MAE 112 Fall 2042 Homework Assignment #3

Due: 11:59 pm, Sunday, October 27, 2024 Follow submission instructions from TAs

- 1. A rocket nozzle has initial pressure and temperature of fifty atmospheres and 5000°R with $\gamma = 1.25$; $c_p = 0.30$ Btu/1bm °R; and A* = 1.5 ft². The flow is slightly over-expanded to a Mach number $M_e = 3.5$ at the nozzle exit with the ambient pressure at 0.50 atmosphere. Assume 95% for nozzle polytropic efficiency. Calculate: (a) the characteristic velocity c*; (b) the mass flow; (c) nozzle exit pressure and cross-sectional area (beware of tables and graphs constructed for air flow); (d) nozzle exit velocity U; and (e) effective exhaust velocity c.
- 2. Consider a nozzle with initial upstream entry pressure and temperature of thirty atmospheres and $4000^{\circ}R$. The value of $\gamma = 1.2$ and the value of $c_p = .30$ Btu/1bm $^{\circ}R$. The throat area is 0.75 ft². The flow is perfectly expanded to the ambient pressure of 0.70 atmospheres. Calculate: (a) the mass flow, (b) the exhaust velocity, (c) the exit area, and (d) the thrust coefficient.
- 3. Consider a rocket engine that uses liquid oxygen and liquid ethanol (C_2H_5OH) fuel aka ethyl alcohol. The oxygen mass-flow rate is 2.0 times greater than the fuel mass-flow rate. Ethanol is stored at 298K while the oxygen is stored at 80K just slightly below its boiling point. Oxygen has a heat of vaporization of 6.81kJ/mole while the value for ethanol is 38.6 kJ/mole. The heat of formation of liquid ethanol is -277.0 kJ/mole. The specific heat at constant pressure for gaseous oxygen is 30.77 joules/mole $^{\circ}$ K. The liquids are sprayed into the combustion chamber.
 - (a) How much energy per mole is required to vaporize and heat a mole of oxygen to the temperature of 298K.
- (b) What is the expected ideal flame temperature? The ideal flame temperature aka theoretical flame temperature is the value with no dissociation. Assume that the products are H₂O, CO₂, and CO. You should make this calculation without using the online computer code. A key step is to determine what fraction of the carbon will appear in CO₂ and what fraction will appear in CO.
- 4. Suppose we have a rocket combustor that has hot products produced at the following conditions:

T = temperature = 4600 ° R P = pressure = 75 atmospheres γ = ratio of specific heats = 1.25 MW = average molecular weight = 27

(a) Design a nozzle that will produce 75,000 pounds of thrust with an ambient pressure of one atmosphere. In particular, determine the following quantities: mass flow rate, exit pressure, exit or exhaust velocity, effective exhaust velocity, thrust coefficient, throat cross-sectional area, and exit cross-sectional area.

- (b) Design a nozzle that produces 100,000 pounds of thrust with an ambient pressure at vacuum conditions. Limit the nozzle exit cross-sectional area to no more than thirty times the throat cross-sectional area. Determine the same quantities as described in Part (a).
- 5. Consider a jet engine flying at a Mach number of 1.4. A normal shock sits at the entrance of the divergent diffuser. The diffuser entrance cross-sectional area is 2.5 ft². The ambient conditions are 500°R for temperature and 0.8 atmosphere for pressure.
- (a) What is the stagnation pressure immediately in front (upstream) of the shock? What is the stagnation pressure immediately behind (downstream) the shock? What is the Mach number immediately behind the shock? What is the mass flow through the diffuser?
- (b) What is the minimum cross-sectional area required at the downstream end of the diffuser in order to assure that the Mach number of the flow there does not exceed 0.10?