

# EECS 496: Sequential Decision Making

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# Announcements

- Exam TBA
  - In class, 75 minutes
  - Bring a calculator
- Possibility that one lecture in the upcoming two weeks will be canceled/rescheduled/given by a TA

# Recap

- In the automated planning problem, an agent is given (i) \_\_\_\_\_ (ii) \_\_\_\_\_ and (iii) \_\_\_\_\_. It needs to find a \_\_\_\_\_ which is a \_\_\_\_\_, often also \_\_\_\_\_ some criterion.
- In classical planning, we assume the world is \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_ and \_\_\_\_\_. Actions are \_\_\_\_\_.
- What is the “makespan”?
- We describe planning problems using \_\_\_\_\_ which take \_\_\_\_\_. These can be \_\_\_\_\_.
- States in STRIPS are \_\_\_\_\_ of \_\_\_\_\_ literals.
- What is the “closed world assumption”? Why is it useful?
- Goals in STRIPS are \_\_\_\_\_ of \_\_\_\_\_ literals.
- An action schema has an action \_\_\_\_\_ and \_\_\_\_\_, followed by lists of \_\_\_\_\_ and \_\_\_\_\_. The first contains a \_\_\_\_\_ of \_\_\_\_\_ literals. The second contains a \_\_\_\_\_ of literals.
- What are ADD and DELETE lists?
- What is the STRIPS assumption? Why is it useful?
- What are two kinds of planning algorithms?
- How do we formulate state space planning as a search problem?
- What is an admissible heuristic?
- We can formulate heuristics for planning through \_\_\_\_\_ plans or \_\_\_\_\_. \_\_\_\_\_ plans are obtained by \_\_\_\_\_ the \_\_\_\_\_ lists in \_\_\_\_\_. \_\_\_\_\_ are obtained by considering a \_\_\_\_\_ \_\_\_\_\_ at a time.
- Multiple admissible heuristics can be combined through the \_\_\_\_\_ function.

# Today

- Automated Planning (Ch 10 R&N)

# Backward State-Space Search

- Forward search has trouble with irrelevant actions
  - E.g., suppose there are 50 blocks on the table and I just want A on top of B
- This could be solved by backward search (“regression planning”)
  - But this requires “inverting” the search operators (i.e. the actions)
  - Fortunately this is easy to do for STRIPS

# Relevant Actions

- An action is relevant to a goal if its effects include at least one literal in the goal
- Suppose the goal is  $On(A,B)$ , then the only relevant actions are  $Move(A,x,B)$

# Backward State Space Search

- Start with the goal conjunction  $G$  (initial state)
- For each relevant action  $A$  (search operators), produce a new state by:
  - Deleting any literals in  $G$  that are added by  $A$
  - Adding all precondition literals of  $A$  to  $G$  (unless they are already present)
- Goal test: A state which is satisfied by the initial state of the planning problem

# Example

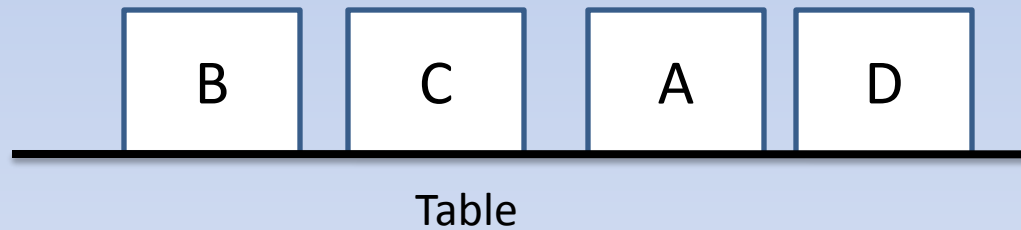
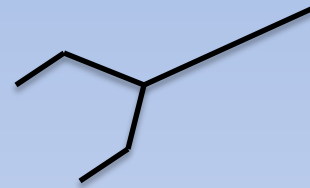
- Goal:  $On(A,B)$
- $Move(A,x,B)$ 
  - Preconditions:  $On(A,x), Clear(B), Clear(A)$
  - Add List:  $On(A,B), Clear(x)$
  - Delete List:  $On(A,x), Clear(B)$
- Result:  $On(A,C), Clear(B), Clear(A)$



# Kinds of Search for Planning

- Search algorithms for classical planning fall into two categories
  - “State space planners”: States of the search problem are states of the world; search operators are actions of the world
  - “Plan space planners”: States of the search problem are partial plans; search operators are modifications to the current partial plan

# Blocks World



Goal:  $On(A,B) \wedge On(C,D)$

Solutions:  $\{Move(A, Table, B), Move(C, Table, D)\},$   
 $\{Move(C, Table, D), Move(A, Table, B)\}$

