

Haskell Tutorial

A guide to Haskell basics

Ruben Saunders

Contents

1	Intr	roduction	1
	1.1	Language Overview	1
	1.2	Installation	1
		1.2.1 The Haskell Toolchain	1
		1.2.2 Install Command	1
2	Eval		2
	2.1	V	2
	2.2		2
			2
			2
			3
	2.3	Sharing	3
	2.4	Normal Form	3
		2.4.1 Weak Head Normal Form	4
3	Vari		5
	3.1	Local Name Binding	5
		3.1.1 let	5
		3.1.2 where	5
4	Fun		6
	4.1		6
			6
			6
	4.2	11	7
	4.3	Recursion	7
		4.3.1 Defined Base Case	7
		4.3.2 If-Else Expression	7
		4.3.3 Guards	7
		4.3.4 Accumulators	8
	4.4	Lambdas	8
	4.5	Higher Order Functions	8
			8
	4.6	· ·	9
	4.7		9
	4.8	v e	9
		v G	9
	4.9	Function Composition	
5	Typ	pes 1	1
	5.1	Variable Types	1
		5.1.1 Lists	1
	5.2	Function Types	1
		5.2.1 Type Variables	1
	5.3	Type Aliasing	1
	5.4	Type Classes	1
		5.4.1 Definition	
		5.4.2 Implementation	
		5.4.3 Common Type Classes	
		5.4.4 Instances	
		5.4.5 Derivation	
	5.5	Defining Datatypes	
	J.J	5.5.1 Examples	
	5.6	Records	
	5.0	5.6.1 Multiple Constructors	
		- 0.0.1	J

6	Use	ful Types	14
	6.1	Maybe	14
	6.2	Either	14
7	Coll	ections 1	15
	7.1	Lists	15
		7.1.1 Construction	15
		7.1.2 Pre-defined functions	15
		7.1.3 List Comprehension	16
			16
	7.2		16
	•		
8	Kin	${ m ds}$	L 7
9	Mod	lules	18
	9.1		18
	0.1		18
		•	18
		1	18
	9.2	0 1	18
	9.2	Importing Datatypes	LO
10	Typ	e Classes	۱9
			19
		0 1	19
			19
		-	19
	10.3		20
	10.0		20
	10.4	•	20
			20
	10.5		
			21
			21
			22
			22
		V	22
		10.5.6 Kleisli-Composition	22
11	T /O	e	
11	I/O		23
		v -	23
		•	23
		•	23
		9	23
	11.5		23
			23
		11.5.2 Environment Variables	24
		11.5.3 Error Handling	24
	11.6	Files	24
12	Тур	e Families	25

1 Introduction

Haskell is a purely functional programming language. The following sections will give a brief overview of Haskell, and how to install it.

1.1 Language Overview

In Haskell, everything is a *pure* function - that is, they abide by the Mathematical definition of a function; they map inputs to a unique output.

Data is immutable, meaning that our data types cannot be changed in-place. Combined, this means that there a re few or no side-effects from functions, which make programming more simple.

Haskell is declarative, meaning that the program defines what the issue is, rather than simply giving an algorithm to solve a problem.

Functional programs are easier to verify as we can use maths to verify an algorithm.

1.2 Installation

Link: https://www.haskell.org/ghcup/ I used GHCup to install several components of the Haskell toolchain.

1.2.1 The Haskell Toolchain

The Haskell Toolchain consists of several useful tools for Haskell compilatio and development:

- GHC the Glasgow Haskell Compiler;
- cabal-install Cabal installation tool for managing Haskell software;
- Stack a cross-platform proram for developing Haskell projects;
 - Msys2 provides a UNIX shell and environment which is necessary for executing configuration scripts.
- haskell-language-server a language server which may be integrated into an IDE;

1.2.2 Install Command

The command to use on Windows (in a normal Powershell instance) is

```
Set-ExecutionPolicy Bypass -Scope Process -Force; [System.Net.ServicePointManager
]::SecurityProtocol = [System.Net.ServicePointManager]::SecurityProtocol -bor
3072; try { Invoke-Command -ScriptBlock ([ScriptBlock]::Create((
    Invoke-WebRequest https://www.haskell.org/ghcup/sh/bootstrap-haskell.ps1 -
    UseBasicParsing))) -ArgumentList $true } catch { Write-Error $_ }
```

2 Evaluation

This section will explain how Haskell evaluates its expressions and is fundamental to understanding how the language operates.

In summary, Haskell employs lazy evaluation which uses outermost reduction and sharing.

2.1 Lazy Evaluation

Haskell is lazy. This means that it will only evaluate an expression when that expression is required; otherwise, the expression is stored in an un-evaluated form as a *thunk*.

