
Homework 2

Problem 2.1

a)

$$A = 13$$

$$w_0 = 1300000\pi$$

$$\theta = 30^\circ$$

b)

$$A = 0.5$$

$$w_0 = 960000\pi$$

$$\theta = -15^\circ$$

c)

$$A = 200$$

$$w_0 = 720000\pi$$

$$\theta = 45^\circ$$

d)

$$A = 125$$

$$w_0 = 540000\pi$$

$$\theta = -25^\circ$$

e)

$$A = 0.001$$

$$w_0 = 1200000\pi$$

$$\theta = -37^\circ$$

Problem 2.2

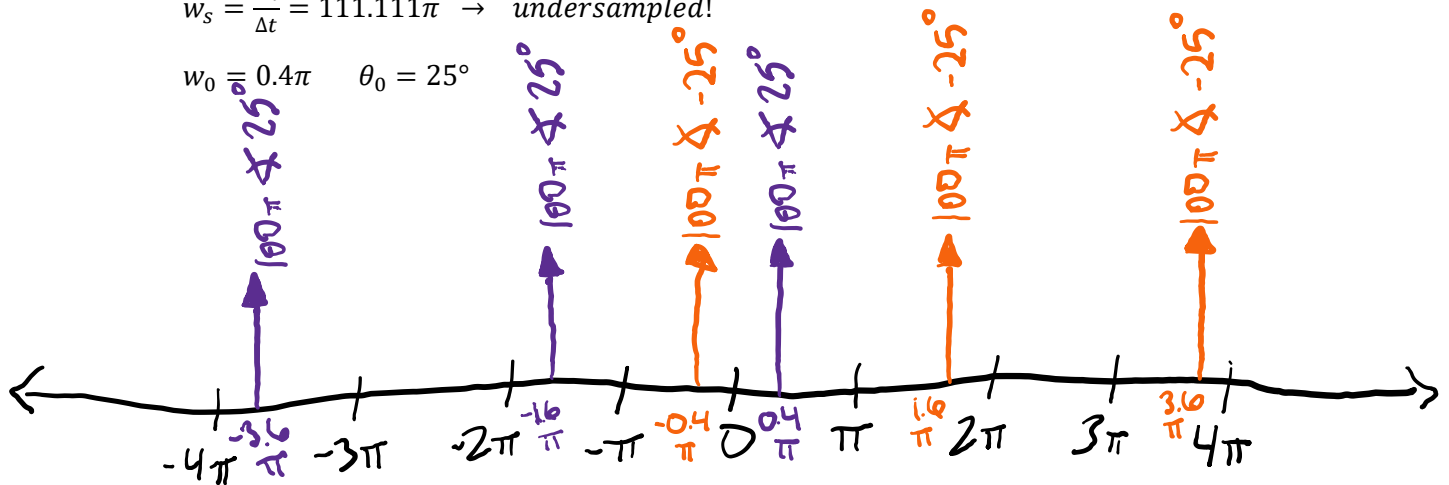
a)

$$T_s = \Delta t = 18ms = 0.018s$$

$$\hat{w}_A = 200\pi * 0.018 = 3.6\pi$$

$$w_s = \frac{2\pi}{\Delta t} = 111.111\pi \rightarrow \text{undersampled!}$$

$$w_0 = 0.4\pi \quad \theta_0 = 25^\circ$$



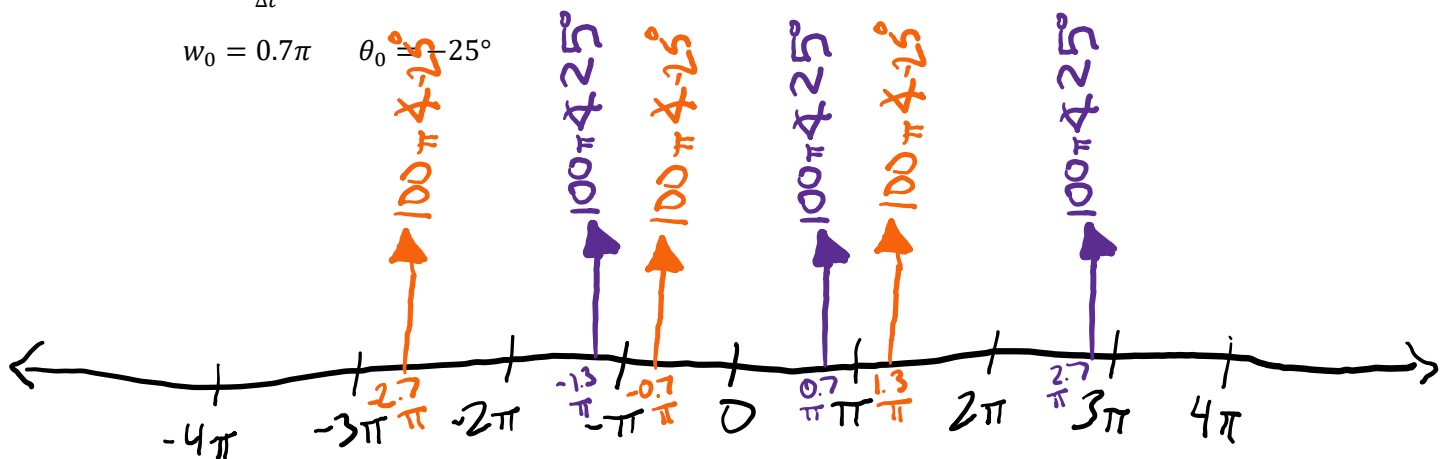
b)

