

Objectives:

Upon completion of this SI session, participants will be able to:

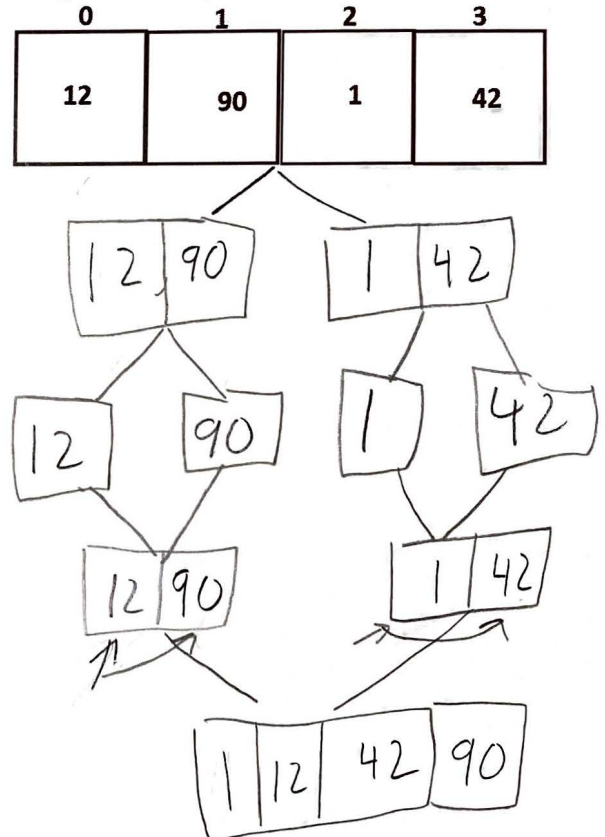
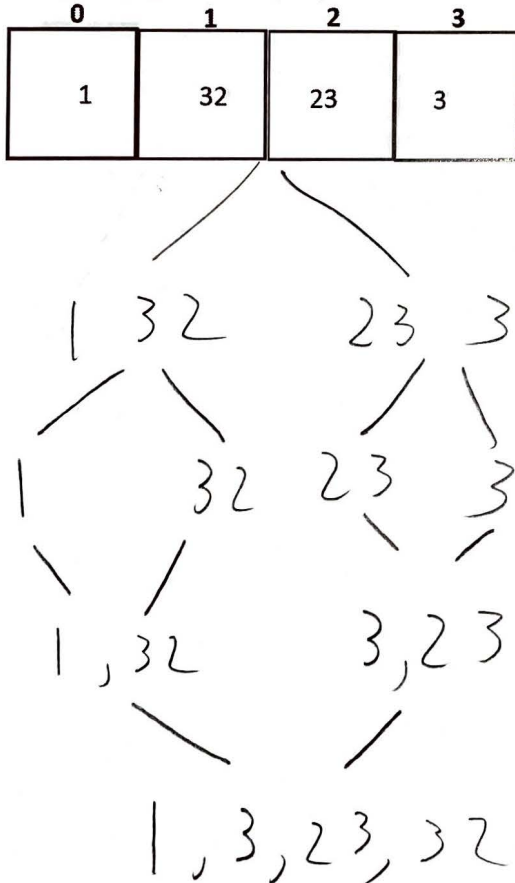
1. Recognize the big O expression of merge sort
2. Determine how arrays will look after cycles of merge sort

Foundations:

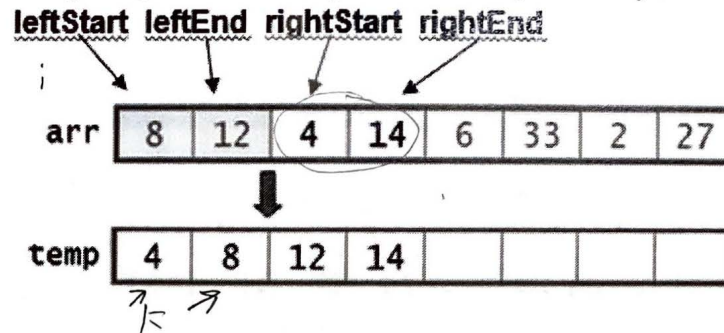
1. What are the steps for merge sort? Words: sort, merging, ~~divide~~, merging
- 1) divide array into left and right subarrays until size 1
- 2) While merging, sort
- 3) continue merging until sorted