An un-evaluated expression may be viewed in GHCi using :sprint <expr>. Underscores represent thunks which have not been evaluated.

To evaluate an expression, Haskell recursively reduces terms and applies atomic calculations where necessary (operations such as + and * on numeric types).

2.2 Reductions

This is the technique Haskell uses to evaluate expressions. The idea is that anything appearing on the left-hand side of = may be replaced by its right-hand side (and vice versa). Pattern matching is used in more complex replacements.

Example:

```
square :: Int -> Int
 2
  square x = x * x
 3
 4
   f :: Int -> int -> Int
 5
  f x y = y + square x
 6
 7
  155 + f 94 10
                            -- Apply definition of 'f'
8
  = 155 + 10 + square 94 -- Apply definition of 'square'
  = 155 + 10 + 94 * 94
 9
                            -- Atomic operation '(*)'
1.0
  = 155 + 10 + 8836
                            -- Atomic operation '(+)'
  = 155 + 8846
                            -- Atomic operation '(+)'
11
   = 9001
                            -- Fully evaluated
12
```

As Haskell functions are mathematically pure, the order of reduction does not matter- the end result is the same. We could reduce 155 + 10 before applying square and the result would still be the same. This is known as the *Church-Rosser* theorem and applies to some variants of lambda-calculus. There are two reduction variants.

2.2.1 Innermost Reduction

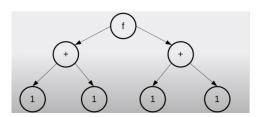
Fully evaluate the arguments of a function before the function definition is applied.

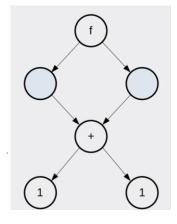
2.2.2 Outermost Reduction

Fully apply function definitions first.

2.2.3 Graph Reduction

This is all good in theory, but how does Haskell *actually* evaluate a program? Under the hood, haskell uses graph reduction. Essentially, every expression and equation in Haskell is part of a large graph structure. Each vertex contains either a function which can be reduced, or an atomic value. To deal with sharing, each non-value vertex points to a placeholder vertex where the result will be stored, which i turn points to the expression. Therefore, *sharing* is where two or more placeholder vertices point to the same expression.





2.3 Sharing

Possible due to lack of side effects, sharing results in any equivalent thunks only being evaluated once. This is done by *memoising* evaluated thunks to avoid re-evaluation of equivalent thunks in the future.

2.4 Normal Form

An expression is in a normal form iff it is fully evaluated (i.e. no further reductions can be applied). Examples:

```
1 | 1 + 1 => 2
2 | (1, 2+2) => (1, 4)
3 | [True && False] => [False]
4 | (\x -> x * 10) -- Already in normal form!
```

Note that the following are not in normal form:

• Function definitions. Expand the definition into a value.

```
\begin{array}{l} 1 \\ f \\ x = \dots \\ 2 \\ -- \\ Becomes \\ 3 \\ f = \\ x \rightarrow \dots \end{array}
```

• Top-level pattern matching. Expand into a case .. of .. expression.

```
1  f <p1> = <e1>
2  f <p2> = <e1>
3  -- Becomes
4  f = \x -> case x of
5  p1 -> e1
  p2 -> e2
```

2.4.1 Weak Head Normal Form

An expression which is fully evaluated up to at least the first data constructor. Values/equations in WHNF are:-

- 1. A data constructor
- 2. A built-in function applied to too few arguments e.g. (+ 2)
- 3. A lambda expression

```
1 1 + 1 => 2
2 (1, 2+2) -- In WHNF as values are inside a data constructor
3 [True && False] => _ : _ -- The values do not matter. Only the constructor '(:)'
    matters in WHNF.
```

The seq function is strict in its first argument - it enforces its first argument to be evaluated to WHNF. This function is defined this way explicitly in GHC and is one of the only functions to do this.

3 Variables

Variables are name-bounded values. Variables in Haskell are immutable - they cannot be changed.

```
name = <value>
```

Variable types are inferred. To explicitly assign variables a type,

```
name :: Type
```

In GHCI, the type of a symbol may be retriesed by :t name.

3.1 Local Name Binding

Two methods are provided to bind a symbol to a value in a local scope: let and where. Each follow a "main" expression.

3.1.1 let

Syntax:

For example, re-define in_range as follows:

```
in_range x min max =
let
    in_lb = min <= x
    in_ub = max > x
in
    in
    in_lb && in_ub
```

3.1.2 where

Syntax:

For example, re-define in_range as follows:

```
1   in_range x min max = in_lb && in_ub
2   where
3   in_lb = min <= x
4   in_ub = max > x
```

4 Functions

Functions are defined to map a value from an input set - the *domain* - into an output set - the co-domain. Every output of the function is contained in a subset of the co-domain, called the *range*. **Pure** mathematical functions must be able to map every value from the domain, and each input value must map to only one output value.

