Lab3

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###Assignment 1: Analysis of mortality rates using splines

Pre

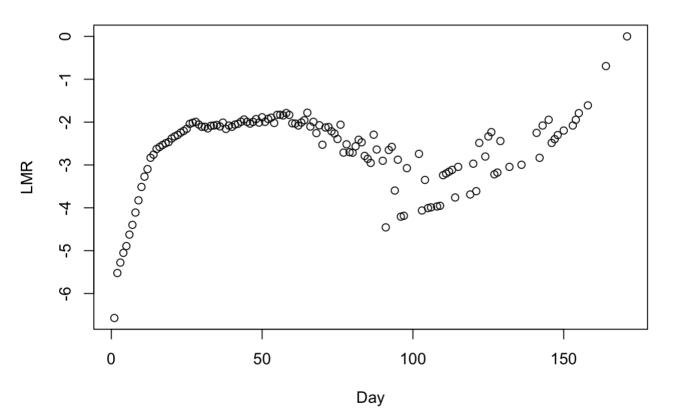
```
mortality_rate = read.csv('mortality_rate.csv', header = TRUE, sep = ';')
summary(mortality_rate$Rate)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.00140 0.04940 0.09455 0.09836 0.12848 1.00000
```

1.a.

```
mortality_rate$lmr = log(mortality_rate$Rate)
plot(mortality_rate$Day, mortality_rate$lmr,
    ylab = 'LMR',
    xlab = 'Day',
    main = 'Log-Mortality-Rate (LMR)')
```

Log-Mortality-Rate (LMR)



> Plot looks a little bit scrappy and you cannot see a solid 'line' to indicate that data follows an exponential mortality rate.

```
library(splines)

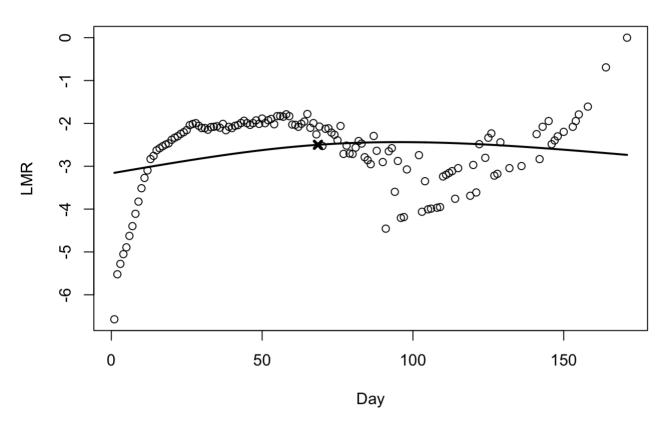
fit_ns_1 = lm(lmr ~ ns(Day, df = 2), data = mortality_rate)
pred1 = predict(fit_ns_1, newdata = list(Day=mortality_rate$Day))

fit_ns_2 = lm(lmr ~ ns(Day, df = 3), data = mortality_rate)
pred2 = predict(fit_ns_2, newdata = list(Day=mortality_rate$Day))

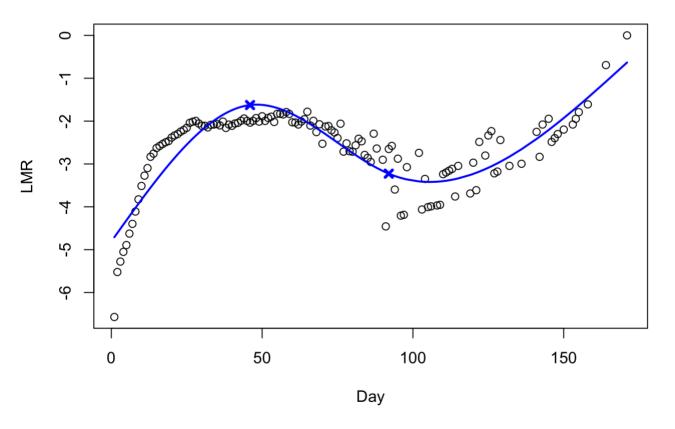
fit_ns_3 = lm(lmr ~ ns(Day, df = 16), data = mortality_rate)
pred3 = predict(fit_ns_3, newdata = list(Day=mortality_rate$Day))

fit_ns_4 = lm(lmr ~ ns(Day, df = 51), data = mortality_rate)
pred4 = predict(fit_ns_4, newdata = list(Day=mortality_rate$Day))
```