Exercises:

2. Using a merge sort where you create a new array at each step, draw the phases of each array.



3. Finish the following merge code for merge sort with only two arrays.



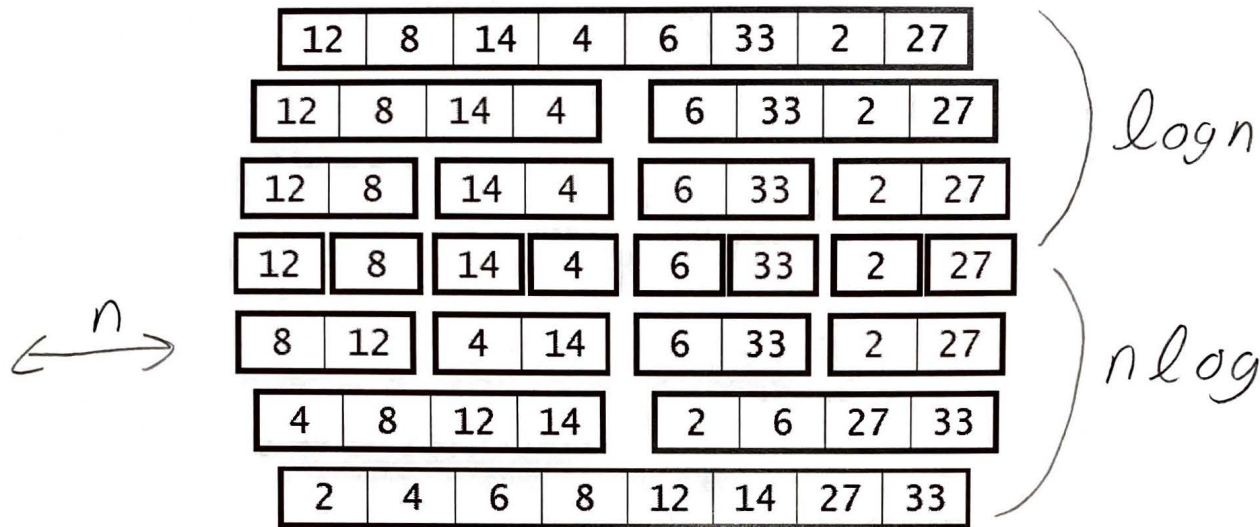
```
static void merge(int[] arr, int[] temp, int leftStart, int leftEnd, int rightStart, int rightEnd)
```

```
{
    int i = leftStart; // index into left subarray
    int j = rightStart; // index into right subarray
    int k = leftStart; // index into temp
    while ( i <= leftEnd && j <= rightEnd ) {
        if (arr[i] <= arr[j]) {
            temp[k] = arr[i];
            i++;
        }
        else {
            temp[k] = arr[j];
            j++;
        }
        k++;
    }
    /* Copy remaining elements of left array if any */
    while (i <= leftEnd)
    {
        temp[k] = arr[i];
        i++;
        k++;
    }

    /* Assume we copy the code from above but for right subarray*/

    for (i = leftStart; i <= rightEnd; i++) // copy back
        arr[i] = temp[i];
}
```

4. Let's figure out the Big O of merge sort intuitively.
Hint: How many levels get merged?



Big O: $n \log n$

Best: $n \log n$

Summary

5. What is the best case and worst case of merge sort for the implementation we talked about in class?

~~B~~

6. Given the following conditions, what sorting method would you use?
- The data is mostly sorted, but there are a few out of place elements
 - The data is random, shifting is expensive, and you have extremely limited memory.
 - The data is random and you have practically unlimited space in memory.