In Haskell, occurences of functions are expanded into their RHS.

4.1 Function Definition

Functions are defined by providing its name, a list of arguments, and setting it equal to an expression.

```
name arg1 arg2 ...argn = <expr>
```

The arguments may be set to constants, or may be given a name to accept a variable value.

The type of a function is specified by an arrow (->) seperated list of its argument types and its return type:

```
func :: type<sub>1</sub> -> type<sub>2</sub> -> ...-> type<sub>n</sub> -> type<sub>return</sub>
```

For an example, take a function which returns the sum of the elements of an array:

```
sum :: [a] -> Int -- Takes an array of arbitrary type and returns an integer
sum [] = 0 -- Define the sum of an empty array to be zero
sum (h:t) = h + sum t -- Define the sum of an array to be the head plus the sum of the tail
```

4.1.1 Infix Functions

A good example of infix functions are operators such as +. Functions which take two arguments may be writen between the arguments instead.

For example, say we had add a b = a + b. Then add 5 7 and 5 `add` 7 are equivalent.

To reference the function defined by an operator i.e. +, surround it with parenthesis i.e. (+).

The associativity and precedence of infix operators may be changed via infixr/infixl <function name> where $0 < prec \le 9$.

4.1.2 Pattern Matching

Parameters of functions may be matched against a pattern. Note that order matters: more specific patterns should be defined first, with general cases last.

- Accept any value by using a symbol e.g. $f x = \dots$
- Accept a certain value e.g. $f 0 = \ldots, g [] = \ldots$
- List splicing using (x:xs) where x is the head, xs is the tail.
- Tuple unpacking e.g. (Int, Int) could be unpacked using (x, y).
- Accept and extract a custom types. E.g., say we had type Pos = (Int, Int), we would define getX (x, y) = x.
- Accept and extract a custom datatype. E.g., say we had data Num = Zero | Succ Num. We could then define f Zero = ... and f (Succ n) =

Pattern matching may also be done using case ... of ... construct.

4.2 Function Application

A function is applied (called) to some arguments as follows:

```
name arg1 arg2 ...argn
```

For example, consider the function in_range x min max = x >= min && x < max, an implementation of $x \in [min, max)$.

Then, in_range 3 0 5 would evaluate to True, but in_range 5 0 5 would evaluate to False.

4.3 Recursion

Recursion is the process of a function calling itself. Recursion requires a *base case* to stop the function recursing indefinitely.

There are many ways to implement recursion, which will be demonstrated using the factorial, defined as

$$n! = n \cdot (n-1) \cdot \ldots \cdot 1 = \prod_{k=1}^{n} k$$

4.3.1 Defined Base Case

We can hard-code the case where the function is called with the base case:

```
1 fac 1 = 1
2 fac n = n * fib (n-1)
```

4.3.2 If-Else Expression

We can use the if-else expression:

```
if <expr> then <ifTrue> else <ifFalse>
```

For example,

```
1 fac n = if n \le 1 then 1 else n * fac (n-1)
```

4.3.3 Guards

Guards are similar to piece-wise functions.

Where <expr> is a boolean expression. If <expr> is matches, then <value> will be returned. If none is matched, the otherwise is returned. For example,

4.3.4 Accumulators

In this example, we define an auxiliary function aux inside fac to calculate the the factorial

This is called *tail recursion*. This is because the final result of aux is the result we want, meaning that it is much more memory efficient. A good compiler could even unwind this into a non-recursive imperative approach using a loop. (For more insight, see https://www.youtube.com/watch?v=_JtPhF8MshA.)

Normal recursion (using an above definition of fac):

```
fac 4
= 4 * fac 3
= 4 * (3 * fac 2)
= 4 * (3 * (2 * fac 1))
= 4 * (3 * (2 * 1))
= 4 * (3 * 2)
= 4 * 6
= 24
```

Tail recursion (using the definition in this sub-section):

```
fac 4
= aux 3 4
= aux 2 12
= aux 1 24
= 24
```

4.4 Lambdas

Syntax:

Some examples:

- $(\x -> x+1)$ 2 returns 3.
- $(\xyz -> x+y+z)$ 1 2 3 returns 6.

Lambdas may be bound to names.

4.5 Higher Order Functions

Higher order functions are functions that take other functions as arguments. For example, a function which takes another function and applies it to an argument:

```
1 app :: (a -> b) -> a -> b
2 app f x = f x
```

A synonym of such a function is the dollar (\$) operator: (\$) :: (a -> b) -> a -> b.

