

## ECE 3030 Spring 2025 HOMEWORK ASSIGNMENT NO. 7

Due: Friday, March 28<sup>th</sup> 11:59 pm upload to Carmen 3030 SpeedGrader

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1. (15 pts) Calculate the capacitance for the following Si  $n^+$ -p junction.  
 $N_a = 10^{15} \text{ cm}^{-3}$ ; Area =  $0.001 \text{ cm}^2$ ; Reverse bias  $V_R = 1, 5, \text{ and } 10 \text{ V}$ .  $\epsilon = 11.8 \epsilon_0$ . Plot  $1/C^2$  vs.  $V_R$ ; Demonstrate that the slope yields  $N_a$ . Repeat calculations for  $N_a = 10^{17} \text{ cm}^{-3}$ . Since  $n^+$  doping is not specified, approximate with  $E_F^n \sim \frac{1}{2} E_G$ .
2. (15 pts) A  $p^+$ -n Si junction is doped with  $N_d = 3 \times 10^{16} \text{ cm}^{-3}$  on the n side, where  $D_p = 10 \text{ cm}^2/\text{s}$  and  $\tau_p = 0.1 \text{ } \mu\text{s}$ . The junction area is  $10^{-4} \text{ cm}^2$ . Find (a) the junction capacitance  $C_j$  with a reverse bias of 10 V, and (b) the charge storage capacitance  $C_s$  with a forward bias of 0.6 V, where  $C_s = qI \tau_p / kT$
3. (15 pts) Modify the  $x_{po}$  and  $x_{no}$  expressions for the case of reverse bias  $V_r \gg V_0$  and show that the peak electric field  $\mathcal{E}_0$  is dominated by the doping on the lightly doped side of the junction. Solve for  $V_r$  for a  $p^+$ -n junction. If avalanche occurs at a peak field of about 400 kV/cm in a Si  $p^+$ -n junction doped with  $10^{16} \text{ cm}^{-3}$  donors on the n side, what is the breakdown voltage?
4. (15 pts) If the critical field for Zener breakdown is  $10^6 \text{ V/cm}$ , calculate the reverse bias required for this type of breakdown in the following abrupt Si junction:  $N_a$  on the p side =  $N_d$  on the n side =  $4 \times 10^{18} \text{ cm}^{-3}$ . Assume that breakdown can occur if the peak electric field in the junction reaches  $10^6 \text{ V/cm}$ .
5. (10 pts) A  $p^+$ -n Si diode ( $V_0 = 0.956 \text{ V}$ ) has a donor doping of  $10^{17} \text{ cm}^{-3}$  and an n-region width =  $1 \text{ } \mu\text{m}$ . Does it break down by avalanche or punch through ( $W > 1 \text{ } \mu\text{m}$ )? From Lecture 23, slide 6 (S&B Fig. 5-22), avalanche  $V_{br} = 13 \text{ V}$ .
6. (15 pts) An ideal Schottky barrier is formed on n-type Si with  $N_d = 10^{17} \text{ cm}^{-3}$ . The metal work function is 4.8 eV, and electron affinity is 4 eV. Draw equilibrium diagrams such as in S&B Fig. 5-40 to scale. Draw the forward- and reverse-bias diagrams, as in Fig. 5-42 to scale, for  $V_f = 0.3 \text{ V}$  and  $V_r = 3 \text{ V}$ .
7. (15 pts) A Schottky barrier is formed between a metal having a work function of 4.3 eV and p-type Si. The acceptor doping in the Si is  $10^{17} \text{ cm}^{-3}$ . (a) Calculate  $V_0$  and draw the equilibrium band diagram, illustrating  $V_0$ , (b) Draw the band diagram with 0.3 V forward bias. Repeat for 2 V reverse bias.
8. (10 pt Bonus) Design an abrupt Si  $p^+$ -n junction that has a reverse breakdown voltage of 150 V and provides a forward current of 1 mA when  $V = 0.6 \text{ V}$ . Solve for square or circle area A. Assume that n-side  $\tau_p = 0.1 \text{ } \mu\text{s}$  and that  $\mu_p \sim 450 \text{ cm}^2/\text{V-s}$  from S&B fig. 3-23.