a) insertion, maybe shell

b) quicksort

c) merge

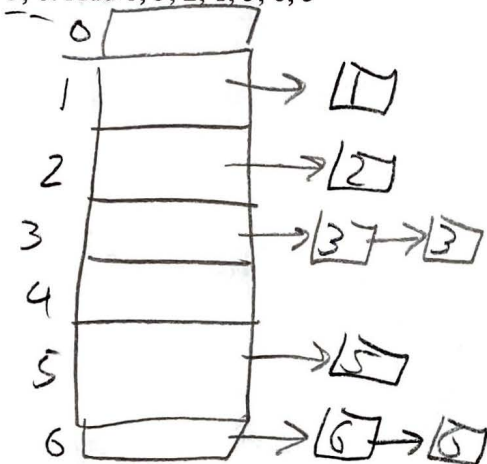
Objectives:

Upon completion of this SI session, participants will be able to:

1. Recognize Graph terminology

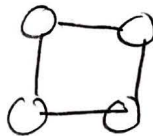
Exercises:

1. Using bucket sort, determine where the following numbers would go with buckets 1, 2, 3, 4, 5, 6. Add 6, 3, 2, 1, 5, 6, 3



1, 2, 3, 3, 5, 6, 6

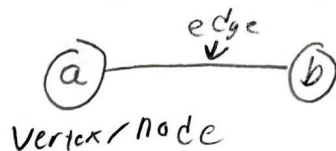
2. Draw a graph with a cycle



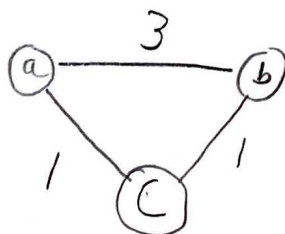
directed



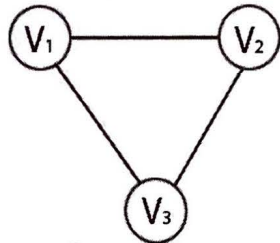
3. What is a vertex/node? What is an edge? Draw them



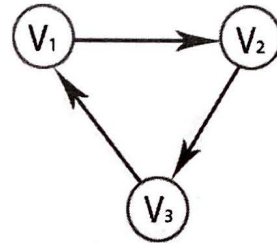
4. What is a weight?



5. Label the following graphs as directed or undirected graphs.



undirected

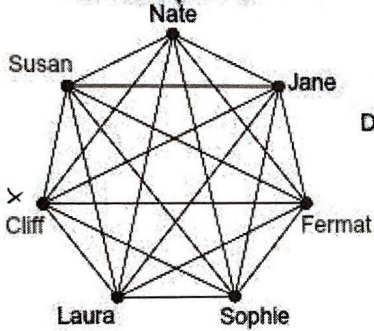


directed

6. Which of the following is a complete graph? Which is only a connected graph?

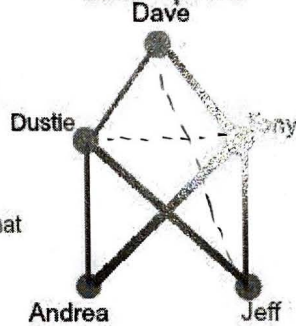
Social Media Graph Examples

Example 1



Complete

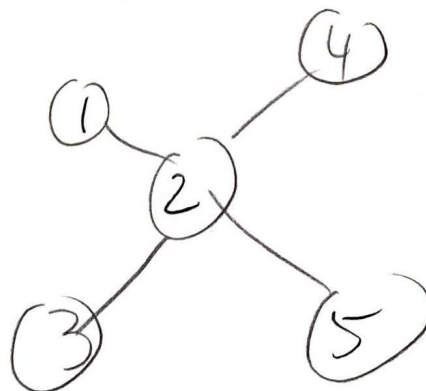
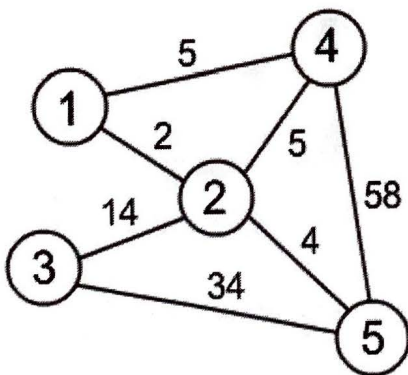
Example 2



