

Upon completion of this SI session, participants will be able to:

- ### Exercises:

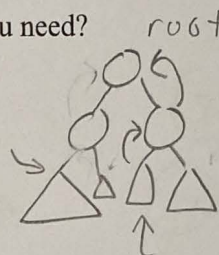
- right

- Left

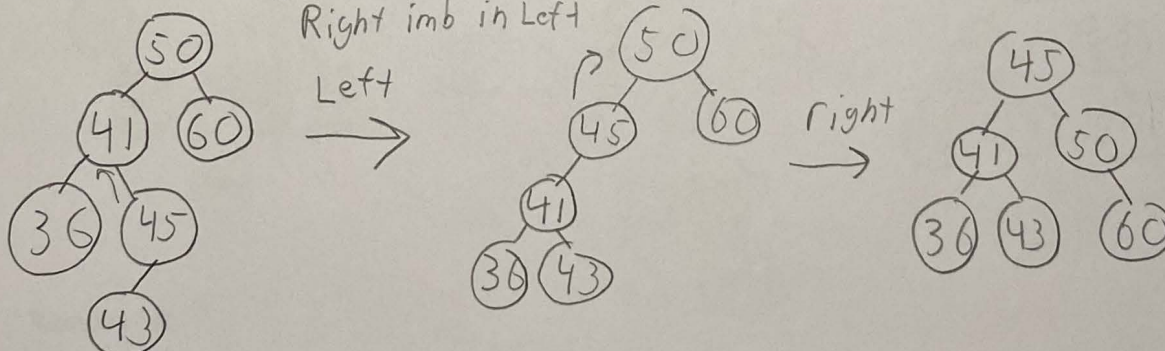
- right

- right +

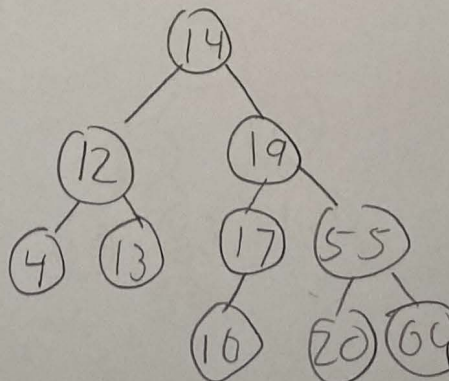
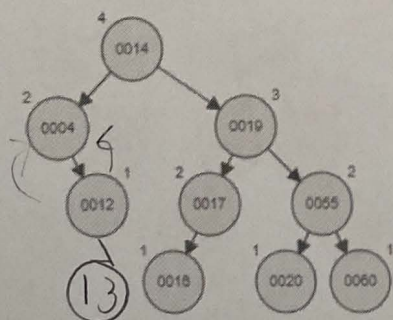
Left