$$T_s = \Delta t = 13.5ms = 0.0135s$$

$$\hat{w}_A = 200\pi * 0.0135 = 2.7\pi$$

$$w_s = \frac{2\pi}{\Delta t} = 148.148\pi \rightarrow \text{oversampled!}$$

$$w_0 = 0.7\pi \quad \theta_0 = 25^\circ$$



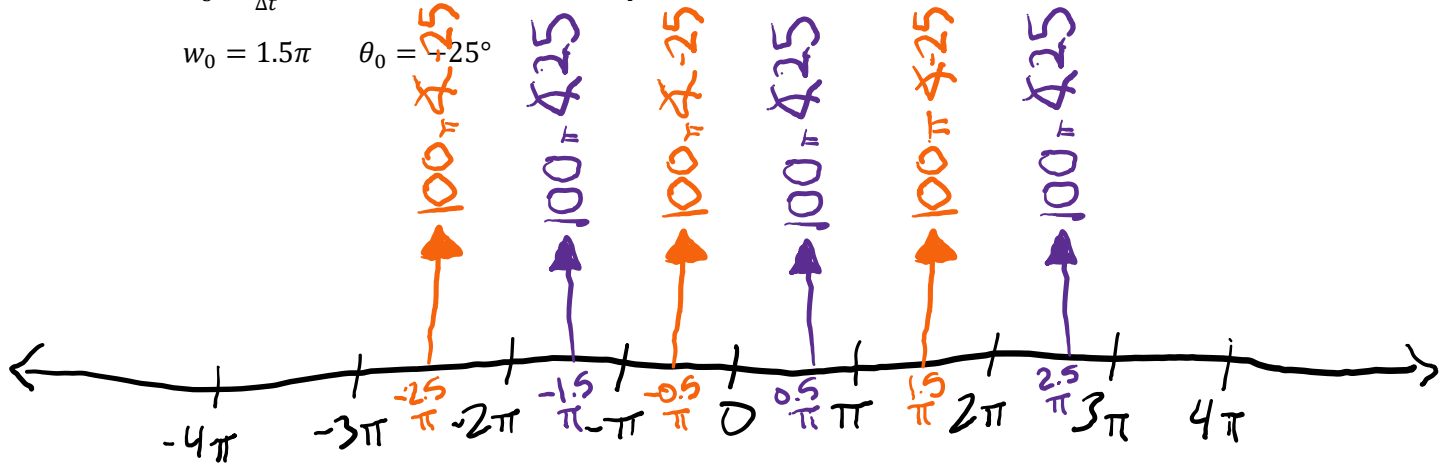
c)