connected

7. List the neighbors of 5. Draw a spanning tree

$n: 2, 3, 4$



also
others

8. Are the given graphs acyclic?

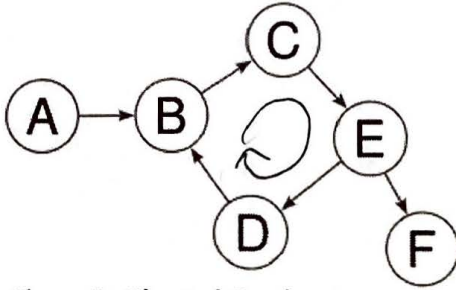
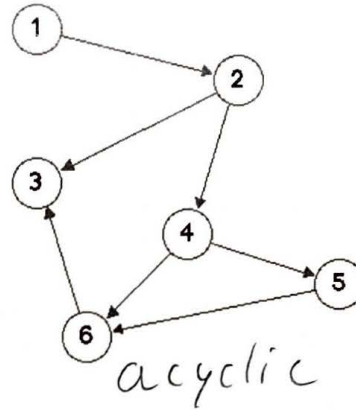


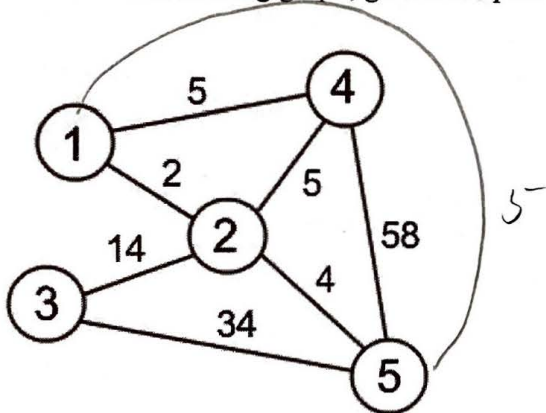
Figure 3 : Directed Graphs

Not



Summary

9. Given the following graph, give three paths from 1 to 4.

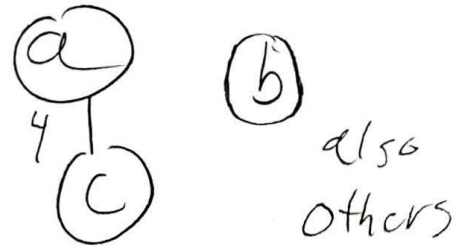


1 → 4

1 → 2 → 3 → 5 → 4

1 → 2 → 4

10. Draw a graph that is not connected but has three vertices a, b, and c that contain a path from a to c that costs 4.



Upcoming Events and Suggestions for Further Study:

Events:

- Next SI session is ~~Wednesday~~ ^{thurs} from 6:00 to 8:00 at Olin 313

Further Study:

- https://cwru.az1.qualtrics.com/jfc/form/SV_1Th0sizrbealYXz
 - Survey link
- In class lecture slides

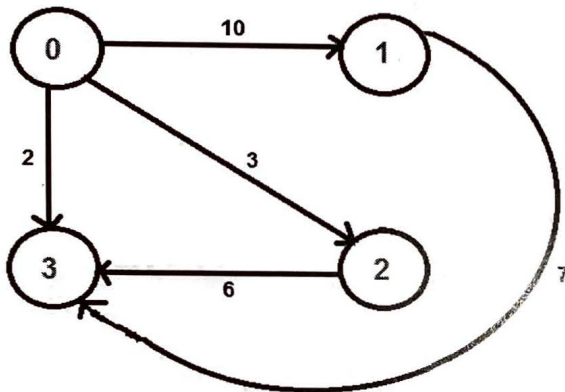
Objectives:

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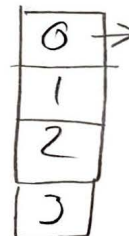
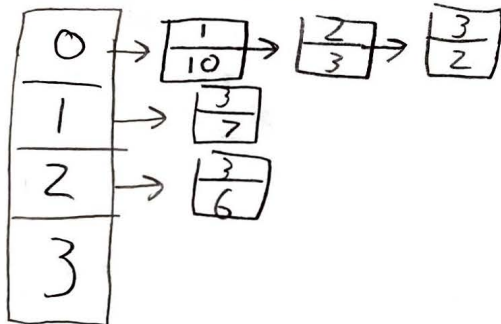
1. Determine how graphs look in matrix/list form
2. Traverse through a graph using breadth and depth strategies

Foundations:

1. Draw the following in adjacency matrix (2D array) and adjacency list (LL) form.



	0	1	2	3
0		10	3	2
1				7
2				6
3				



2. What are the steps for depth first search? Words: process, visited, neighbors

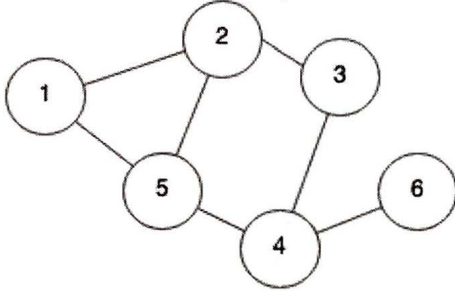
- a) Choose a starting vertex
 - b) Mark vertex as visited and process it
 - c) For all neighbors that aren't visited, recurse DFS on each (Choose neighbors in order of lowest to highest for convenience)
- process = print / if ()*

3. What are the steps for breadth first search? Words: queue, mark, queue

- a) Process starting vertex, mark, and place it in a queue
- b) Remove a vertex, v, from the front of the queue, process ✓
- c) For each unmarked neighbor u of v, process u, mark u, and then place u in the queue (since u may have further processed neighbors)
- d) Repeat b

Exercises:

4. Write the DFS (depth first search) and BFS (breadth first search) for the following graph



DFS: stack: ~~1~~, ~~2~~, ~~3~~, ~~4~~, ~~5~~, ~~6~~

visited: 1, 2, 3, 4, 5, 6

print: 1, 2, 3, 4, 5, 6

BFS: Q: ~~1~~, ~~2~~, ~~3~~, ~~4~~, ~~5~~, ~~6~~

marked: 1, 2, 5, 3, 4, 6

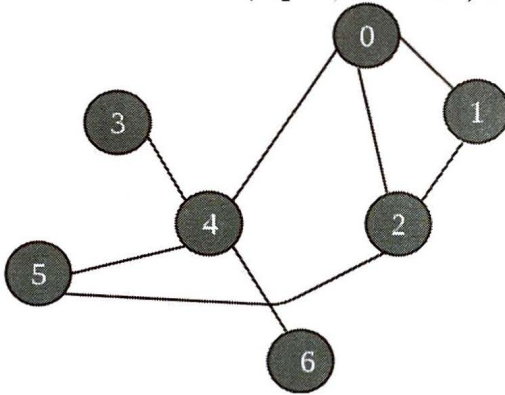
print: 1, 2, 5, 3, 4, 6

BFS: Q: ~~1~~, ~~2~~, ~~3~~, 4

marked: 1, 2, 5, 3, 4

print: 1, 2, 5

5. Write the DFS (depth first search) and BFS (breadth first search) for the following graph



DFS: 0, 1, 2, 5, 4, 3, 6

BFS: 0, 1, 2, 4, 5, 3, 6

6. Your coworker is on vacation and he doesn't name methods well. Determine what type of traversal this is and tell me how you know.

```
public void hawaii(int i, int parent){
    System.out.println(vertices[i].id);
    vertices[i].encountered = true;
    vertices[i].parent = parent;
    Iterator<Edge> edgeItr = edges.iterator();
    while(edgeItr.hasNext()){
        Edge curEdge = edgeItr.next();
        j = curEdge.endNode;
        if(vertices[j].encountered == false)
            hawaii(j, i);
    }
}
```

DFS

recursion

7. The following is Pseudocode that Dr. Ayday gave us in class. Fill in the missing pseudocode Trav(origin)

```

origin.parent = null
create a new Queue q
q.insert(origin)

while(!q.isEmpty())
    v = q.remove()
    process v

    for each vertex w in v's neighbors
        if w ! marked
            mark w as encountered
            w.parent = V
            q.insert(w)

