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MA30044/MA40044/MA50181: Mathematical Methods I Information Sheet

The course will be taught by **Dr. Philippe Trinh**. A number of the problem classes will be directed by **Dr. Samuel Crew**.

Schedule of Classes

There will be three classes per week.

Lecture: Tuesday 16:15h in 3E 2.1 Lecture: Thursday 11:15h in CB 2.6 Problems class: Friday 9:15h in CB 2.6

The problems class will be replaced by a lecture in week 1. For MA50181 students there will be an additional lectures on *Asymptotic Methods*. The timetabling will be determined in Week 1.

All lectures will be recorded.

Content of lectures

This course will introduce you to a number of useful advanced mathematical methods that can be applied to the solution of linear systems and partial differential equations. Although we will prove key theorems, the focus will be on introducing you to a number of practical techniques and their applications, rather than mathematical rigour. Topics covered are:

- **Sturm Liouville Theory** Definition of and reduction to Sturm-Liouville systems, Self-adjoint operators, eigenfunction, othogonality and orthonormal expansions, approximation of functions, Legendre polynomials, inhomogeneous equations and the Fredholm alternative, solution of PDEs, applications in electrostatics
- **The Fourier Transform** Definition of the Fourier transform, elementary properties (shift theorems, derivative theorems, distributions and the Dirac δ -function, the convolution theorem, solution of second order equations, Plancherel's theorem, solving PDEs
- **Quasilinear first order PDEs** Classification of PDEs, data curves and contour lines, the method of characteristics, envelopes and domains of influence, Burgers' equation
- **Second order hyperbolic PDEs** Classification of second order PDEs (elliptic, parabolic, hyperbolic), characteristics and changes of variables, d'Alemberts' solution of the wave equation

Assessment scheme

The course will be assessed by an exam at the end of the semester. The format of the exam will be the same as in the last years; you can find past exams on the library webpage. All material covered in the lectures and applied on the problem sheets is examinable, unless explicitly marked otherwise.

MA30044 students: The exams counts as 100% of the final mark.

MA40044 students: There will be an **additional** piece of **coursework**, set by physics¹, in week 8 and due in the revision week. The final mark consists of the exam (80%) and the coursework (20%).

MA50181 students: There will be an **additional** 40-minute written **class test** on asymptotic methods in the revision week. The final mark consists of the exam (75%) and the class test (25%). The exact date, time and location for this test is:

Class test (MA50181 only): Thursday 13th Jan 2022 (to be confirmed) TBD in TBD

Problem sheets

If you would like feedback on your workings for problem sets, please submit them by the date indicated on the top of the problem set. In order to help us provide you with feedback that is tailored for *you*, all submitted problem sets must be accompanied by a cover page found on the Moodle homepage. A hand-written version of the above template is also perfectly fine!

Any problem sets that are not accompanied by a cover page will be returned and can be re-submitted later with the correct format. Submissions should be deposited in the 4W pidgeonholes.

Resources

The Moodle page for the course is

https://moodle.bath.ac.uk/course/view.php?id=29834

referred to throughout the course as the homepage. It will contain lecture notes, problem sheets and solutions. You should automatically be enrolled. If not, please contact me.

References

The lecture notes aim to be self-contained and should provide you with all material for the course. There is a plethora of books on topic in engineering mathematics and mathematical methods for physicists available in the library.

I sincerely hope you will enjoy the course. If you have any problems please do not hesitate to see me at the end of a lecture or email me.

¹The coursework for MA40044 students will be set and overseen by Dr. David Tsang (dcwt21@bath.ac.uk), please direct any queries regarding the coursework directly to him.