

\*See the HiHW grading rubric posted on Carmen\*

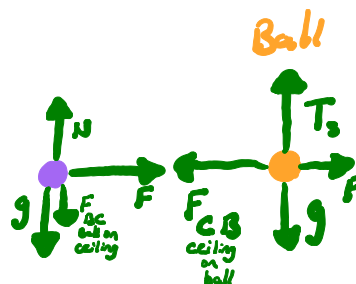
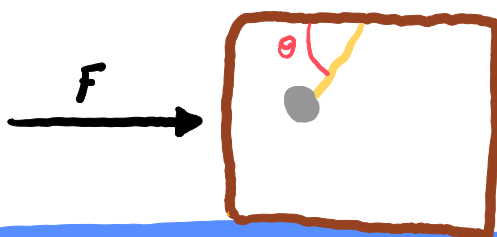
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A metal ball ( $m = 1.9 \text{ kg}$ ) hangs by a light string from the ceiling of a wooden crate ( $M = 5.2 \text{ kg}$ ). The crate is then pushed with a constant horizontal force  $F$  along some friction-less ice. This causes the ball hang inside the crate at an angle of  $\theta = 40^\circ$  with respect to the vertical. What is the value of  $F$ ? (Hint: if the ceiling of the crate is pulling on the ball, then the ball is pulling back on the ceiling of the crate.) For the limit check, investigate what happens to  $F$  as the angle  $\theta$  drops to zero.

Representation:	0	1	2
Physics Concept(s):	0	1	2
Initial Equation(s):	0	0.5	1
Symbolic Answer:	0		1
Units Check:	0	0.5	1
Limits Check:	0	0.5	1
Neatness:	-2	-1	0
Total:			
Correct Answer:	Y	N	

Representation

$$m = 1.9 \text{ kg} \quad M = 5.2 \text{ kg} \quad \theta = 40^\circ$$



Physics Concept(s) (Refer to the list posted on Carmen)

(1) Newton's Laws of Motion

Initial Equations

$$F = ma$$

$$\tan \theta = \frac{a}{g}$$

$$F_g = mg$$

$$\theta_i = 90 - \theta$$

$$\tan \theta_i = \frac{F}{F_g} \rightarrow F = F_g \tan \theta_i$$

Ball

$$\sum f_x = ma_x$$

$$\hookrightarrow T \sin \theta = ma \quad [\text{Eq. 1}]$$

$$\sum f_y = ma_y$$

$$\hookrightarrow T \cos \theta - mg = 0$$

$$T \cos \theta = mg$$

$$T = \frac{mg}{\cos \theta} \quad [\text{Eq. 3}]$$

Crate

$$\sum f_x = M_c a_x$$

$$-T \sin \theta + f = M_c a \quad [\text{Eq. 2}]$$

Eq. 1 + Eq. 2

$$a = \frac{f}{M_c + m}$$

$$\hookrightarrow f = g \tan \theta (M_c + m)$$

Symbolic Answer:

$$F = F_g \tan \theta_i$$

Units Check

$$F_g = mg$$

$$N = \text{kg} \cdot \text{m/s}^2 \quad \checkmark$$

$$F = F_g \tan \theta_i$$

$$N = N \cdot ? \quad \checkmark$$

Limits Check

a) As  $\theta \rightarrow 0^\circ$ , what limit does  $F$  approach?

$$\lim_{\theta \rightarrow 0^\circ} F = \infty$$

b) Why does the result make physical sense?

The angle approaching  $0^\circ$  means that the force is increasing

Numerical Answer: (Obtain this by plugging numbers into your symbolic answer.)

$$F_g = 18.62 \text{ N}$$

$$F = 22.19 \text{ N}$$