

Exploring millennial responses of reefs to climatic forcing, insights from coupled wave and carbonate growth forward stratigraphic model

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Key Points.

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Abstract. (Type abstract here)

1. Introduction

(Article text here.)

2. Carbonate platform evolution models

3. pyReef model

3.1. Model overview

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3.2. Large-scale forcings

temperature, salinity sea-level tectonics ph

3.3. Wave transformation

SWAN, short for *Simulating WAVes Nearshore*, is a third-generation, finite-difference, wave model used to predict wave propagation in coastal areas and estuaries. It is governed by the wave action balance equation [Bretherton and Garrett, 1968; Hasselmann et al., 1973; Holthuijsen et al., 1993; Booij et al., 1999]:

$$\frac{\partial N}{\partial t} + \nabla_{\vec{x}} \cdot [(\vec{c}_g + \vec{U}) N] + \frac{\partial c_\theta N}{\partial \theta} + \frac{\partial c_\sigma N}{\partial \sigma} = \frac{S_{tot}}{\sigma} \quad (1)$$

where $N(\vec{x}, t, \sigma, \theta)$ is the wave action function of geographical space \vec{x} , time t , relative frequency σ and wave direction θ . $\nabla_{\vec{x}}$ is the gradient operator in space, \vec{c}_g and \vec{U} are the wave group velocity and ambient current vector respectively and c_θ , c_σ is the propagation velocity in θ and σ domain. Finally S_{tot} is the source term which can include wind, whitecapping, surf breaking and bottom friction [Booij et al., 1999]. In our model, shoaling and refraction are accounted for from a series of deep-water wave conditions through time in the absence of wind forcing. Hence to compute wave field generation, the model requires bathymetric conditions and defi-

nitions of offshore significant wave height, characteristic period of the energy spectrum and wave direction and associated spreading angle.

To evaluate reef responses over several hundreds of years, the approach taken here does not examine temporal evolving wave fields, such as those produced during storm events and relies on SWAN stationary mode. In pyReef, the wave transformation model is generally performed for time intervals varying from 0.5 to 10 years. Our aim is to simulate realistic wave fields by imposing a sequence of wave forcing conditions (*e.g.* series of fair-weather and/or storm events). At any given time interval, we define a percentage of activity for each deep-water wave conditions and the bathymetry is used to compute associated wave parameters. Possibility is given to derived these parameters for both low and high tides.

Combined with the climatic forcing described above, two additional wave factors could be adjusted in the model: the breaking parameter and the bottom friction.

In regions where wave height is close to water depth, wave breaking is an important source of energy dissipation on reefs [Symonds et al., 1995; Becker et al., 2014]. This effect is typically approximated with a constant breaking parameter γ_s [Symonds et al., 1995; Vetter et al., 2010] which values have been calibrated for different reef systems [Apotsos et al., 2007; Vetter et al., 2010; Monismith et al., 2013; Franklin et al., 2013; Rogers et al., 2015].

The high rugosity of reefs plays a significant role on wave dynamics by increasing the frictional dissipation of wave energy flux [Young, 1989; Lowe et al., 2005; Lowe and Falter, 2015]. This dissipation is usually approximated with a wave roughness friction factor f_w which values have been well constrained for sand grain [Kamphuis, 1975; Grant and Madsen, 1979; Dean and Dalrymple, 1991]. In phase-averaged wave action approach like SWAN, this bottom dissipation is parameterised as a function of wave excursion to bottom roughness scale with a maximum value of 0.3 for f_w [Jonsson, 1966; Madsen et al., 1988]. Several studies [Nelson, 1996; Lowe et al., 2005; Lentz et al., 2015; Rogers et al., 2015; Monismith et al., 2015] indicates that this roughness factor can be much higher for reef systems (*i.e.* up to 5.0 for reef platform in the Red Sea [Lentz et al., 2015]). To better estimate the impact of reef rugosity on frictional dissipation, we have modified the existing formulation for f_w in SWAN and used the proposed parameterisation from Rogers et al. [2015] based on Swart [1974]:

$$f_w = \begin{cases} \exp[a_1 (A_b/k_N)^{a_2} + a_3], & A_b/k_N \geq 0.0369 \\ 50, & A_b/k_N < 0.0369 \end{cases} \quad (2)$$