```

Summary

8. Is it possible to implement DFS and BFS without recursion?

yes

9. What type of a graph would work well with an adjacency list implementation?

Sparse

10. What is the Big O of BFS when we use arrays?

~~$O(V+E)$~~ $O(V^2)$

11. What is the Big O of DFS when we use arrays?

~~$O(V+E)$~~ $O(V^2)$

Upcoming Events and Suggestions for Further Study:

Events:

- Next SI session is Wednesday from 6:00 to 8:00 at Sears 336

Further Study:

- https://cwru.az1.qualtrics.com/jfe/form/SV_1Th0sizrbealYXz
 - Survey link
- <https://www.hackerearth.com/practice/algorithms/graphs/breadth-first-search/tutorial/>
 - This contains a connection between the BFS of trees and graphs
- <https://www.geeksforgeeks.org/breadth-first-search-or-bfs-for-a-graph/>
 - A topic just for graph DFS
- All the websites above have their DFS equivalent

Objectives:

Upon completion of this SI session, participants will be able to:

1. Find the shortest path through a graph using Dijkstra's algorithm
2. Read/Create Dijkstra tables

Foundations:

1. Comment the steps of Dijkstra's algorithm

Choose a starting vertex A // *begin vertex*
 Create an array $D[v]$ to keep track of the distance from A to v // *distance of A to v*
 Create an array $P[v]$ to keep track of the parent of v // *holds parent of vertex v*
 Create a set N to keep track of nodes with least cost path known // *least cost path known*

For all vertex v

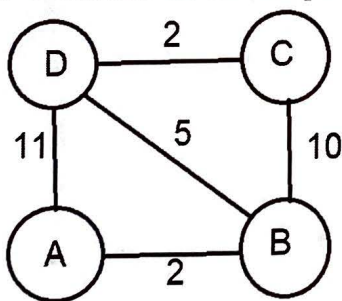
$D[v] = \text{infinity}$

$P[v] = \text{null}$

//The important part starts here

until all nodes are in N or we reach our target vertex // *until visited all or we visited our target*
 find w not in N with smallest $D[]$ value // *find vertex w that we haven't visited with smallest distance from A*
 add w to N // *visited*
 For each neighbor n not in N
 if $D[w] + c(w, n) < D[n]$ // *update*
 $D[n] = D[w] + c(w, n)$ // *Distance if we found a smaller one*
 $P[n] = w$ // *update parent*