4.5.1 Useful Higher Order Functions

• map :: (a -> b) -> [a] -> [b] applies a function to every element on an array.

$$L' = \{ f(x) : x \in L \}$$

Example: map $(\x -> x^2)$ [1,2,3] returns [1,4,9].

• filter :: (a -> Bool) -> [a] -> [a] filters the list on a predicate.

$$L' = \{x \in L : P(x)\}$$

Example: filter (x -> mod x 2 == 0) [1,2,3,4,5] returns [2,4].

• fold :: (a -> b -> b) -> b -> [a] -> b processes a list with some function to produce a single value, starting at a given value.

In Haskell, fold doesn't exist, but rather foldr and foldl wherein the position of the base value is different

```
foldr f a [] = a
foldr f a (x:xs) = f x (foldr f a xs)
-- foldr f a [x1, x2, ..., xn] = (x1 'f' (x2 'f' (... (xn 'f' a))))

foldl f a = []
foldl f a (x:xs) = f (foldl f a xs) x
-- foldl f a [x1, x2, ..., xn] = (...((a 'f' x1) 'f' x2) 'f' xn)
```

See code/folding.hs

Example: foldr (+) 0 [1,2,3,4,5] returns 15.

4.6 Currying

The principle behind currying is that given

We could re-write this as

$$f'$$
 :: a -> (b -> (c -> d))

For example, one could define a function add in multiple ways:

```
1 add x y = x + y

2 add x = (\y -> x + y)

3 add = (\x -> (\y -> x + y))
```

4.7 Currying

```
1 curry :: ((a,b -> c) -> a -> b -> c)
2 curry f x y = f (x,y)
```

4.8 Uncurrying

```
1 uncurry :: (a -> b -> c) -> (a,b) -> c
2 uncurry f (x,y) = f x y
```

4.8.1 Partial Function Application

Using the last definition of add, consider the result of add 1. This would be a new function; add 1:: Int -> Int. This is known as a section.

A good example would be using map.

```
doubleList = map (\x -> x * 2)
```

4.9 Function Composition

Function composition is a way to combine functions. For this, we use the dot (.) operator.

```
(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow (a \rightarrow c)
```

Then, (f.g) is equivalent to $(\x -> f (g x))$.

For example, all three definitions of descSort are equivalent:

```
descSort = reverse . sort
descSort = (\x -> reverse (sort x))
descSort = reverse (sort x)
```

5 Types

Every expression in Haskell has a type. Types are inferred, even when given explicitly.

Types always begin with an UPPERCASE letter.

The cardinality of a type is how many *states* the data type could hold. Polymorphic types have no cardinality.

5.1 Variable Types

```
var :: type
```

5.1.1 Lists

To define a list of a type, one would write [type]. This may be nested.

5.2 Function Types

```
func :: type1 -> ... -> typeN -> ret_type
```

Where the function func takes n arguments of types type1, ..., typeN and returns ret_type.

5.2.1 Type Variables

Type variables may be used where any type would be permissable and must be lowercase. For example,

id ::
$$a \rightarrow a$$

id $x = x$

This is called "parametric polymorphism".

5.3 Type Aliasing

This doesn't define a new datatype, but rather an alias for another type.

```
type Pos = type
```

A common example is using a tuple e.g. type Pos = (Int, Int). The type name need not be stated in pattern matching.

5.4 Type Classes

Type classes may be used to restrict the types a polymorphic function may take. This is useful if we would like to use features in a polymorphic function that may only be available to certain types. For a type to be a member of a type class, it must implement all of the required methods.

To impose a constraint on variable a in a function f: f:: (<TypeClass> a, ...) => This is called "ad-hoc polymorphism".

5.4.1 Definition

A type class definition begins with

```
class <Name> <var> where
```

Below is a list of function declarations. For a type to be a member of <Name>, it must implement all of these functions.

5.4.2 Implementation

To define a new type which belongs to a type class: instance <TypeClass> <TypeName> where Where below this is a list of function definitions.

5.4.3 Common Type Classes

Common type classes include:

- Eq types which may be compared i.e. (==) is defined;
- Num numeric types, gives us access to standard mathematical operations i.e. (+), (-), (*), abs, ... are defined;
- Ord types which may be ordered, imposes a total ordering i.e. (<), (>), (<=) are defined;
- Read types which may be converted from a string i.e. read is defined;
- Show types which may be converted to a string i.e. show is defined;
- Integral types which are integer-like i.e. div, ... is defined;
- Floating types which are float-like i.e. (/), ... is defined;
- Enum types which may be enumerated i.e. succ, pred, ... are defined;

N.B. for information on complex type classes, see Type Class section

5.4.4 Instances

Intances allow us to write functions which make use of type classes. Syntax: instance (<constraints>) => <typeClass> <value> where followed by a list of function definitions.

