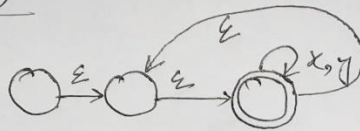


Name : MD Nahid Hasan

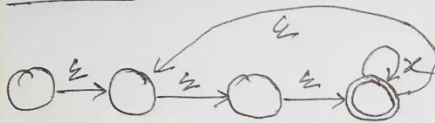
ID : 21-45018-2

1) $(x \cup y)^* \cup (x^* \cup y^*)x$ RE to NFA

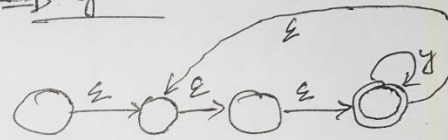
$\Rightarrow (x \cup y)^*$



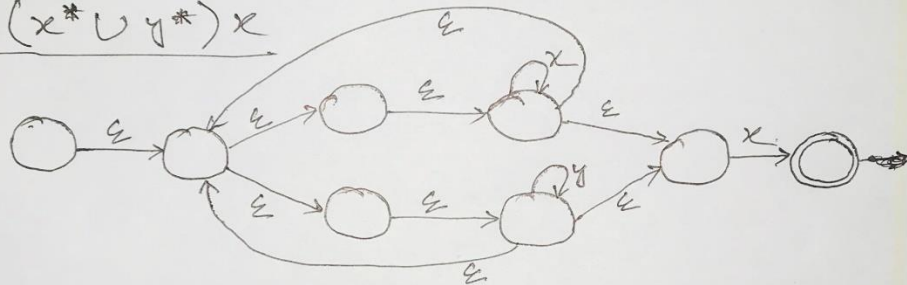
$\Rightarrow x^*$



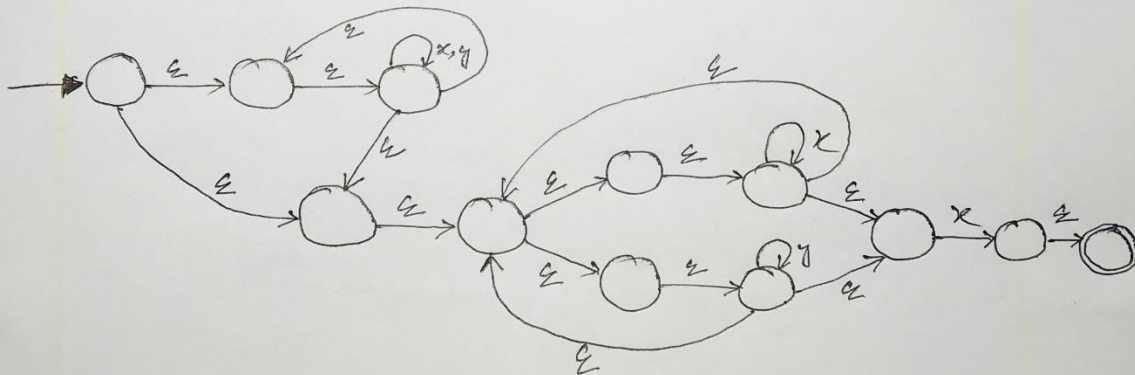
$\Rightarrow y^*$



$\Rightarrow (x^* \cup y^*)x$



$\Rightarrow (x \cup y)^* \cup (x^* \cup y^*)x$



(Ans)

$$\begin{aligned}
 2) \{ w \mid \text{each } a \text{ in } w \text{ is followed by exactly three } b \} \\
 &= \{ abbb, abbbabbb, babbb, bbbabbbabbb, \dots \} \\
 &= \{ (b^*)^{\bullet} \cup a(bbb)^* \}
 \end{aligned}$$

So, w can start with either zero or more b 's or it can start with a and followed by 3 b 's.

$$3) \textcircled{1} cddcc(cud)^*$$

$$= \{ w \mid w \text{ ~~can~~ starts with substring "cddcc" ^{and} ends with either } c \text{ and } d. \}$$

$$\textcircled{2} (cud)(cud)^*$$

$$= \{ w \mid w \text{ starts with either } c \text{ or } d \text{ and ends with either } c \text{ or } d. \}$$