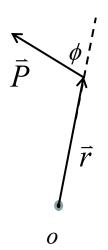
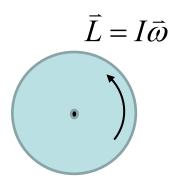
Angular Momentum

$$\vec{L} = \vec{r} \times \vec{P} = \vec{r} \times m\vec{V}$$
 for a pointlike particle $L = rmV \sin \phi$



$$\vec{L} = I\vec{\omega}$$
 for a rotating object $L = I\omega$



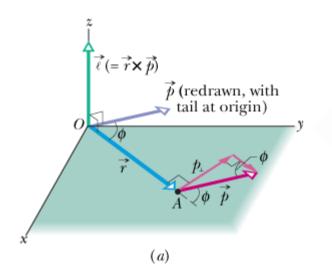
Angular Momentum

 $\vec{L} = \vec{r} \times \vec{P} = \vec{r} \times m\vec{V}$ for a pointlike particle

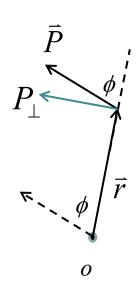
$$L = rmV \sin \phi$$

 $\vec{L} = I\vec{\omega}$ for a rotating object

$$L = I\omega$$







$$\vec{L} = I\vec{\omega}$$

 $\vec{L} = I\vec{\omega}$ for a rotating object

$$I = \frac{1}{2}MR^2$$
 for a disk

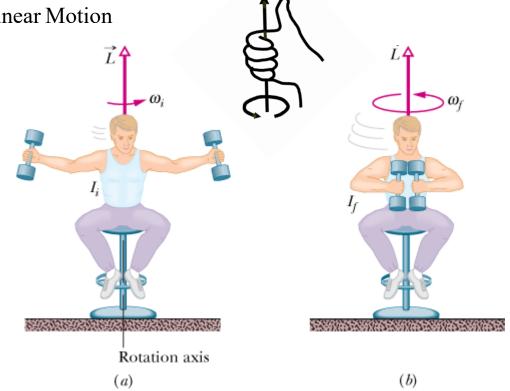
$$L = I\omega = \frac{1}{2}MR^2\omega$$

$$\vec{\tau}_{net} = \frac{d\vec{L}}{dt}$$
 Newton's 2nd Law in Angular Form

$$\vec{F}_{net} = \frac{d\vec{P}}{dt}$$
 Newton's 2nd Law in Linear Motion

When
$$\vec{\tau}_{net} = 0$$
,

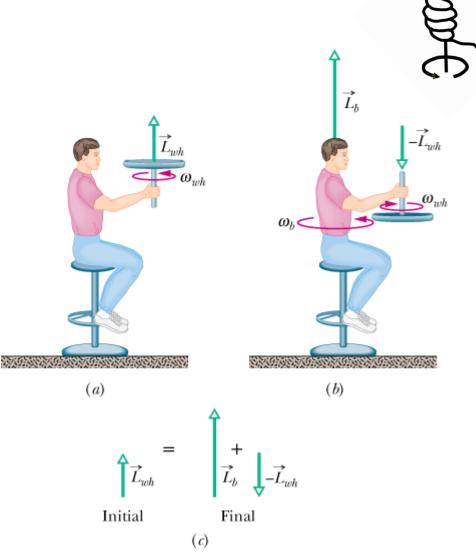
$$\vec{L}_i = \vec{L}_f$$



$$ec{L}_i = ec{L}_f$$
 $ec{L}_i = I_i ec{\omega}_i$ $ec{L}_f = I_f ec{\omega}_f$ Rotation axis

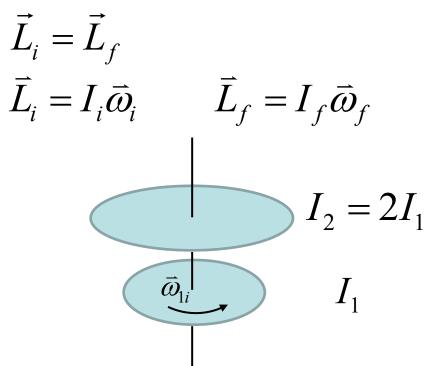
$$\vec{L}_i = \vec{L}_f$$

$$\vec{L}_{bi} + \vec{L}_{wi} = \vec{L}_{bf} + \vec{L}_{wf}$$



A wheel is rotating freely with an angular speed of 700 rev/min on a shaft whose rotational inertia is negligible. A second wheel, initially at rest and with twice the rotational inertia of the first, is suddenly coupled to the same shaft.