2. Determine the shortest path from A to C



N
 A

A, B

A, B, D

A, B, D, C

$D[B], P[B]$ $D[C], P[C]$

$\frac{B}{2, A}$

$\frac{C}{\infty, \text{null}}$

$\frac{D}{11, A}$

12, B

7, B

9, D

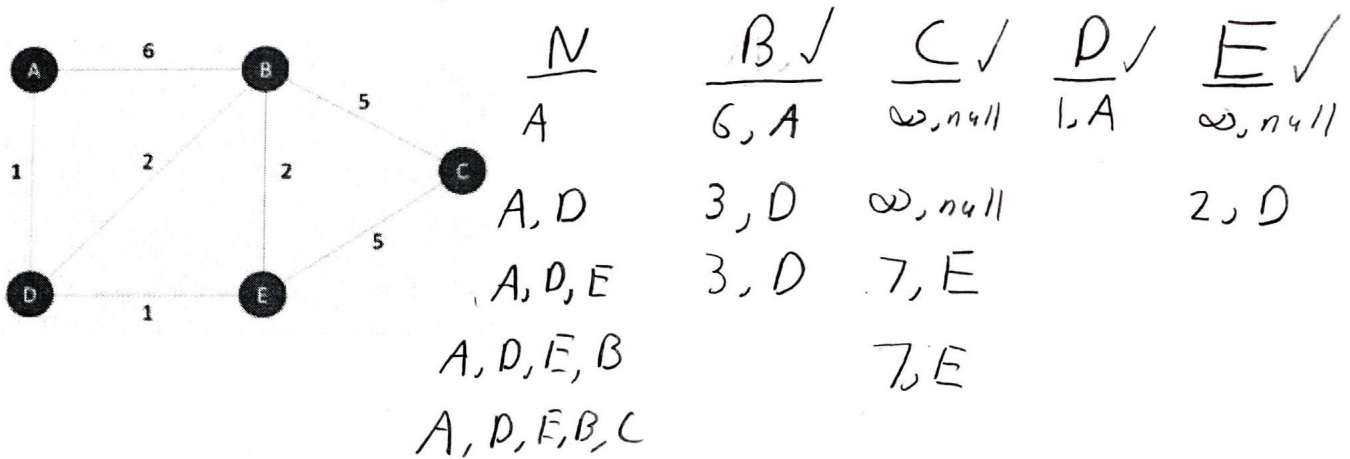
C, D, B, A

A \rightarrow B \rightarrow D \rightarrow C

9

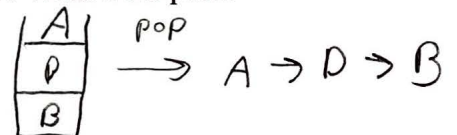
Exercises:

3. The president has tasked you with finding the shortest flight time from city A to all these individual cities in different trips that all start from A

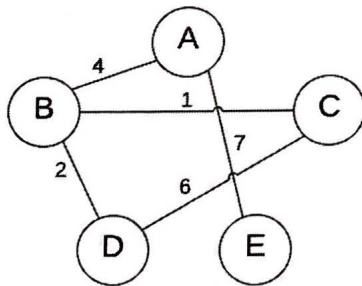


Using your chart, what would be the shortest flight time from A to B? What's the path?

3



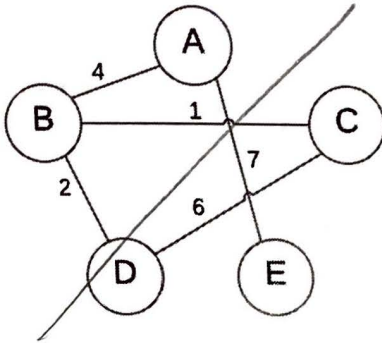
4. Determine the shortest path from A to C.



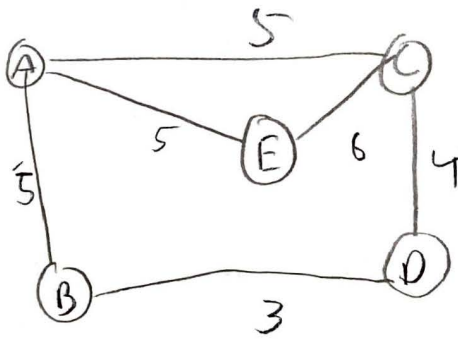
A → B → C

Summary

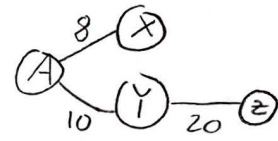
5. Determine the shortest path for all the vertexes. Start from A



<u>N</u>	<u>B</u> ✓	<u>C</u> ✓	<u>D</u>	<u>E</u> ✓
A	5, A	5, A	∞	5, A
A, B		5, A	8, B	5, A
A, B, C			8, B	5, A
			8, B	



A, B, C, E
A, B, C, E, D



6. Given the following chart, what was the total cost of the path of a to z?

Step	n	D(x), p(x)	D(y), p(y)	D(z), p(z)
0	a	8, a	10, a	infinite
1	a, x		10, a	infinite
2	y, a, x			30, y
3	z, y, a, x			

30

7. From the chart above, what was the path from a to z?

$z \rightarrow Y \rightarrow A \Rightarrow A \rightarrow Y \rightarrow z$

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Further Study:

- https://cwru.az1.qualtrics.com/jfe/form/SV_1Th0sizrbealYXz
 - Survey Link
- <https://www.youtube.com/watch?v=eFZCPIZCyIM>
 - If you're more inclined to videos, here's a nice video tutorial