5.4.5 Derivation

The deriving keyword can be used to automatically generate implementations for the given type class(es).

```
Syntax: data <Name> = ...deriving (<Class1>, ...) 
Example: data Shape = Circle Int | Rect Int Int deriving Show. Then, print (Circle 5) \rightarrow Circle 5.
```

5.5 Defining Datatypes

The data keyword is used to define a new datatype; unlike the above, these are entirely custom. This may be done using the data keyword:

```
data Name = Constructor1 [<args>] | ...
```

where <args> are the types of each argument, not literals.

Constructors are either plain values, or functions which take args and return the datatype.

Data consturctors can include polymorphism by including type variables after <Name> e.g. data Maybe a = Nothing | Just a.

5.5.1 Examples

- rock-paper-scissors.hs A basic example revolving around Rock-Paper-Scissors;
- expr.hs A program to build and evaluate expressions;
- tree.hs A representation of a tree structure;
- nat-num.hs A definition of natural numbers using the successor function;

5.6 Records

Records allow data to be stored with an associated name. Syntax:

```
data <Name> = <Name> { <field> :: <type>, ...}
```

This will automatically generate functions <field> :: <Name> -> <type> to extract said properties. This has the side-effect that field names must be globally unique.

5.6.1 Multiple Constructors

```
Note that records may also have multiple constructors,

data Point = D2 { x :: Int, y :: Int } | D3 { x :: Int, y :: Int, z :: Int}

}

Duplicate field names in this context is OK.
```

This will generate functions x, y and z all with the signature x/y/z:: Point -> Int. Both x and y will work on either D2 or D3, but applying z to D2 will throw an exception. For an example, see code/vector.hs.

6 Useful Types

This section will list some common, useful types which should be known.

6.1 Maybe

The Maybe type is incredibly useful, as it can be used to represent the *absence* of a value. This is useful when our function is passed invalid data, for example.

If it defined as: data Maybe a = Nothing | Just a

Functions Found inside Data. Maybe.

- isJust :: Maybe a -> Bool returns if the passed Maybe is a Just value;
- fromMaybe :: a -> Maybe a -> a returns the Just value if a value is present, else returns the default value;
- fromJust :: Maybe a -> a returns the Just value, or throws an exception if recieved Nothing;
- catMaybes :: [Maybe a] -> [a] returns a list containing all the Just values.
- mapMaybe :: (a -> Maybe b) -> [a] -> [b] maps a function over a list of Maybes, discarding any Nothings;
- maybe :: b -> (a -> b) -> Maybe a -> b takes a maybe. If Just, applies a function and returns. Else, returns a default;

6.2 Either

The Either type can be used to represent a union of types – a value which is either one type, or another. It is defined as data Either a b = Left a | Right b

Functions Found inside Data. Either.

- lefts :: [Either a b] -> [a] returns an array of left-hand side values;
- rights :: [Either a b] -> [b] returns an array of right-hand side values;
- isLeft :: Either a b -> Bool returns whether the provided value is a left-hand side value;
- isRight :: Either a b -> Bool returns whether the provided value is a right-hand side value;
- fromLeft :: a -> Either a b -> a returns the left-hand side value if a Left is provided, else returns a default;
- fromRight :: n -> Either a b -> n returns the right-hand side value if a Right is provided, else returns a default;
- either :: (a -> c) -> (b -> c) -> Either a b -> c processes the left- or right-hand value in the Either as per the given functions;
- partitionEithers :: [Either a b] -> ([a],[b]) traverses the list, placing and Left values in one list and any Right values in another;

 $Use-Error\ Handling$ Either can be used in place of Maybe for error handling. Left can represent a correct input/output with Right holding the incorrect value.

7 Collections

Haskell has two collections: lists, and tuples.

7.1 Lists

A mutable collection of elements of the same type. Every elements has an ordinal. A list of type type has the given type signature

```
name :: [type]
```

7.1.1 Construction

A list may be greated by the following constructor:

- Using square brackets: $[x_1, x_2, \ldots, x_n]$
- Using the prepend operator: $x_1:x_2:\ldots:x_n:[]$. With the syntax of x:list, it prepends x to the list list.

7.1.2 Pre-defined functions

Many pre-defined functions for lists are defined in the Data.List module.

General Functions These functions work on a list of any type, namely [a].

- head t>. This function returns the head (x_1) of the list. Example: head [1,2,3] returns 1.
- tail tail tail [1,2,3] returns [2,3].
- length t>. This function returns the length of the list. Example: length [1,2,3] returns 3.
- init init init (1,2,3] returns [1,2].
- null t>. This function returns whether the list is empty. Example: null [1,2,3] returns False.
- take $\langle n \rangle$ tist>. This function returns a list of the first n elements of the list. Example: take 2 [1,2,3,4,5] returns [1,2].
- drop <n> the list. This function returns a list excluding the first n elements of the list. Example: drop 2 [1,2,3,4,5] returns [3,4,5].
- ++ t1> ++ t2>. This function "append" returns a concatenation of both lists. Example: [1,2] ++ [3,4] returns [1,2,3,4].