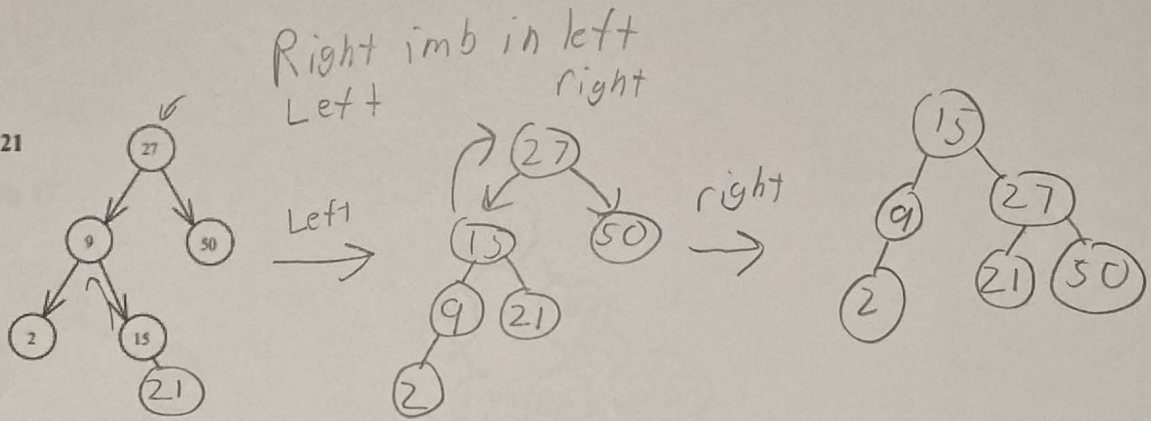
- Right imb in Left



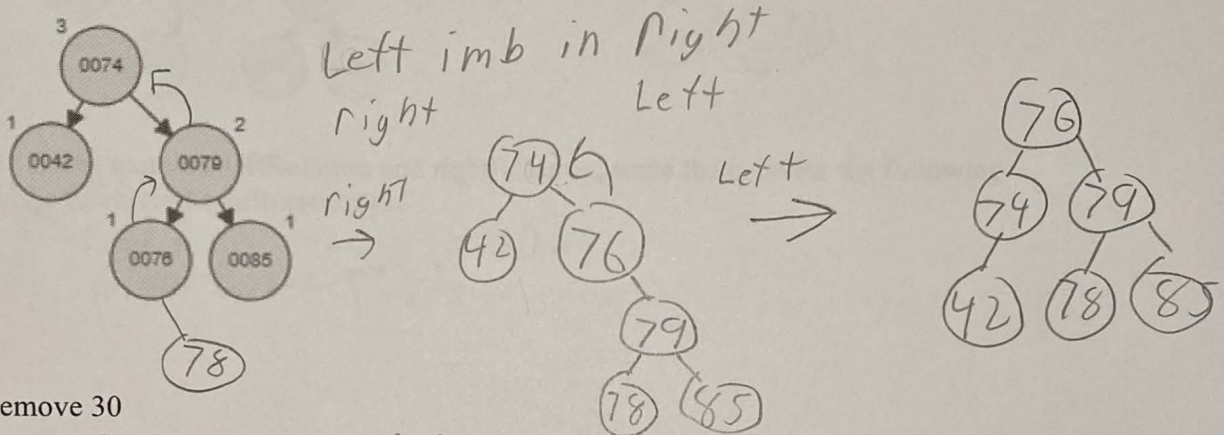
- Let +
→



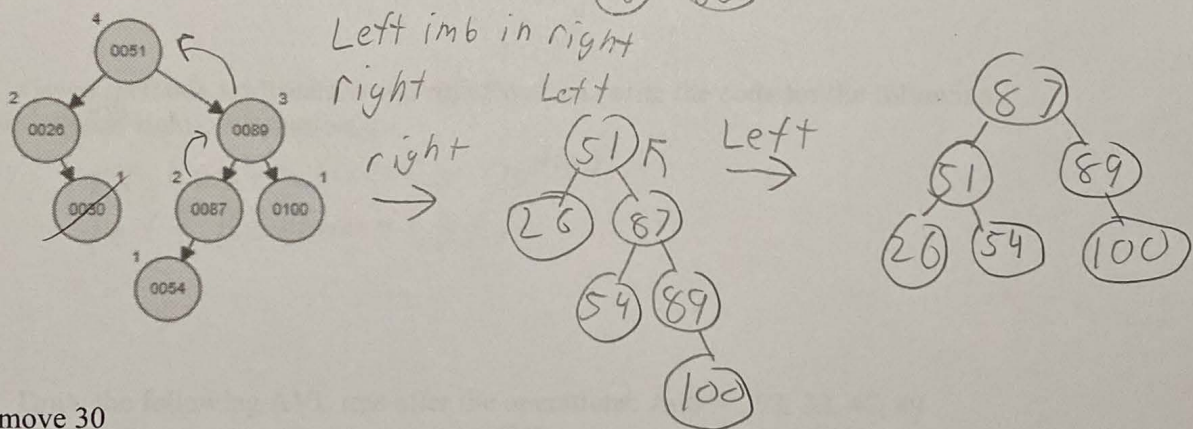
Insert 21



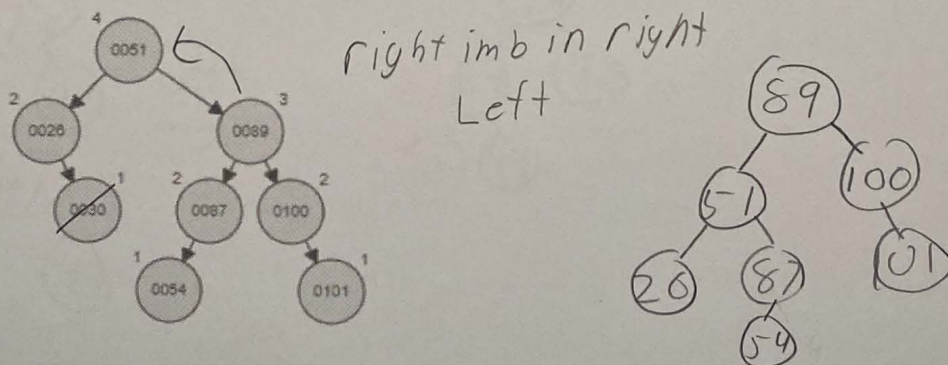
Add 78



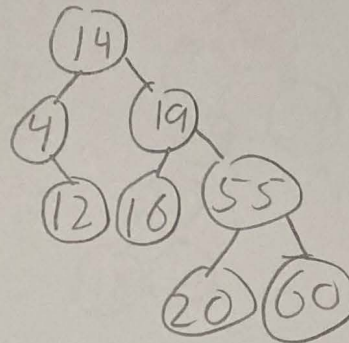
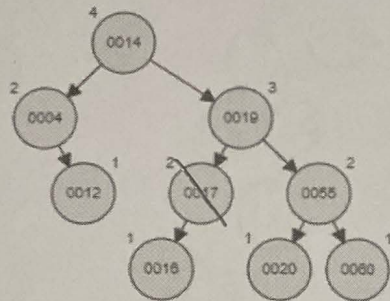
Remove 30



