

1.

a. When increasing the size of an array, you are only using one loop to increase the size.

As one loop will always be  $O(n)$ , and doubling a  $O(n)$ , no matter how many times you do it would only add the current number of iterations to the total.

Thus, the runtime is  $n + 1 + 2 + 4 + 8 + \dots + 2^k = n + 2^{k+1} - 1 = 2n - 1$ , which is  $O(n)$ .

b. If  $n$  is a power of two, the recursion will continue to loop until  $n = 2$ , at which point the the program will output  $B[0]$ .

example: if  $n = 16$ , then iterations would go  $8 + 4 + 2 + 1 = 15$

$$n - 1 = n/2 + n/2/2 + n/2/2/2 + \dots + n/2^{(n^{1/2})}$$

As  $O(n-1) = O(n)$ , the run time is  $O(n)$ .