$$T_s = \Delta t = 7.5 \text{ms} = 0.0075 \text{s}$$

$$\hat{w}_A = 200\pi * 0.0075 = 1.5\pi$$

$$w_s = \frac{2\pi}{\Delta t} = 266.666\pi \rightarrow \text{oversampled!}$$

$$w_0 = 1.5\pi \quad \theta_0 = +25^\circ$$



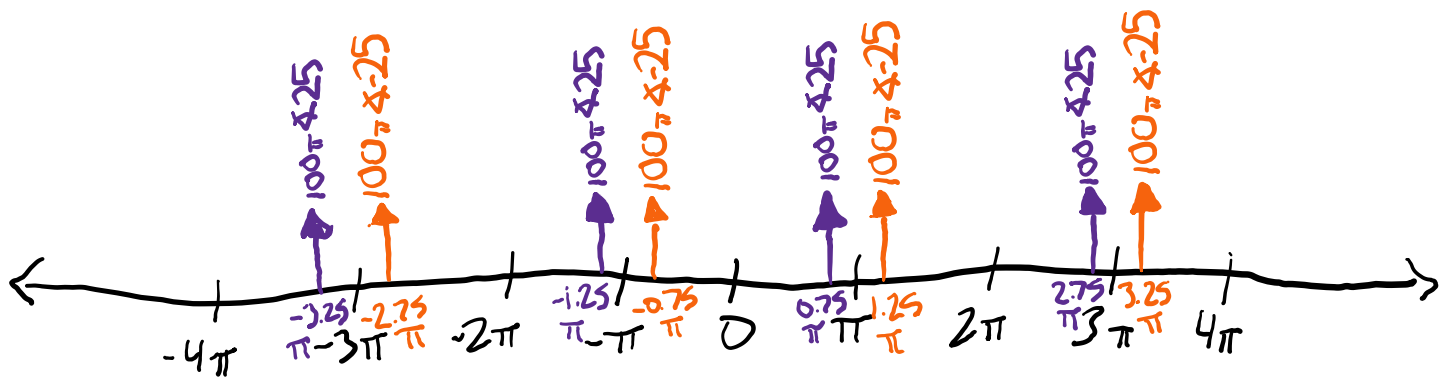
d)

$$T_s = \Delta t = 3.75 \text{ms} = 0.00375 \text{s}$$

$$\hat{w}_A = 200\pi * 0.00375 = 0.75\pi$$

$$w_s = \frac{2\pi}{\Delta t} = 533.333\pi \rightarrow \text{oversampled!}$$

$$w_0 = 0.75\pi \quad \theta_0 = -25^\circ$$



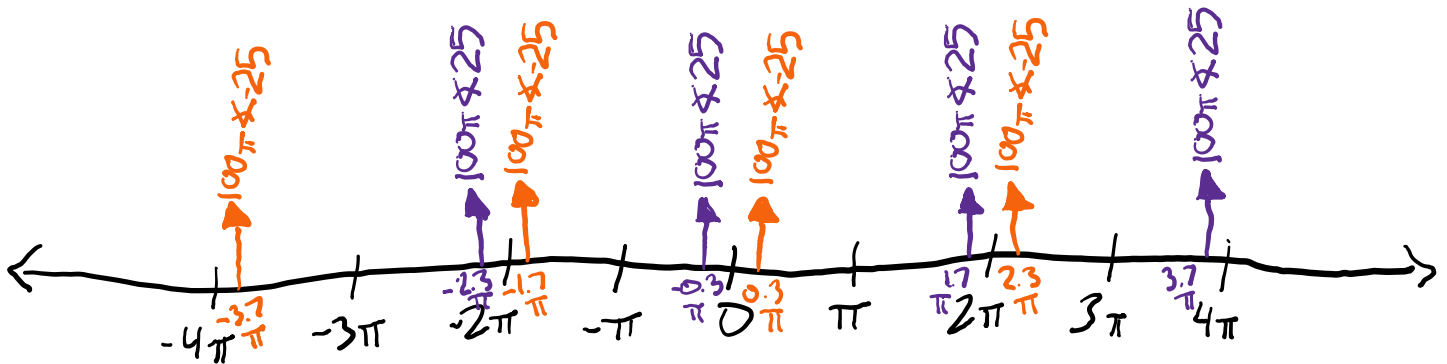
e)

$$T_s = \Delta t = 1.5 \text{ ms} = 0.0015 \text{ s}$$

$$\hat{w}_A = 200\pi * 0.0015 = 0.3\pi$$

$$w_s = \frac{2\pi}{\Delta t} = 1333.333\pi \rightarrow \text{oversampled!}$$

$$w_0 = 0.3\pi \quad \theta_0 = -25^\circ$$



Problem 2.3

a) $f_a[n] = \sum_{-5}^5 \sin(0.55\pi n + 17^\circ) \delta[n - q]$

b) $f_b[n] = \sum_{-3}^8 \sin(0.55\pi n + 17^\circ) \delta[n - q]$

c) $f_c[n] = \sum_0^\infty (0.353553\angle -45^\circ)^{n-1} \delta[n - q]$

d) $f_d[n] = \sum_3^\infty (1\angle -60^\circ)^{n-1} \delta[n - q]$

e) $f_e[n] = \sum_3^\infty (1\angle 60^\circ)^{1-n} \delta[n - q]$

Problem 2.4

a) $f_a[n] = \sin(0.55\pi n + 17^\circ)(u[n + 5] - u[n - 6])$

b) $f_b[n] = \sin(0.55\pi n + 17^\circ)(u[n + 3] - u[n - 09])$

c) $f_c[n] = (0.35\angle 45^\circ)^{n-1}(u[n])$

d) $f_d[n] = (1\angle -60^\circ)^{n-1}(u[n + 5])$

e) $f_e[n] = (1\angle 60^\circ)^{1-n}(u[n - 3])$