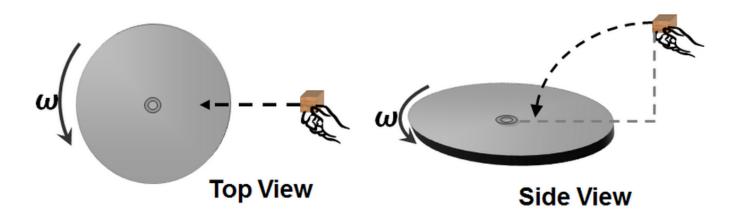
- (a) What is the angular speed of the resultant combination of the shaft and two wheels?
- (b) What fraction (written as a decimal) of the original rotational kinetic energy is lost?



$$\vec{L}_i = I_i \vec{\omega}_i = I_1 \vec{\omega}_{1i} + I_2 \cdot 0$$

$$\vec{L}_f = I_f \vec{\omega}_f = (I_1 + I_2) \vec{\omega}_f$$

The magnitude of the angular momentum for a freely rotating disk around its center is L. You drop a heavy block onto the disk along the direction as depicted below, and the block then stays on the disk. Now the magnitude of the angular momentum for the disk-block system is:

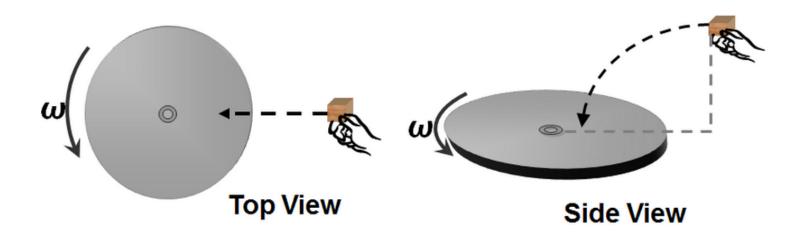


$$(1) > L$$
 $(2) < L$

$$(3) = L$$

(4) Not enough information to determine

The angular speed of a freely rotating disk around its center is ω . You drop a heavy block onto the disk along the direction as depicted below, and the block then stays on the disk. The angular speed of the disk-block system now:

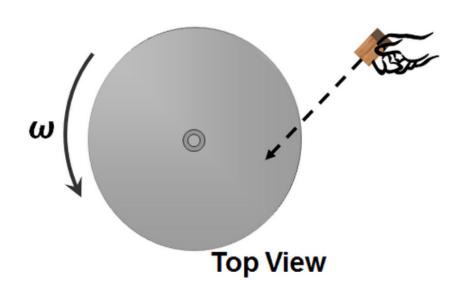


(1) decreases

(2) increases

- (3) remains the same
- (4) Not enough information to determine

The magnitude of the angular momentum for a freely rotating disk around its center is L. You drop a heavy block onto the disk along the direction as depicted below, and the block then stays on the disk. Now the magnitude of the angular momentum for the disk-block system is:



$$(1) > L$$
 $(2) < L$ $(3) = L$

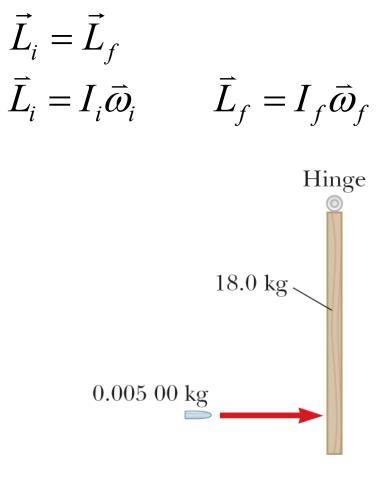
(4) Not enough information to determine

A 0.005-kg bullet traveling horizontally with speed 1000 m/s strikes an 18.0-kg door, imbedding itself 10.0 cm from the side opposite the hinges. The 1.00-m wide door is free to swing on its frictionless hinges.

(a) At what angular speed does the door swing open immediately after the collision?

$$\vec{L}_i = I_i \vec{\omega}_i = I_1 \vec{\omega}_{1i} + I_2 \cdot 0$$

$$\vec{L}_f = I_f \vec{\omega}_f = (I_1 + I_2) \vec{\omega}_f$$



A 0.005-kg bullet traveling horizontally with speed 1000 m/s strikes an 18.0-kg door, imbedding itself 10.0 cm from the side opposite the hinges. The 1.00-m wide door is free to swing on its frictionless hinges.

(a) At what angular speed does the door swing open immediately after the collision?

$$\vec{L}_i = \vec{r} \times \vec{p} + I_2 \cdot 0 \Rightarrow L_i = m_1 v_{1i} r$$

$$L_f = I_f \omega_f = (I_1 + I_2) \omega_f$$

$$= (m_1 r^2 + \frac{1}{3} m_2 L^2) \omega_f$$

$$(m_1 r^2 + \frac{1}{3} m_2 L^2) \omega_f = m_1 v_{1i} r$$

$$\begin{split} \vec{L}_i &= \vec{L}_f \\ \vec{L}_i &= I_i \vec{\omega}_i \qquad \vec{L}_f = I_f \vec{\omega}_f \end{split}$$