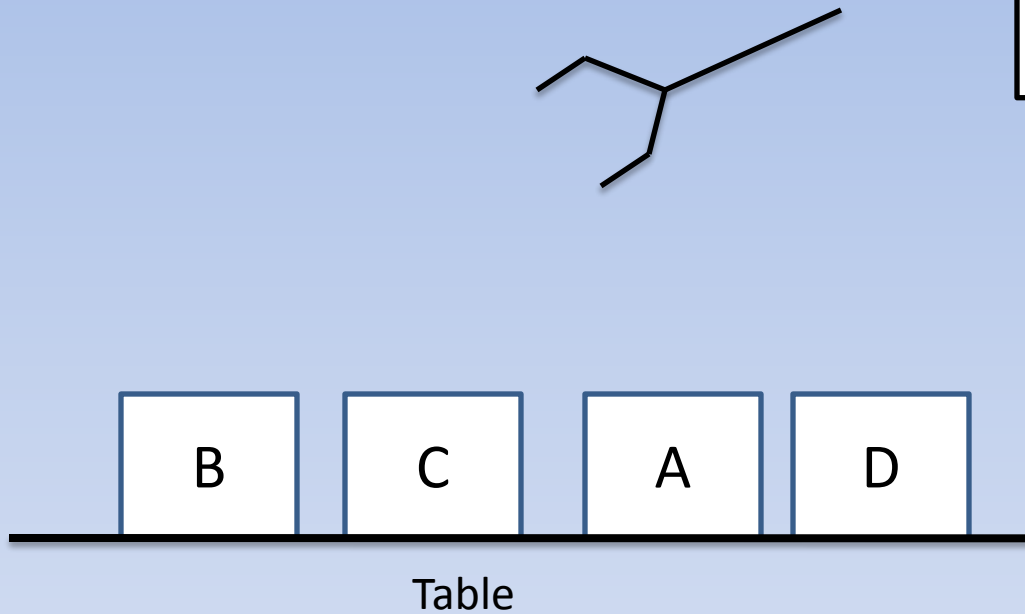
# Total Order Plans

- In a Total Order plan, every pair of actions  $A_1$  and  $A_2$  has a *temporal ordering constraint*
  - Either  $A_1$  is done first, or  $A_2$
  - Forward state space planners produce plans like this

# Partial Order Plans

- In many situations, actions do not have to be done in order
  - Might be trying to achieve unrelated things
- This creates a *partial order plan*: a plan with some actions that have no temporal ordering constraints between them
  - i.e. there is some  $A_1, A_2$  so that  $A_1$  does not have to be completed before  $A_2$  and  $A_2$  does not have to be completed before  $A_1$  for the plan to succeed

# Blocks World



Goal:  $On(A,B), On(C,D)$

A dummy action with no preconditions and effect==initial state

Start

Move(A,Table,B)

Move(C,Table,D)

End

A dummy action with no effects and preconditions==goal

# Partial Order Plans

- Represented as a set of actions and ordering constraints ( $A < B$ )
  - Ordering constraints can't introduce cycles
- Partial Order plans have three advantages over total order plans
  - Action Parallelism
  - Flexibility when executing the plan
  - (Partial) Failure resilience

# Finding a POP

- To find POPs, we will perform a *plan-space* search
- The states of the search space will be *incomplete POPs*, augmented with some bookkeeping information

# States of the POP Search Space

- A state will have
  - The incomplete POP (list of actions and ordering constraints)
  - A list of *open conditions*
  - A list of *causal links*



# Open Conditions

- A precondition of some action in the plan that is not currently the effect of some action in the plan
- The termination states of the search are those where this list is empty
- Initially, this is the goal, represented by the dummy action *End*

# Causal Links

- Suppose an action  $B$  in the incomplete POP has an open precondition  $p$
- Suppose the planner adds an action  $A$  to the POP that has  $p$  as an effect
- The *cause* for adding  $A$  is so it fulfils  $p$  for  $B$
- This is indicated in the POP by adding a *causal link*, denoted  $A \xrightarrow{p} B$

# Conflict and Threats

- Suppose the planner has just added  $A$  and a causal link  $A \xrightarrow{p} B$
- Suppose there is an action  $C$  in the plan that has  $\neg p$  as an effect and *could* be executed after  $A$  and before  $B$
- We say that  $C$  *conflicts with*, or *threatens*, the causal link  $A \xrightarrow{p} B$

# Consistent Plans

- A *consistent plan* is a POP where:
  - the ordering constraints have no cycles and
  - there are no conflicts with causal links
- So a solution is a consistent plan with no open conditions

# POP Search Algorithm

- Initial State: Plan= $(Start, End, Start < End)$ , open conditions=preconditions of  $End$  (goal), no causal links
- Search operators: Pick an open condition, and an action to satisfy it; generate next state (a new, consistent, possibly incomplete POP)
- Goal test: empty list of open conditions

# Generating the Next State

- Suppose we pick open condition  $p$  to satisfy, using action  $A$ 
  - $p$  must have been a precondition of some action  $B$
  - $A$  might be an action already in the plan

# Generating the Next State

- To generate the next state:
  - Remove  $p$  from list of open conditions
  - Add  $A$  to list of actions in POP (if not using existing)
  - Add ordering constraints  $Start < A, A < B, A < End$
  - Add  $A$ 's preconditions to list of open conditions
  - Add a causal link  $A \xrightarrow{p} B$
  - Resolve conflicts/threats if any

# Conflict Resolution

- Conflicts can arise between
  - The new causal link and existing actions
  - The new action and existing causal links
- To resolve a conflict, add ordering constraints
  - Suppose  $C$  conflicts with  $A \xrightarrow{p} B$
  - Then add either  $C < A$  or  $B < C$  (assuming no cycles)



# Example

- Init:  $At(Flat, Axle), At(Spare, Trunk)$
- Goal:  $At(Spare, Axle)$
- $Remove(Spare, Trunk)$ 
  - PRE:  $At(Spare, Trunk)$
  - EFF:  $\neg At(Spare, Trunk), At(Spare, Ground)$
- $Remove(Flat, Axle)$ 
  - PRE:  $At(Flat, Axle)$
  - EFF:  $\neg At(Flat, Axle), At(Flat, Ground)$
- $PutOn(Spare, Axle)$ 
  - PRE:  $At(Spare, Ground), \neg At(Flat, Axle)$
  - EFF:  $\neg At(Spare, Ground), At(Spare, Axle)$
- $LeaveOvernight$ 
  - PRE:
  - EFF:  $\neg At(Spare, Trunk), \neg At(Spare, Ground), \neg At(Spare, Axle), \neg At(Flat, Axle), \neg At(Flat, Ground)$