Boolean Functions These functions are of the type fn :: [Bool] -> Bool

- and t>. This functions returns True if every elements in t> is True.
- or <list>. This functions returns True if at least one element in t> is True.

7.1.3 List Comprehension

List comprehension can be used to transform one or more lists according to a predicate. Syntax:

```
[ <gen> | <elem> <- <li>! <guard>, ..., <guard>, ...]
```

Where

- <elem> <- st> is called a generator it binds each value from to <elem> in turn so that they may be used. There may be multiple generators, in which case they will be worked through left-to-right.
- \bullet <guard> is a statement which returns a Bool. If false, the current bound value(s) will not be output.

Examples:

- [2*x | x < [1,2,3]] generates [2,4,6]
- [x^2 | x < [1,2,3], x > 1] generates [4,9]
- [(x,y) | x <- [1,2,3], y <- ['a', 'b']] generates [(1, 'a'), (1, 'b'), (2, 'a'), (2, 'b'), (3, 'a'), (3, 'b')]

7.1.4 Ranges

Generate ranges (arithmetic sequences) in Haskell using the ellipse ..:

Where

- step is optional, and default to 1 e.g. [1..5] = [1,2,3,4,5], [1,3..5] = [1,3,5]
- <end> may be omitted to generate an infinite list e.g. [1 ...] = [1,2,3,...].

7.2 Tuples

An immutable collection of elements of different types.

A tuple has the signature

```
(x,y,\ldots) :: (type_x, type_y, \ldots)
```

8 Kinds

The types of types and type constructors are called kinds.

A kind signature is denoted by ::.. The number of kinds correspond to the number of type parameters a type constructor takes.

 $\bullet\,$ Types which take no type parameters are of kind \star ("type").

```
- Bool :: *
- String :: *
- Maybe :: * -> *
```

 \bullet When we apply a type parameter, one of the parameters is consumed in the kind

```
- Maybe Int :: *
```

9 Modules

In Haskell, each file is a module. Hence, each file (other than the entry file) must begin with a module declaration:

```
module filename [(n1, n2, ...)] where
```

By default, every symbol is exported. If (n1, n2, ...) is included, only symbols n1, n2 etc. are exported.

9.1 Importing

To import a module, use an import statement:

```
import module [(n1, n2, ...)]
```

By default, every symbol exported by module is imported. If (n1, n2, ...) is included, only symbols n1, n2 etc. are imported.

To import Animals.hs one would write import Animals. To import Farm/Tractor.hs one would write import Farm.Tractor.

Once imported, symbols may be used freely. For example, if the function double is imported, to reference it we would write double. However, if two different definitions for double are imported, we must use its full name e.g. Module.double.

9.1.1 Qualified Imports

Syntax:

```
import qualified module [(...)]
```

This forces the module name to precede any symbols imported. In the example above, Module.double must be used.

9.1.2 Aliased Imports

Syntax:

```
import module [(...)] as alias
```

Using the above example, now, instead of writing Module.double one would now write Alias.double.

9.1.3 Hiding Imports

The hiding keyword can be used to omit imports. E.g. import Prelude hiding (map) would import every function from Prelude but omit map.

9.2 Importing Datatypes

Let's say data DataType = A | B | C is defined inside module Module.

- To import every constructor, we'd write import Module (DataType(..))
- To import only constructor A, we'd write import Module (DataType(A))
- To import constructors A and B, we'd write import Module (DataType(A,B))

10 Type Classes

This section covers more complex type classes. For basics, see Types -> Type Classes.

10.1 Semigroups

A type is a Semigroup if there exists some function which, when two values from the group are combined, that value is also in the Semigroup.

```
1 class Semigroup a where
2 (<>) :: a -> a -> a
3 
4 infixr 6 <>
```

This diamond operator must be associative:

```
1 x <> (y <> z) == (x <> y) <> z
```

10.2 Monoid

A Monoid is an extension of a Semigroup, adding an identity element.

```
class Semigroup a => Monoid a where
mempty :: a

-- Optional functions
mappend :: a -> a -> a
mappend = (<>)

mconcat :: [a] -> a
mconcat = foldr mappend mempty
```

mempty must be an identity element for the Semigroup. Therefore, it must obey:

```
1 x <> mempty == x 2 mempty <> x == x
```

10.2.1 Multiple Monoids

A type may have multiple Monoid implementations (i.e. multiple viable operators exist which satisfy Monoidal conditions).

