

Algorithm 3.1 Algorithm for finding nodes reachable from X given Z via active trails

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Procedure Reachable (
     $\mathcal{G}$ , // Bayesian network graph
     $X$ , // Source variable
     $Z$  // Observations
)
1 // Phase I: Insert all ancestors of  $Z$  into  $A$ 
2  $L \leftarrow Z$  // Nodes to be visited
3  $A \leftarrow \emptyset$  // Ancestors of  $Z$ 
4 while  $L \neq \emptyset$ 
5     Select some  $Y$  from  $L$ 
6      $L \leftarrow L - \{Y\}$ 
7     if  $Y \notin A$  then
8          $L \leftarrow L \cup \text{Pa}_Y$  //  $Y$ 's parents need to be visited
9          $A \leftarrow A \cup \{Y\}$  //  $Y$  is ancestor of evidence
10
11 // Phase II: traverse active trails starting from  $X$ 
12  $L \leftarrow \{(X, \uparrow)\}$  // (Node,direction) to be visited
13  $V \leftarrow \emptyset$  // (Node,direction) marked as visited
14  $R \leftarrow \emptyset$  // Nodes reachable via active trail
15 while  $L \neq \emptyset$ 
16     Select some  $(Y, d)$  from  $L$ 
17      $L \leftarrow L - \{(Y, d)\}$ 
18     if  $(Y, d) \notin V$  then
19         if  $Y \notin Z$  then
20              $R \leftarrow R \cup \{Y\}$  //  $Y$  is reachable
21              $V \leftarrow V \cup \{(Y, d)\}$  // Mark  $(Y, d)$  as visited
22             if  $d = \uparrow$  and  $Y \notin Z$  then // Trail up through  $Y$  active if  $Y$  not in  $Z$ 
23                 for each  $Z \in \text{Pa}_Y$ 
24                      $L \leftarrow L \cup \{(Z, \uparrow)\}$  //  $Y$ 's parents to be visited from bottom
25                 for each  $Z \in \text{Ch}_Y$ 
26                      $L \leftarrow L \cup \{(Z, \downarrow)\}$  //  $Y$ 's children to be visited from top
27             else if  $d = \downarrow$  then // Trails down through  $Y$ 
28                 if  $Y \notin Z$  then
29                     // Downward trails to  $Y$ 's children are active
30                     for each  $Z \in \text{Ch}_Y$ 
31                          $L \leftarrow L \cup \{(Z, \downarrow)\}$  //  $Y$ 's children to be visited from top
32                 if  $Y \in A$  then // v-structure trails are active
33                     for each  $Z \in \text{Pa}_Y$ 
34                          $L \leftarrow L \cup \{(Z, \uparrow)\}$  //  $Y$ 's parents to be visited from bottom
35 return  $R$ 

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