Remove 30



Remove 17



4. Given methods `leftRotation` and `rightRotation`, write the code for the following

```
public Node leftRightRotation(y){
    leftRotation(y.left);
    rightRotation(y);
```

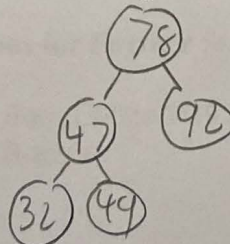
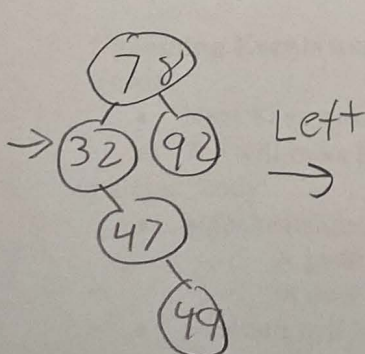
```
}
```

5. Given methods `leftRotation` and `rightRotation`, write the code for the following

```
public Node rightLeftRotation(y){
    rightRotation(y.right);
    leftRotation(y);
```

```
}
```

6. Draw the following AVL tree after the operations: Add 78, 92, 32, 47, 49



7. Draw the following AVL tree after the operations: Add 54, 42, 21, 18, 29, 26, 57

Diagram illustrating the insertion of 57 into a B+ tree structure, showing the sequence of operations and the resulting tree structure.

Initial Tree Structure (5 slots):

- Slot 1: 18
- Slot 2: 21
- Slot 3: 29
- Slot 4: 42
- Slot 5: 54

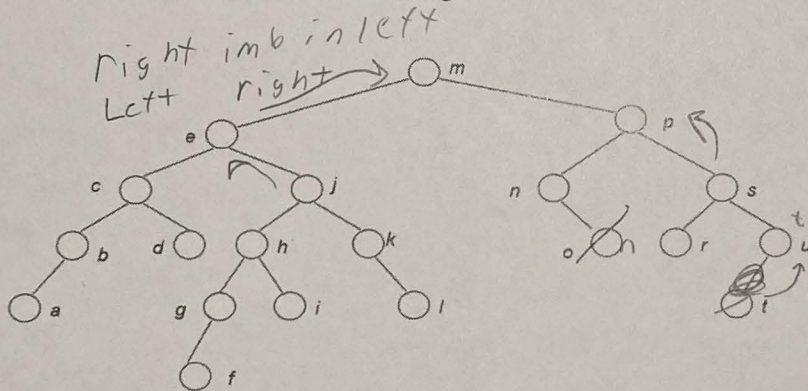
Operations:

- Insert 54 into the 4th slot.
- Insert 21 into the 2nd slot.
- Insert 29 into the 3rd slot.
- Insert 26 into the 5th slot.
- Insert 18 into the 1st slot.
- Insert 57 into the 5th slot.
- Merge 21 and 29 into the 3rd slot.
- Merge 29 and 42 into the 4th slot.
- Merge 42 and 54 into the 5th slot.
- Merge 54 and 57 into the 5th slot.

Final Tree Structure (4 slots):

- Slot 1: 18
- Slot 2: 21
- Slot 3: 42
- Slot 4: 57

Exercise: Delete o from the following AVL tree



Events:

- ### Further Study:

- bigocheatsheet.com
 - A great graph that visualizes the big o complexity chart. It also has the big O time of data structures and algorithms that we will cover in the future.
- Deletion will NOT be on the midterm, but it may show up in the homework.
- <https://www.cs.usfca.edu/~galles/visualization/AVLtree.html>
 - Practice AVL trees

EECS 233 SI Session 9
 Leader: Bertram Su
 October 5, 2019

Objectives:

Upon completion of this SI session, participants will be able to:

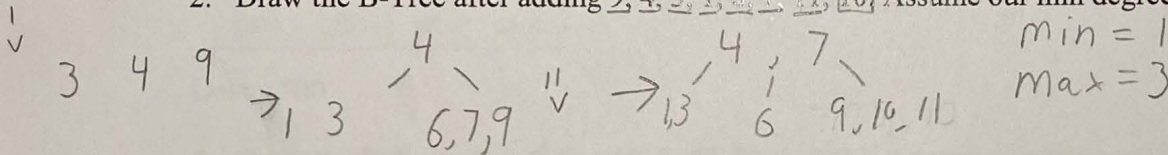
1. Recognize B-tree terminology
2. Determine what adding would do to a B-Tree of varying degrees