Natural cubic splies fit #1 (knots = 1)

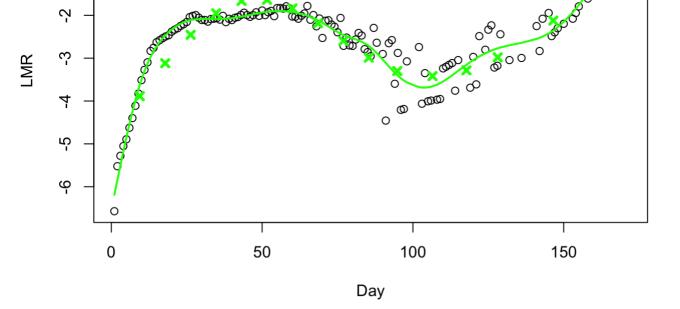


Natural cubic splies fit #2 (knots = 2)

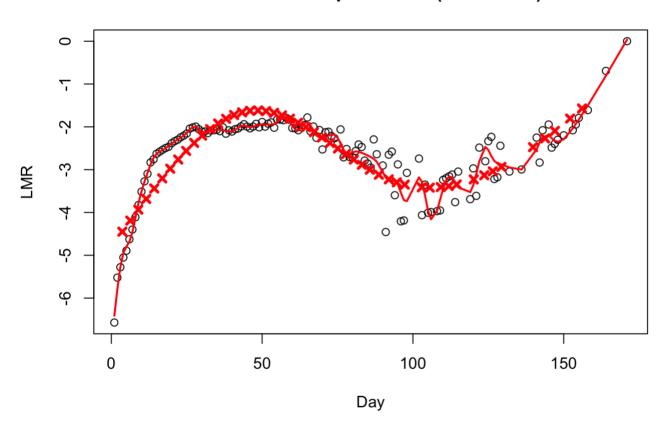


Natural cubic splies fit #3 (knots = 15)





Natural cubic splies fit #4 (knots = 50)



```
## Model #1 MSE: 0.80

## Model #2 MSE: 0.20

## Model #3 MSE: 0.08

## Model #4 MSE: 0.06
```

