

# Data Structures & Algorithms

| Data Structure | Time Complexity |        |           |          | Space Complexity |        |           |          |
|----------------|-----------------|--------|-----------|----------|------------------|--------|-----------|----------|
|                | Average         |        | Worst     |          | Worst            |        |           |          |
|                | Access          | Search | Insertion | Deletion | Access           | Search | Insertion | Deletion |
|                |                 |        |           |          |                  |        |           |          |

# Time/Space Complexity

## What is the big-O for the following series:

$$1 + 2 + 3 + \dots + n = ?$$

$$1 + 2 + 4 + 8 + \dots + n = ?$$

$$2^0 + 2^1 + 2^2 + \dots + 2^n = ?$$

$$1+2+\dots+n = (n(n+1))/2 = O(n^2)$$

$$1 + 2 + 4 + 8 + \dots + n = O(2n) = O(n)$$

|      | Power     | Binary | Decimal       |
|------|-----------|--------|---------------|
|      | $2^0$     | 00001  | 1             |
|      | $2^1$     | 00010  | 2             |
|      | $2^2$     | 00100  | 4             |
|      | $2^3$     | 01000  | 8             |
|      | $2^4$     | 10000  | 16            |
| sum: | $2^5 - 1$ | 11111  | $32 - 1 = 31$ |

Therefore, the sum of  $2^0 + 2^1 + 2^2 + \dots + 2^n$  would, in base 2, be a sequence of  $(n + 1)$  1s. This is  $2^{n+1} - 1$ .

What is the difference between combinations and permutations, and how do you compute them? What's the intuition behind the equation?

**Permutations:** Order matters

- Represents multiplying  $n * (n-1) * \dots * (n-k+1)$
- If  $n=k$ , becomes  $n!$

$$P_k^n = \frac{n!}{(n-k)!}$$

**Combinations:** Order invariant

- Same as permutation, but divide out the duplicates with same elements but different ordering
- If  $n=k$ , becomes 1

$$C_k^n = \frac{n!}{k!(n-k)!}$$

## What is the time complexity of $nCk$ ?

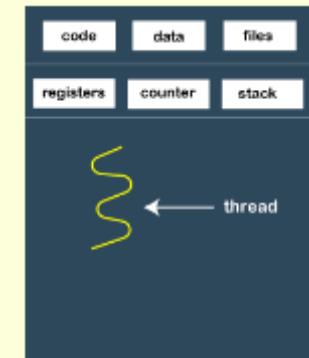
- In general,  $O(n^{\min\{k,n-k\}})$
- In most cases,  $k$  is very small, so  $O(n^k)$

# Misc

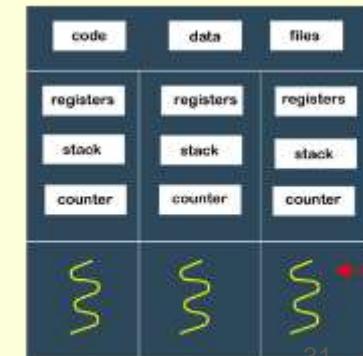
# What are processes and threads?

- Each process must start with least one thread, but can also later create multiple.
- Processes/threads are implemented on the OS level, and uses the underlying CPU's cores/processors
  - For example, a Intel Core i5-1335U has 10 cores and 12 hardware threads. This means that 10 processes can be run at once (true parallel), and 12 threads scheduled at once. You can have more software processes/threads – they will be scheduled using context switching.
- In CPython, the Global Interpreter Lock (GIL) allows only one thread to hold control of the Python interpreter.
  - So, only one thread can be executing at any point in time. This was done for simplicity/compatibility
  - However, other python implementations don't have a GIL

|                          | Processes   | Threads  |
|--------------------------|---|--|
| <b>Memory Space</b>      | Each has a separate memory space  | Threads of a process run in a shared memory space  |
| <b>Communication</b>     | Harder to share objects between processes; more isolated from each other. Need inter-process communication (IPC)      | Easier to share objects in the same memory, but need to be careful to avoid race conditions  |
| <b>Python Package</b>    | threading   | multiprocessing  |
| <b>Overhead</b>          | Larger memory footprint   | Lightweight, low memory footprint  |
| <b>True parallelism?</b> | In python, takes advantages of multiple CPUs/cores  | In python, threads cannot be run in parallel using multiple CPUs/cores, due to the GIL.  |
| <b>Use Case</b>          | <b>Use case in python:</b> For when you want to really do more than one thing at a given time on the CPU (CPU-bound). | <b>Use case in python:</b> enables applications to be responsive, when execution is I/O bound (eg from internet, database retrieval, etc). Things aren't being done in parallel on the CPU, but concurrently due to context switching. |



Single-threaded process



Multi-threaded process

## **Question Goes Here**

- Answer goes here