

Claim: Let A, B, C be $n \times n$ Matrices. Then $A + B = B + A$.

Proof: In order to show that these two matrix expressions are equal, we need to show that $(A + B)_{ij} = (B + A)_{ij}$ for any indices $1 \leq i, j \leq n$.

$$\begin{aligned} & (A + B)_{ij} \\ = & A_{ij} + B_{ij} && \text{Definition of Matrix Addition} \\ = & B_{ij} + A_{ij} && \text{Commutativity of Addition for Real Numbers} \\ = & (B + A)_{ij} && \text{Definition of Matrix Addition (Reverse)} \end{aligned}$$

Thus showing that $(A + B)_{ij} = (B + A)_{ij}$ as desired.