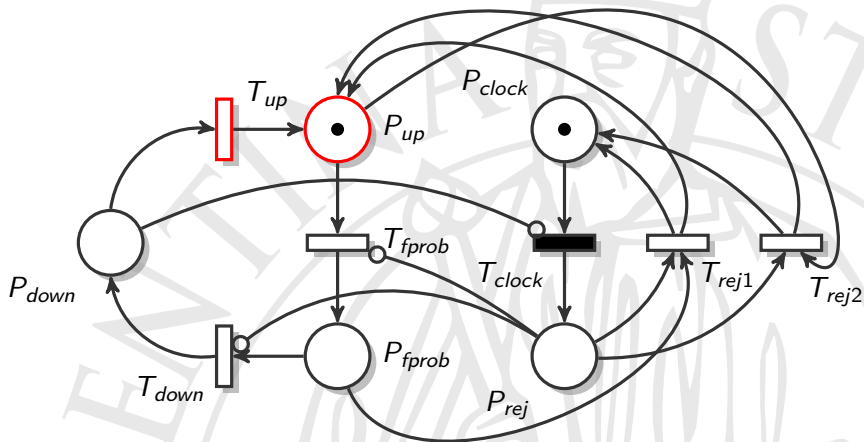
Rejuvenation



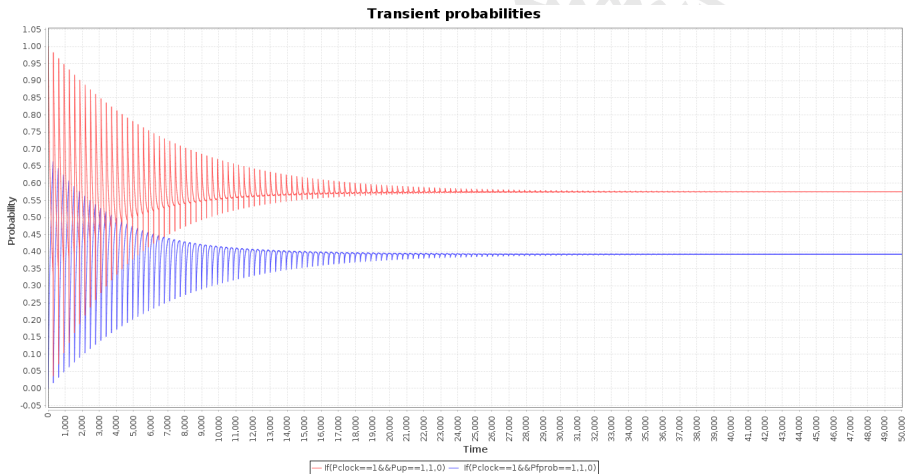
Rejuvenation



Rejuvenation



Transient analysis

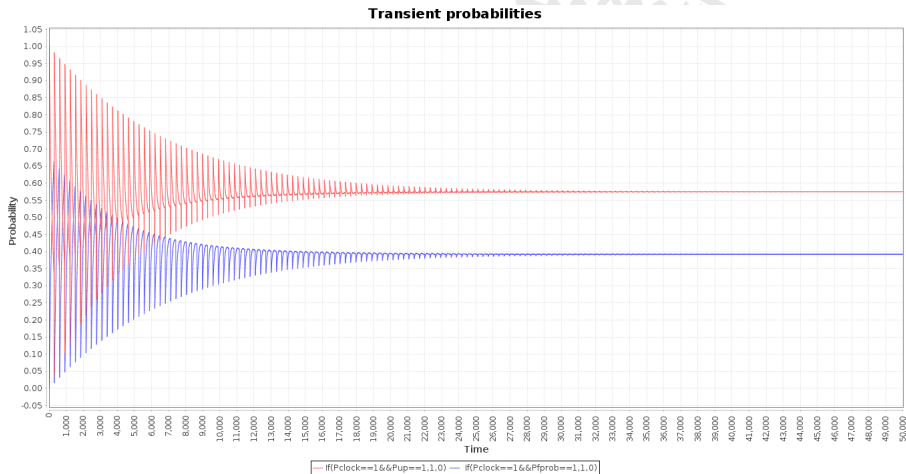


✓ Steady-state estimation using **transient** analysis:

- $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{up}} = 1) \approx 0.58$

- $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{fprob}} = 1) \approx 0.40$

Transient analysis



✓ Steady-state estimation using **transient** analysis:

- $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{up}} = 1) \approx 0.58$
- $\text{Prob}(P_{\text{clock}} = 1 \wedge P_{\text{fprob}} = 1) \approx 0.40$

Steady state analysis

```
1 Map<String, Integer> tmpPlacesMarking = new HashMap<  
    ↪ String, Integer>();  
2 tmpPlacesMarking.put("Pup", Integer.parseInt("1"));  
3 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
4 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.58"));  
5  
6 tmpPlacesMarking = new HashMap<String, Integer>();  
7 tmpPlacesMarking.put("Pfprob", Integer.parseInt("1"));  
8 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
9 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.40"));
```

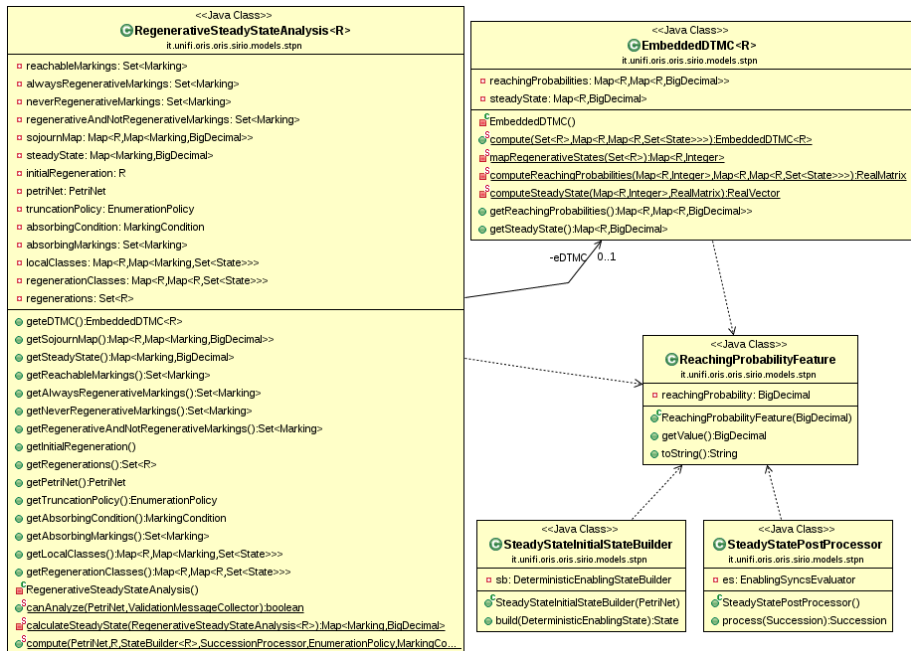
Test
Passed

Steady state analysis

```
1 Map<String, Integer> tmpPlacesMarking = new HashMap<  
    ↪ String, Integer>();  
2 tmpPlacesMarking.put("Pup", Integer.parseInt("1"));  
3 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
4 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.58"));  
5  
6 tmpPlacesMarking = new HashMap<String, Integer>();  
7 tmpPlacesMarking.put("Pfprob", Integer.parseInt("1"));  
8 tmpPlacesMarking.put("Pclock", Integer.parseInt("1"));  
9 getTestPlacesMarkings().put(tmpPlacesMarking, new  
    ↪ BigDecimal("0.40"));
```



Test
Passed





The End.

Questions? Thank you!



The End.

Questions? Thank you!

The End.



Questions? Thank you!