> Based on MSE model number four performs best. However with that many knots it can lead to overfit of the model. Model number three or even number two could be better choices. Needs more testing/validation.

```
# Calc MSE
calc mse = function(actual, pred) {
  return(mean((actual - pred) ** 2))
test = function(data, nknots) {
  mse_data = data.frame(matrix(nrow = 0, ncol = 4))
  # Column names based on the knots
  cnames = c()
  cnames_mse = c()
  for (x in 1:length(nknots)) {
    cnames[x] = paste(c('nkonts ', nknots[x]), collapse ='')
    cnames_mse[x]= paste(c('MSE_of_nkonts_', nknots[x]), collapse ='')
  }
  colnames(mse_data) = cnames
  # Fitting and data splitting
  for (i in 1:10) {
    set.seed(2707 + i)
    smp_size <- floor(0.7 * nrow(data))</pre>
    train_ind <- sample(seq_len(nrow(data)), size = smp_size)</pre>
    train <- data[train ind, ]</pre>
    test <- data[-train_ind, ]</pre>
    for (j in 1:length(nknots)) {
      fit = lm(lmr ~ ns(Day, df = nknots[j] + 1), data = train)
      pred lmr = predict(fit, newdata=list(Day=test$Day))
      # Warning: prediction from a rank-deficient fit may be misleading
      # A matrix that does not have "full rank" is said to be "rank deficient".
      # A matrix is said to have full rank if its rank is either equal to its
      # number of columns or to its number of rows (or to both).
      mse data[i, j] = calc mse(test$lmr, pred lmr)
    }
  }
  # Return data
  return data = vector(mode="list", length=5)
  names(return data) = c('MSE data', cnames mse)
  return data$MSE data = mse data
  for (c in 1:ncol(mse data)) {
    return_data[c + 1] = mean(mse_data[, c])
  }
  return (return data)
}
print(test(mortality rate, nknots=c(1, 2, 15, 50)))
```

```
## $MSE_data
##
       nkonts_1 nkonts_2 nkonts_15 nkonts_50
      1.2126710 0.2586166 0.13411374 0.2406041
     0.7586419 0.2247611 0.14333672 0.2001176
## 3 0.7671834 0.1851173 0.14391866 0.1879292
## 4
      0.8506521 0.1701308 0.05815796 0.1285059
## 5
     1.2539013 0.3078850 0.11833177 0.1939775
## 6
     0.8229711 0.2836649 0.12737188 0.1739669
## 7
      0.5195506 0.1946205 0.11513143 0.1882166
## 8 0.8361542 0.1941088 0.12766387 0.3611628
     0.8218388 0.2531594 0.09597262 0.1679729
## 9
## 10 1.2656458 0.3401780 0.13025601 0.2069081
##
## $MSE of nkonts 1
## [1] 0.910921
##
## $MSE_of_nkonts_2
## [1] 0.2412242
##
## $MSE of nkonts 15
## [1] 0.1194255
##
## $MSE of nkonts 50
## [1] 0.2049362
```

```
> Compared to 1 b MSEs are considerably higher. With this seed best MSE (1.56) is from model with fifthteen knots.
Model with fifty knots gives absurd MSE.
1.d.
 fit_smooth <- smooth.spline(x=mortality_rate$Day, y=mortality_rate$lmr, cv = T)</pre>
 pred lmr = predict(fit smooth, newdata=mortality rate)$y
 MSE=mean((mortality rate$lmr-pred lmr)^2)
 cat(sprintf('MSE: %.2g \n', MSE))
 ## MSE: 0.081
 cat(sprintf('Lambda: %.2g \n', fit smooth$lambda)) #Smoothing parameter
 ## Lambda: 6.2e-05
 cat(sprintf('Number of Knots: %s \n', fit smooth$fit$nk))
 ## Number of Knots: 76
 cat(sprintf('Avarage of the effective Degrees of Freedom: %.3g \n', fit smooth$df - 2))
 ## Avarage of the effective Degrees of Freedom: 12.4
```

> Smoothing splines performs effectively comprored to natural cubic splines with MSE of 0.081 and difference to best cubic models MSE is (0.119 - 0.081) 0.038.