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where A_b is the wave excursion distance, k_N is the bottom roughness scale and the coefficients $a_1 = 5.213$, $a_2 = -0.194$, and $a_3 = -5.977$ have been set based on *Rogers et al.* [2015] Palmyra study. Alternate coefficient from *Nielsen* [1992] can also be used ($a_1 = 5.5$, $a_2 = -0.2$, and $a_3 = -6.3$). For large values of A_b/k_N , this formulation is similar to the one from *Madsen et al.* [1988] (implemented in SWAN), but extends the parameterisation for lower A_b/k_N . In pyReef, the bottom friction is based on the proposed formulation and requires the definition of the bottom roughness scale (k_N) which values is generally set to 2-3 times the characteristic diameters of the studied region [*Nielsen*, 1992; *Lowe et al.*, 2005; *Rogers et al.*, 2015].

For each forcing conditions, the wave transformation model computes and returns the significant wave height, the mean wave direction and the root-mean-square value of the maxima of the orbital velocity near the bottom. These parameters are subsequently used to evaluate the long-term hydrodynamic forces active over the simulated region.

3.4. Long-term wave-driven circulation

Flow circulation in and around reef platforms depends on the complex interactions between the overlying water motion and the three-dimensional bottom roughness formed by reef organisms. Attempts to numerically simulate flow dynamics around individual coral colonies have been proposed [*Kaandorp et al.*, 2003; *Chang et al.*, 2009; *Chindapol et al.*, 2013] but such models require the flows to be solve down to few millimetres scale and are beyond the scope of our approach. Here we assume that the flow circulation in the reef platform is mainly driven by waves and regional-scale drivers of reefs hydrodynamics such as coastal upwelling or ocean currents are ignored. Numerical studies of wave-driven flow around reef systems commonly use depth-averaged Navier-Stokes equations [*Raupach and Shaw*, 1982; *Symonds et al.*, 1995; *Lowe et al.*, 2005, 2009; *Pomeroy et al.*, 2012; *Taebe et al.*, 2011]. In the context of millennial scale reef platform evolution, these methods however are still computationally prohibitive. In pyReef, the proposed method consists in producing *snapshots* of wave-driven circulation distribution resulting from series of deep-water wave scenarios by computing time-averaged cross-shore and longshore currents.

In nearshore environments, longshore current runs parallel to the shore and is generated by the radiation stresses associated with the breaking process for obliquely incoming waves and by the surplus water which is carried across the breaker zone towards the shoreline [*Longuet-Higgins*, 1970]. This current affect the transport and transfer of mass (loose carbonate sands, nutrients and carbon) in the nearshore reef waters [*Hamner and Wolanski*, 1988; *Monismith*, 2007; *Lowe and Falter*, 2015]. Many empirical formulation of longshore current have been proposed since the initial work from *Longuet-Higgins and Stewart* [1964] [*Komar and Inman*, 1970; *Komar and Miller*, 1975; *Galvin*, 1987; *Reniers and Battjes*, 1997; *Ruessink et al.*, 2001; *Grasmeijer and Ruessink*, 2003]. In pyReef, the approach from *Komar and Miller* [1975] is used to calculate the longshore current velocity (\vec{v}_l) in the middle of the breaking zone:

$$\vec{v}_l = \kappa_l u_b \cos(\theta) \sin(\theta) \vec{k} \quad (3)$$

where u_b is the maximum near-bed orbital velocity obtained from SWAN, θ the angle of incidence of the incoming waves, κ_l a scaling parameter and \vec{k} the unit vector parallel to the breaking depth contour. For wave rays approaching the reef at an oblique angle, the component of wave energy flux parallel to the reef shore will drives this longshore velocity. The calculation of the angle of incidence in pyReef is quite straightforward and requires an estimate of wave breaking depth (defined for each wave scenario) and wave direction (obtained from the wave transformation model).

In addition to longshore current, two types of cross-shore velocities are simulated in pyReef. First we estimate the onshore velocity which is essential in predicting the shoreward transport of broken carbonate particles during fair-weather periods [*Elfrink et al.*, 1999; *Ruessink et al.*, 1998]. In our model, we assume a linear dependency between the near-bed orbital velocity and the intensity of this onshore current \vec{v}_o :

$$\vec{v}_o = \kappa_o u_b \vec{n} \quad (4)$$

with u_b the maximum near-bed orbital velocity, \vec{n} the unit vector parallel to the incoming wave direction and κ_o a correction factor. κ_o can be derived from local shallow reef water conditions and reflects natural wave skewness and asymmetry which are known to play a central part in cross-shore velocity profile [*Grasmeijer and Ruessink*, 2003; *Crawford and Hay*, 2003]. The onshore velocity (\vec{v}_o) is usually associated to the wave crest and is stronger than the one due to the wave trough [*Isobe and Horikawa*, 1982; *Grasmeijer and Ruessink*, 2003].