Foundations:

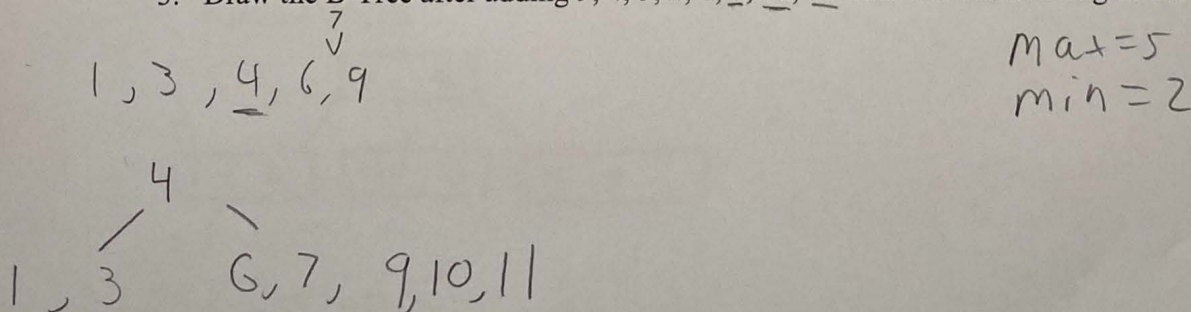
1. Given a minimum degree t
 - a) What's the minimum amount of keys each non-root node must have?
 $t-1$
 - b) What's the maximum amount of keys each node can contain?
 $2t-1$
 - c) What's the minimum amount of keys a root must have?
 1

Exercises:

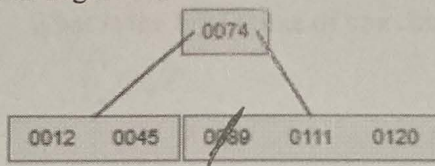
2. Draw the B-Tree after adding 9, 4, 3, 1, 4, 7, 11, 10. Assume our min degree is 2



3. Draw the B-Tree after adding 9, 4, 3, 1, 6, 7, 11, 10. Assume our min degree is 3



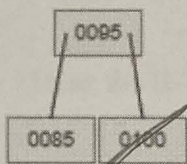
4. What are some possible B-Trees after the following operations?
Min degree = 3



$$\begin{aligned} \text{Max} &= 5 \\ \text{min} &= 2 \end{aligned}$$

Delete 89

- Min Degree = 2 (There are two possible solutions)

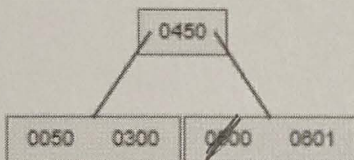


85, 95

$$\begin{aligned} \text{min} &= 1 \\ \text{max} &= 3 \end{aligned}$$

Delete 100

- Min Degree = 3

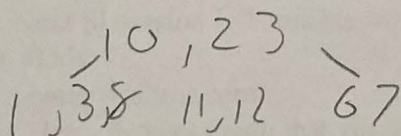


$$\begin{aligned} \text{Max} &= 5 \\ \text{min} &= 2 \end{aligned}$$

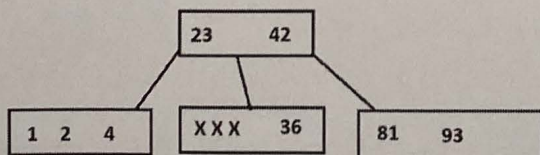
50, 300, 450, 601

Delete 500

5. Draw the B-Tree after adding 10, 3, 67, 23, 1, 8, 12. Assume min degree is 2



6. What is the possible range of values for the three variables X? The min 2 and assume no repeated integers



$$23 < X < 36$$

Summary

7. What is the big O time of searching for something in a B-Tree? $t \ll n$

$\log n$

8. When would we use B-Trees?

No rotations, going through memory
fewer random jumps

9. Draw the B-Tree after adding 10, 3, 67, 23, 1, 8, 12. Assume min is 3

$\begin{matrix} 8 \\ \downarrow \\ 1, 3, 10, 23, 67 \end{matrix} \rightarrow \begin{matrix} 10 \\ \swarrow \quad \searrow \\ 1, 3, 8 \quad 12, 23, 67 \end{matrix}$

degree

$\min = 2$

$\max = 5$

Upcoming Events and Suggestions for Further Study:

Events:

- Next SI session is Thursday from 1:00 to 2:30 at Sears 336

Further Study:

- bigocheatsheet.com
 - A great graph that visualizes the big o complexity chart. It also has the big O time of data structures and algorithms that we will cover in the future
- <https://www.cpp.edu/~ftang/courses/CS241/notes/b-tree.htm>
 - This website has examples of addition and removal