For example, take numerical types:

```
1 newtype Sum n = Sum { getSum :: n }
 2
  instance Num a => Semigroup (Sum a) where
 3
     (<>) = (+)
 4
   instance Num a => Monoid (Sum a) where
 5
    mempty = 0
 6
8
  newtype Product n = Product { getProduct :: n }
 9
   instance Num a => Semigroup (Product a) where
10
    (<>) = (*)
  instance Num a => Monoid (Product a) where
11
    mempty = 1
```

10.2.2 Foldable

A Foldable datatype is one which may be reduced to a single value i.e. folded in on itself.

```
class Foldable t where
foldr :: (a -> b -> b) -> b -> t a -> b
```

10.3 Functors

A Functor is a type class which may have an operation mapped over it.

```
class Functor f where
fmap :: (a -> b) -> f a -> f b -- Infix symbol is <$>

The following functions are optional
(<$) :: a -> f b -> f a
(<$) = fmap . const</pre>
```

A Functor instance must obery the following laws:

- The mapping must preserver the structure of the arguments.
- Identity:

```
1 fmap id == id
```

• Distributive over Composition:

```
1 fmap (f . g) == fmap f . fmap g
```

10.3.1 Fmap

fmap allows a function to be mapped over a structure without the internal structure of the Functor changing.

Example:

```
1 data Tree a = Leaf a | Node (Tree a) a (Tree a)
2
3 instance Functor Tree where
4 fmap f (Leaf a) = Leaf (f a)
5 fmap f (Node a b c) = Node (fmap f a) (f b) (fmap f c)
```

10.4 Applicatives

Applicatives are Functors with more and better functionality, with <*> essentially injecting a value into a wrapped function, and pure allowing easy construction of an applicative.

```
class Functor f => Applicative f where
pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b

-- Optional functions
(*>) :: f a -> f b -> f b

a *> b = b
(<*) :: f a -> f b -> f a
a <* b = a</pre>
```

An Applicative must obey the following laws:

• Identity:

```
1 pure id <*> v == v
```

• Homomorphism:

```
pure f <*> pure x == pure (f x)
```

• Interchange:

```
1 u * pure y == pure (\$ y) <*> u
```

• Composition:

```
1 pure (.) <*> u <*> v <*> w == u <*> (v <*> w)
```

10.5 Monads

A Monad allows the transformation of a value into a Monad via a function.

Any implementation must abide by these laws:

• Left identity:

```
1 return a >= h == h a
```

• Right identity:

```
1 m >= return == m
```

• Associativity:

```
1 (m >>= g) >>= h == m >>= (\x -> g x >>= h)
```

10.5.1 Bind

```
(>>=) :: Monad m => m a -> (a -> m b) -> m b
```

This function takes a monad and a function which takes a raw value and returns a new monad, and returns another new monad.

When implemented, then, we may vary the action taken depending on the value of the provided monad, such as returning a default value – this is what (>>=) does with Maybe, as shown below:

Example:

```
add :: Num a => Maybe a -> Maybe a

add mx my = mx >>= (\x -> my >>= (\y -> Just (x + y)))

-- Then addition works as expected

add (Just 1) (Just 2) -- => Just 3

-- And if either one of the arguments is Nothing, it returns Nothing

add Nothing (Just ?) -- => Nothing
```

10.5.2 Then

```
(>>) :: Monad m => m a -> m b -> m a
```

This function discards the second monad given to it. m >> n is equivalent to $m >> = \setminus_- -> n$.

[&]quot;Then" can be though of wanting to carry out an action but not caring what the result is.

10.5.3 Return

```
return :: Monad m => a -> m a
```

Return wraps a monad around a raw value.

Using the example from the Bind section, we could substitute the explicit Just with the more general return. Now, this would theoretically work with any appropriately-defined monad.

```
1 add mx my = mx >>= (\x -> my >>= (\y -> return (x + y)))
```

10.5.4 Fail

```
fail :: Monad m => String -> m a
```

Fail is intended to be called when something goes wrong. The default implementation is to call error (i.e. error out of the program), but it may be implemented so that certain errors may be handled and return an appropriate monad as a response.

10.5.5 "do" Syntax

Chaining together applications of (>>=), (>>) and lambda functions can get tedious; that's where the syntactic sugar "do" expression comes in.

The "statements" inside of do are executed in order, and if one "statement" fails this will be propagated through.

