

# Coefficient of Determination - $R^2$ & Adjusted $R^2$

$R^2$  is defined as the proportion of the variation in the dependent variable that is collectively explained by all of the independent variables / regression model.

$$R^2 = \frac{\text{Explained Variation (RSS)}}{\text{Total Variation (TSS)}}$$

But:  $R^2$  may not be a reliable measure of the explanatory power of the multiple regression model.

$R^2$  almost always increases as variables are added to the model, even if the marginal contribution of the new variables is not significant.

How well does the model fit the data & explain the dependent variable?

Solution: Using Adjusted  $R^2$  → Adding new variables to the model increases or decreases Adjusted  $R^2$  (depending on the new variable's marginal contribution).

Adjusted  $R^2$  is always less than  $R^2$ .

$$Adj R^2 = 1 - \left[ \left( \frac{n-1}{n-k-1} \right) * (1 - R^2) \right]$$

n = number of observations

k = number of independent variables