```
0 /**
 1 * This script does some simple Markov Chain Monte Carlo simulations on a Phi^4
 2 * model. The metropolis Markov Chain algorithm is used.
 3 */
 4 #include <stdlib.h>
                            // calloc()
                            // sqrt()
 5 #include <math.h>
 6 #include "dSFMT/dSFMT.h" // random numbers
 7 #include "phi quad.h" // my header
9 // pre-compute neigbors instead of "on the fly"
10 #define GUGU STORE NEIGHBORS
11
12 // length of a stack array; won't work on heap arrays!
13 #define LENGTH(stack array) (sizeof(stack array) / sizeof(stack array[0]))
15 typedef unsigned long int ulong;
16 typedef unsigned long int ullong;
17 typedef unsigned int uint;
18 typedef unsigned short int ushort;
20 static const ulong kSeed = 123456;
                                            // it's seed value
21 static const uint kDim[3] = {16, 16, 16}; // lattice dimensions
22 // How far to we jump in the array when "searching" for neigbours?
23 // This may be calculated at runtime, however, this way it's a compile time
24 // constant.
25 static const ulong steps[3] = {16, 256, 4096};
26 static const ullong kSweeps = (ullong)1e6;
27 static const ulong kThermalisationSweeps = 1000000;
28 // scale the normal distribution used for Metropolis proposals. The value is
29 // chosen (by hand) so that acceptance rate is about 0.5
30 static const double kProposalScale = 1.5;
31 static const double kLambda = 1.1;
32 static const double k2Kappa = .1;
33
34 static dsfmt t rng;
                                         // random number generator
35 static double *lat;
                                         // main system
36 static double *A 1, *A 2;
                                        // observables
37 static ulong accepted proposals = 0; // # of acc. metropolis proposals
38 static ulong volume;
                                         // number of lattice sites
39 #ifdef GUGU STORE NEIGHBORS
40 static ulong *neigh idx;
41 static const uint neigh count = 2 * LENGTH(kDim);
42 #endif
43
44 int main() {
45
    SeedRNG(kSeed);
46
47
    // calculate lattice site count
48
    volume = 1;
49
     for (uint i = 0; i < LENGTH(kDim); i++) {
      volume *= kDim[i];
50
51
52
53
     // "calloc" automatically initializes to zero
    lat = (double *)calloc(volume, sizeof(double));
55
     A 1 = (double *)calloc(kSweeps, sizeof(double));
56
     A 2 = (double *)calloc(kSweeps, sizeof(double));
57
58 // pre-compute neighbors
59 #ifdef GUGU STORE NEIGHBORS
     neigh_idx = (ulong *)malloc(neigh_count * volume * sizeof(ulong));
60
61
     for (ulong site = 0; site < volume; site++) {</pre>
62
       // neigbors in positive direction
       neigh idx[neigh count * site] =
63
64
           site - site % steps[0] + (site + 1) % steps[0];
65
       neigh idx[neigh count * site + 1] =
```

```
66
            site - site % steps[1] + (site + steps[0]) % steps[1];
 67
        neigh_idx[neigh_count * site + 2] =
68
            site - site % steps[2] + (site + steps[1]) % steps[2];
69
70
        // neighbors in negative direction
71
        neigh_idx[neigh_count * site + 3] =
72
            site - site % steps[0] + (site + steps[0] - 1) % steps[0];
73
        neigh idx[neigh count * site + 4] =
74
            site - site % steps[1] + (site + steps[1] - steps[0]) % steps[1];
75
        neigh_idx[neigh_count * site + 5] =
76
            site - site % steps[2] + (site + steps[2] - steps[1]) % steps[2];
77
      }
78 #endif
79
      // thermalisation
80
      for (uint i = 0; i < kThermalisationSweeps; <math>i++) {
81
82
        SweepSequential();
83
 84
85
      // main simulation
86
      for (uint i = 0; i < kSweeps; i++) {
87
        SweepSequential();
88
        Observe(i);
89
      }
90
91
      // analysis
      printf("acceptance rate after %.le sweeps: %f\n", (double)kSweeps,
92
93
             (double)accepted proposals / volume / kSweeps);
94
95
      const uint binnings[] = \{10, 100, 1000, 5000, 10000\};
96
      for (uint i = 0; i < LENGTH(binnings); i++) {</pre>
97
        printf("A 1:");
98
        BinningAnalysis(A 1, kSweeps, binnings[i]);
99
        printf("A 2:");
100
        BinningAnalysis(A 2, kSweeps, binnings[i]);
101
      }
102
103
     // cleanup
104
      free(lat);
105
      free(A 1);
      free(A 2);
106
107 #ifdef GUGU STORE NEIGHBORS
108
      free(neigh idx);
109 #endif
110
      return 0;
111 }
112
113 inline void SweepSequential() {
      for (ulong i = 0; i < volume; i++) {
114
115
        Propagate(i);
116
117 }
118
119 inline void Propagate(ulong site) {
120
      double u = lat[site];
121
      // make a proposal on how to alter lattice site state
122
123
      double delta = GaussRandomNumber() * kProposalScale; // change in phi
124
      double n = u + delta;
                                                              // new value
125
126
      // decide if we want to accept it
127
128
      // gauss term
129
      double gauss diff = delta * (k2Kappa * SumNeighbors(site) - n - u);
130
131
      // quartic term (not dependend on neigbors)
```

```
132
      double tmp = u * u - 1;
133
      double quartic diff = tmp * tmp;
134
      tmp = n * n - 1;
      quartic diff -= tmp * tmp;
135
136
      quartic diff *= kLambda;
137
138