During strong wave conditions, a second type of wave-induced cross-shore velocity is defined in pyReef and simulates an offshore-directed steady current referred to as undertow. The time-averaged and depth-averaged undertow velocity \vec{v}_u is derived from the mass flux due to the wave motion and surface roller [*Svendsen et al.*, 1987]. Under normal incident periodic waves, *Longuet-Higgins* [1975] showed that the depth- and time-averaged undertow velocity is related to the wave's kinetic energy density and phase speed. Assuming equipartition of kinetic and potential wave energy, the total energy density of the wave is approximately [*Svendsen*, 1984]:

$$E_w = \frac{1}{8} \rho g H^2 \quad (5)$$

with ρ the ocean density and H the root-mean-square wave height returned by SWAN. Following *Cox and Kobayashi* [1998], the undertow velocity is assumed to have the following form in our model:

$$\vec{v}_u = -\kappa_u \frac{\sqrt{gh}}{8} \left(\frac{H}{h} \right)^2 \vec{n} \quad (6)$$

with κ_u an empirical coefficient [*Kobayashi et al.*, 1998], g the gravitational acceleration, h the water depth and \vec{n} the unit vector parallel to the incoming wave direction.

3.5. Calcareous sand transport

Several studies indicate sufficient variations in the hydraulic properties between siliceous and calcareous sand that would lead to different transport mechanisms of the sediments. Despite these observations and to our knowledge, sediment transport models for calcareous sands under wave and current actions have not yet been proposed.

In pyReef, sediment transport induced by wave and current dynamic is derived from Soulsby and Van Rijn formulation [*Soulsby*, 1997]. The method computes the total load transport rate resulting from the addition of bed load and suspended load for each type of loose carbonate sands initially set by the user. The model also assumes that each of sand particles are perfectly sorted. The method suits well with our approach as it can be applied in a quasi-steady form. The transport rate is defined by:

$$q_t = (A_{sb} + A_{ss}) \bar{v} \left[\sqrt{\bar{v}^2 + \frac{0.018}{C_D} u_b - u_{cr}} \right]^{2.4} (1 - 1.6 \nabla z) \quad (7)$$

where \bar{v} is the depth-averaged current velocity obtained from the long-term wave driven circulation model defined in previous section, C_D is the drag coefficient (due to current alone) and ∇z the slope. The bed load transport A_{sb} is given by:

$$A_{sb} = \frac{0.005h(d/h)^{1.2}}{(s-1)gd} \quad (8)$$

with s is the relative density of sediments and d is the median grain diameter. The suspended load transport A_{ss} is obtained from the following formula:

$$A_{ss} = \frac{0.012hd_*^{-0.6}}{(s-1)gd} \quad (9)$$

where d_* refers to the dimensionless particle diameter. The threshold current velocity (\bar{u}_{cr}) of motion follows:

$$\bar{u}_{cr} = \begin{cases} 0.19 d^{0.1} \log_{10}(4h/d), & 0.1 \geq d \geq 0.5 \text{ mm} \\ 8.5 d^{0.6} \log_{10}(4h/d), & 0.5 \geq d \geq 2 \text{ mm} \end{cases} \quad (10)$$

transport formulation multi-sediment stratigraphy Initiation of Motion of Calcareous Sand diffusion

3.6. Carbonate growth and disintegration

The fuzzy model simulates the deposition of reefs and carbonate facies through integration of local and global variables. Local-scale factors include basement relief, sea-level change, climate, latitude, water energy, water depth, background sedimentation rate, and substrate conditions. Regional and global-scale changes include relative sea-level change, climate, and latitude.

4. Models setup

5. Results

impact of storms on carbonate evolution (model with fair weather and model with 1 storm and after 2 storms)
 impact of sea-level change and thermal subsidence
 impact of change in pH and ocean temperature

6. Discussion

7. Conclusions

Acknowledgments. (Text here)

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