

1)

- a) $\neg \exists x P(x)$
- b) $\exists x \neg P(x)$
- c) $\exists x P(x)$
- d) $\exists x \exists y (x \neq y \wedge P(x) \wedge P(y))$
- e) $\forall x \forall y ((P(x) \wedge P(y)) \rightarrow x = y)$
- f) $\exists x P(x) \wedge \forall y (P(y) \rightarrow y = x)$
- g) $\forall x (P(x) \rightarrow Q(x))$
- h) $\forall x (Q(x) \rightarrow P(x))$

2)

- b) $(\exists a, b \in \mathbb{N}) [(x = a \times y + b \times z) \wedge (a = b)]$
- c) $(\forall m \in \mathbb{N}) [(y \mid m \wedge z \mid m) \rightarrow (\forall n \in \mathbb{N}) [(y \mid n \wedge z \mid n) \rightarrow (m \leq n)) \wedge (m = x)]]$
- d) $(x = 3) \vee (x = 1) \vee (\forall a, b \in \mathbb{N} [(x = a \times b) \rightarrow ((a = 1) \vee (b = 1))])$