Assignment 2: Comparison of GAMs with spline and loess basis functions

Pre

```
auto_mpg = read.table('auto-mpg.txt', header = T)

auto_mpg$year = factor(auto_mpg$year)
auto_mpg$origin = factor(auto_mpg$origin)

auto_mpg = auto_mpg[ , !(names(auto_mpg) %in% 'name')]

summary(auto_mpg)
```

```
##
                    cylinders
                                 displacement
                                                  horsepower
                                                                   weight
        mpa
                        :3.000 Min.
##
   Min. : 9.00
                Min.
                                       : 68.0 Min.
                                                      : 46.0 Min.
                                                                      :1613
                                               1st Qu.: 75.0
##
   1st Qu.:17.00
                 1st Qu.:4.000
                                1st Qu.:105.0
                                                               1st Qu.:2225
                 Median :4.000
                                Median :151.0
   Median :22.75
                                                Median: 93.5
                                                              Median :2804
##
##
   Mean :23.45
                 Mean :5.472
                                Mean :194.4 Mean :104.5 Mean
                                                                     :2978
##
   3rd Ou.:29.00
                  3rd Ou.:8.000
                                 3rd Ou.:275.8
                                                3rd Ou.:126.0
                                                               3rd Ou.:3615
##
   Max. :46.60
                 Max. :8.000
                                 Max.
                                      :455.0
                                                Max. :230.0 Max.
                                                                     :5140
##
##
    acceleration
                      year
                               origin
        : 8.00
##
                  73
                               1:245
  Min.
                        : 40
   1st Qu.:13.78
                  78
                        : 36
                               2: 68
##
                               3: 79
##
   Median :15.50
                 76
                        : 34
##
   Mean
          :15.54
                  75
                         : 30
##
   3rd Qu.:17.02
                  82
                        : 30
##
                         : 29
   Max. :24.80
                  70
##
                  (Other):193
```

```
#str(fit_lasso)
#getTrainPerf(fit_lasso)[1]

RMSE = fit_lasso$results$RMSE

cat(sprintf('Lasso best Model RMSE: %.4g', RMSE[which.min(RMSE)]))
```

```
## Lasso best Model RMSE: 3.144
```

```
# 2.b. Set up a GAM model with spline basis functions for all data
# with the train() function in the caret package and use LOOCV to find the best RMSE.
# Find a reasonable interval for the tuning parameter df. Present the table
# of the evaluated models and their model fit criteria.

library(gam)
# Build the GAM model based on splines and find best model with LOOCV
fit_gam_spline <- train(
   mpg~., data = auto_mpg, method = "gamSpline",
   scale = FALSE,
   trControl = trainControl("LOOCV", number = 1),
   tuneGrid = expand.grid(df = seq(1, 9, length = 9)))</pre>
```

```
fit gam spline
```

```
## Generalized Additive Model using Splines
##
## 392 samples
    7 predictor
##
##
## No pre-processing
## Resampling: Leave-One-Out Cross-Validation
## Summary of sample sizes: 391, 391, 391, 391, 391, 391, ...
## Resampling results across tuning parameters:
##
##
    df RMSE
                  Rsquared
##
        3.144266 0.8373873 2.404518
    1
##
       2.726054 0.8777006 1.992124
    2
##
       2.714038 0.8787980 1.973555
    3
##
    4
        2.731593 0.8772613 1.989474
##
       2.750592 0.8755802 2.006770
        2.769341 0.8739123 2.022423
##
     6
##
    7
        2.788327 0.8722171 2.037122
       2.807811 0.8704709 2.053446
##
    8
##
    9
        2.827439 0.8687046 2.069307
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was df = 3.
```

```
#summary(fit_gam_spline$finalModel)
cat(sprintf('GAM Split best model RMSE: %.4g', min(fit_gam_spline$results$RMSE)))
```

```
## GAM Split best model RMSE: 2.714
```

```
fit gam loess
```

```
## Generalized Additive Model using LOESS
##
## 392 samples
    7 predictor
##
##
## No pre-processing
## Resampling: Leave-One-Out Cross-Validation
## Summary of sample sizes: 391, 391, 391, 391, 391, 391, ...
## Resampling results across tuning parameters:
##
##
    span RMSE
                    Rsquared
##
    0.10 2.981868 0.8548833 2.182441
##
    0.15 2.847199 0.8669722 2.069900
##
    0.20 2.792291 0.8718846 2.039434
##
    0.25 2.784916 0.8725021 2.039142
##
    0.30 2.785448 0.8724393 2.031661
    0.35 2.767810 0.8740268 2.015848
##
##
    0.40 2.755734 0.8751059 2.005235
    0.45 2.745060 0.8760588 1.995748
##
##
     0.50 2.734399 0.8769991 1.986050
##
## Tuning parameter 'degree' was held constant at a value of 1
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were span = 0.5 and degree = 1.
```

```
cat(sprintf('GAM Loess best model RMSE: %.4g', min(fit_gam_loess$results$RMSE)))
```

```
## GAM Loess best model RMSE: 2.734
```

2.d. Best Model

```
# Present a plot of the regression coefficient/curves for the method that performed best.

# Best model is Generalized Additive Model using Splines

par(mfrow = c(3,4))
plot(fit_gam_spline$finalModel)
```