      double energy diff = gauss diff + quartic diff;
139
140
      // update site with probablility min(1, exp(energy diff));
141
      if (RandDouble() < exp(energy diff)) {</pre>
142
        lat[site] = n;
143
        accepted proposals++;
144
      }
145 }
146
147 void Observe(ullong observation index) {
148
      double a1 = 0, a2 = 0;
149
      for (ulong i = 0; i < volume; i++) {
150
        a1 += SumPositiveNeighbors(i) * lat[i];
151
        a2 += lat[i];
152
      }
153
      A 1[observation index] = a1 / volume;
      A 2[observation index] = a2 * a2 / volume;
154
155 }
156
157 inline double SumNeighbors(ulong site) {
158
      double sum = 0;
159 #ifdef GUGU STORE NEIGHBORS
160
      for (uint i = 0; i < neigh count; i++) {
161
        sum += lat[neigh idx[site * neigh count + i]];
      }
162
163 #else
      sum += lat[site - site % steps[0] + (site + steps[0] - 1) % steps[0]];
164
165
      sum += lat[site - site % steps[0] + (site + 1) % steps[0]];
166
      sum += lat[site - site % steps[1] + (site + steps[1] - steps[0]) % steps[1]];
      sum += lat[site - site % steps[1]] + (site + steps[0]) % steps[1]];
167
168
      sum += lat[site - site % steps[2] + (site + steps[2] - steps[1]) % steps[2]];
169
      sum += lat[site - site % steps[2] + (site + steps[1]) % steps[2]];
170 #endif
171
      return sum;
172 }
173
174 inline double SumPositiveNeighbors(ulong site) {
175
      double sum = 0;
176 #ifdef GUGU STORE NEIGHBORS
177
      for (uint i = 0; i < neigh count / 2; i++) {
178
        sum += lat[neigh idx[site * neigh count + i]];
      }
179
180 #else
      sum += lat[site - site % steps[0] + (site + 1) % steps[0]];
181
182
      sum += lat[site - site % steps[1] + (site + steps[0]) % steps[1]];
183
      sum += lat[site - site % steps[2] + (site + steps[1]) % steps[2]];
184 #endif
185
      return sum;
186 }
187
188 double BinnedStatisticalError(const double *array, const ulong length,
189
                                   const ulong bin size) {
190 #pragma GCC diagnostic push
191 #pragma GCC diagnostic ignored "-Wbad-function-cast"
192
      ulong n_bins = (ulong)ceil((double)length / bin_size);
193 #pragma GCC diagnostic pop
194
      double *local averages = (double *)calloc(n bins, sizeof(double));
195
      for (ulong i = 0; i < length; i++) {
196
        local_averages[i / bin_size] += array[i];
197
      }
```

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198
      for (ulong i = 0; i < n_bins; i++) {
199
        local_averages[i] /= bin_size;
200
      }
201
      double err = Variance(local averages, n bins) / n bins;
202
      free(local averages);
203
      return sqrt(err);
204 }
205
206 void BinningAnalysis(const double *data, const ulong length,
207
                         const ulong bin size) {
208
      printf("analysing at bin size %lu...\n", bin_size);
209
      double binned_error = BinnedStatisticalError(data, length, bin size);
210
      double raw error = sqrt(Variance(data, length) / length);
      double tau int = .5 * length * pow(binned error / raw error, 2);
211
      printf("value, error and tau int est. : %7f %7f %0f\n", Average(data, length),
212
213
             binned_error, tau_int);
214 }
215
216 // As we just plain sum the elements (no Kahan summation or anything), care
217 // needs to be taken on large systems.
218 inline double Average(const double *array, const ulong length) {
      double sum = 0.;
      for (ulong i = 0; i < length; i++) {
220
221
        sum += array[i];
222
223
      return sum / length;
224 }
225
226 double Variance(const double *array, const ulong length) {
227
      double average = Average(array, length);
228
      double sum of squares = 0.;
229
      for (ulong i = 0; i < length; i++) {
230
        sum of squares += array[i] * array[i];
231
232
      sum of squares /= length;
233
      return sum of squares - average * average;
234 }
235
236 void SeedRNG(uint seed) { dsfmt init gen rand(&rng, seed); }
238 // uses dSFMT from included library
239 inline double RandDouble() { return dsfmt genrand close open(&rng); }
241 // we use the Marsaglia polar method, taken from
242 // https://en.wikipedia.org/wiki/Marsaglia polar method
243 double GaussRandomNumber() {
244
      static char hasSpare = 0;
245
      static double spare;
246
247
      if (hasSpare == 1) {
248
        hasSpare = 0;
249
        return spare;
250
      }
251
252
      hasSpare = 1;
253
     static double u, v, s;
254
      do {
255
        u = dsfmt genrand close1 open2(&rng) * 2 - 3;
256
        v = dsfmt_genrand_close1_open2(&rng) * 2 - 3;
        s = u * u + v * v;
257
258 #pragma GCC diagnostic push
259 #pragma GCC diagnostic ignored "-Wfloat-equal"
260
      } while (s >= 1 || s == 0);
261 #pragma GCC diagnostic pop
262
     s = sqrt(-2.0 * log(s) / s);
263
```

```
264
      spare = v * s;
265
      return u * s;
266 }
267
268 // Does no checks at all.
269 void PersistArray(double *array, long long unsigned int element_count,
                             const char *file name) {
       printf("persisting %i doubles\n", (int)element_count);
FILE *file = fopen(file_name, "wb");
fwrite(array, sizeof(double), sizeof(double) * element_count, file);
271
272
273
274
        fclose(file);
275 }
276
```