• Bind

```
1  m >>= \x -> ...
2  -- Becomes
3  do
4  x <- m
5  ...
```

• Then

```
1 m >> ...
2 -- Becomes
3 do
4 m
5 ...
```

Example:

```
1  -- Re-writing the above definition of 'add'
2  add mx my = do
3  x <- mx
4  y <- my
5  return $ x + y</pre>
```

10.5.6 Kleisli-Composition

This operator, denoted >=>, acts as a Monad composition operator. It is defined in Control.Monad as so

```
1 infixr 1 >=>
2 (>=>) :: Monad m => (a -> m b) -> (b -> m c) -> a -> m c
3 f >=> g = \x -> f x >>= g
```

11 I/O

I/O produces an issue with Haskell as I/O functions aren't pure.

11.1 The IO Type

All I/O functions in Haskell have the following type: IO <value>.

This special type holds a given I/O action. When the IO value is used, the stored action will be carried out, and IO <value> is returned.

For example, in GHCI

```
> hi = putStrLn "Hello, World!"
> hw
Hello, World!
```

Notice how nothing was outputted until the IO value was used. Note that hw may be used mutliple times.

11.2 Input

- getLine :: IO String retrieves a line of input from STDIN;
- readLn :: Read a => IO a retrieves a line of input from STDIN, reading it as specified by a;

11.3 Output

```
• putStr :: String -> IO () - puts the given string to STDOUT;
```

- putStrLn :: String -> IO () puts the given string to STDOUT on a new line;
- print :: Show a => a -> IO () essentially the same as putStrLn . show;

11.4 Extracting **<value>**

IO is a *monad*, and should be extracted as such.

```
1 greet :: IO ()
2 greet = do
3  putStrLn "What is your name?"
4  name <- getLine
5  putStrLn $ "Hello, " ++ name ++ "!"</pre>
```

You can only extract values from IO inside of another IO action.

For a more complex example, see code/IO.hs.

11.5 Environment

The following functions are defined in System. Environment.

11.5.1 Command-Line Arguments

```
Command-line arguments are arguments passed to the executable e.g. ./prog.exe arg1 arg2 ... These can be accessed via getArgs :: IO [String]

Note, the program name "prog.exe" is ommitted; this can be access via getProgName :: IO String
```

11.5.2 Environment Variables

The function getEnvironment :: IO [(String, String)] gets a list of all environment variables in name-value pairs.

To get only one variable, the function lookupEnv :: String -> IO (Maybe String) returns the value of an environment variable.

The function withArgs :: [String] -> IO a -> IO a loads sets the environment variables inside an IO action.

11.5.3 Error Handling

Defined in System. Exit

- exitWith :: ExitCode -> IO a exits the program with the provided exit code (ExitCode = ExitSuccess | ExitFailure Int);
- exitSuccess :: IO a exits the program with exit code of success;
- exitFailure :: IO a exits the program with exit code of failure (1);
- die :: String -> IO a prints the given message, then exits the program with exit code of failure (1);

11.6 Files

The symbols stdout :: Handle and stdin :: Handle are handles to the process' input/output streams. I/O functions defined above use the following functions with these handles provided.

- readFile :: FilePath -> IO String reads contents of the file
- writeFile :: FilePath -> String -> IO () writes to the file (overwrites contents if exists)
- appendFile :: FilePath -> String -> IO () appends to the file
- renameFile :: FilePath -> FilePath -> IO () renamed the given file to the second argument
- deleteFile :: String -> IO () deletes the given file

Alternatively, you can use file handles.

- openFile :: FilePath -> IOMode -> IO Handle Open a file in the given mode.

 data IOMode = ReadMode | WriteMode | AppendMode | ReadWriteMode
- hGetContents :: Handle -> IO String Get contents of the file
- hPutStr :: Handle -> String -> IO () writes the given string to the file
- hPrint :: Show a => Handle -> a -> IO () converts a to a string and write to the file
- hClose :: Handle -> IO () Close the given handle
- withFile :: FilePath -> IOMode -> (Handle -> IO a) -> IO a opens a file, processes it according to the function, then closes it

12 Type Families

Type families are functions at defined at the type level. **Example**:

```
data Nat = Z | S Nat
 2
 3
   -- value-level functions
 4
  add :: Nat -> Nat -> Nat
 5 \mid add \mid Z \mid b = b
 6
  add (S a) b = S (add a b)
8
   -- Type-level type family
9
  type family Add (a :: Nat) (b :: Nat) :: Nat where
10
    Add ' Z b = b
     Add ('S a) b = 'S (Add a b)
```

In the first line of the family definition, we list the types of the arguments and the return type. We populate the block with function definitions. Generally, every equation defined up-front: these are called **closed** type families. We can also have **open** type families which do not define every equation.

```
data Bool = True | False

-- Type-level equivalent to match the value-level function
type family Not (b :: Bool) :: Bool where

Not 'True = 'False
Not 'False = 'True

not :: Bool b -> Bool (Not b)
not True = False
not False = True
```

The input type determines what the output type will be. The type family will be evaluated for each pattern match in our function equation.