

→ Assignment 7:

\* Let consider a simple dataset have one Input ( $x_i$ ) and one Output ( $y_i$ ) and number of samples a develop a simple linear Regression Model by using BGD

Simple ( $i$ )	$x_i$	$y_i$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

\* Do Manual Calculations for 2 iterations with 1st 2 samples.

step 1 :  $[x, y], m = 1, c = -1, \eta = 0.1, \text{epochs} = 2, ns = 2$

step 2 : iter = 1

step 3 :  $\frac{\partial E}{\partial m} = -\frac{1}{ns} \sum_{i=1}^{ns} (y_i - mx_i - c)x_i$

$$= -\frac{1}{2} [(3.4 - (1)(0.2) + 1)0.2 + (3.8 - (1)(0.4) + 1)0.4]$$

$$= -1.34$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} [(3.4 - 0.2 + 1) + (3.8 - 0.4 + 1)]$$

$$= -4.3$$

step 4 :  $\Delta m = -\eta \frac{\partial E}{\partial m}$

$$= -0.1 \times -1.34 = 0.134$$

$$\Delta c = -\eta \frac{\partial E}{\partial c}$$

$$= -0.1 \times -4.3 = 0.43$$

$$\text{step 4: } \Delta m = -\eta \frac{\partial E}{\partial m}$$

$$= 0.1 \times -1.34 = -0.134$$

$$\Delta c = -\eta \frac{\partial E}{\partial c}$$

$$= -0.1 \times -4.3 = 0.43$$

$$\text{step 5: } m += \Delta m$$

$$= 1 + 0.134 = 1.134$$

$$c += \Delta c$$

$$= -0.1 \times 4.3 = -0.43$$

$$\text{step 6: } \text{iter} += 1$$

$$1 + 1 = 2$$

$$\text{step 7: } \% \text{ if (iter > epochs) : goto step 8}$$

$$2 > 2$$

$$\text{else goto step 3}$$

$$\text{step 3: } \% \frac{\partial E}{\partial m} = -\frac{1}{2} [c \cdot 4 - (1.134)(0.2) + (0.54)(0.2) +$$

$$(3.8 - (1.134)(0.4) + 0.57)(0.4)]$$

$$= -1.157$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} [(c \cdot 4 - (1.134)(0.2) + 0.57) +$$

$$(3.8 - (1.134)(0.4) + 0.57)]$$

$$= -3.829$$

$$\text{step 9: } \Delta m = -0.1 \times -1.157 = 0.1157$$

$$\Delta c = -0.1 \times -3.829 = 0.3829$$

$$\text{step 5: } m += \Delta m \Rightarrow 1.134 + 0.1157 = 1.2497$$

$$c += \Delta c \Rightarrow -0.57 + 0.3829 = -0.1871$$

$$\text{step 6: } \text{iter} \neq 1 \Rightarrow 2 + 1 = 3$$

$$\text{step 7: } \% \text{ if (iter > epochs) : goto step 8}$$

$$3 > 2$$

$$\text{else: goto step 3}$$

$$\text{step 8: } m = 1.2497 \quad c = -0.1871$$