Data Description: The dataset used for this project is the Netflix Movie Rating Dataset from Kaggle (Source: https://www.kaggle.com/netflix-inc/netflix-prize-data)

This dataset is large enough to build a good recommendation model and is adapted from 'Netflix Prize Dataset' which is so large that programmers may face memory issues while training a model using that dataset.

Movie file description: Movie_ID, Name, Year Rating file description: Movie_ID, User_ID, Name, Year

Let us build a Latent - Factor Based Recommender System to recommend movies to users. Part 1: Setting up the data:

```
In [1]: from collections import defaultdict
         import scipy
         import scipy.optimize
         import numpy
         import random
         path = "D:/TRL/OneDrive/CourseraPython/Final Course4/NetflixRatingData/Netflix Data
 In [2]:
         path2 = "D:/TRL/OneDrive/CourseraPython/Final_Course4/NetflixRatingData/Netflix_Dat
In [3]: f = open(path)
In [4]: header = f.readline()
In [5]: header = header.strip().split(',')
In [6]:
         header
Out[6]: ['User_ID', 'Rating', 'Movie_ID']
In [7]:
        dataset = []
 In [8]: for line in f:
             fields = line.strip().split(',')
             d = dict(zip(header, fields))
             d['Rating'] = int(d['Rating'])
             d['User_ID'] = int(d['User_ID'])
             d['Movie_ID'] = int(d['Movie_ID'])
             dataset.append(d)
In [9]: type(d['User_ID']), type(d['Movie_ID']), type(d['Rating'])
         (int, int, int)
Out[9]:
In [10]:
        dataset[0]
         {'User_ID': 712664, 'Rating': 5, 'Movie_ID': 3}
Out[10]:
In [11]: # create a dictionary with movie data, i.e. movie id, year of release
         # and movie name
         f2 = open(path2)
         header = f2.readline()
         header = header.strip().split(',')
```

```
movie_data = []
          for line in f2:
              fields2 = line.strip().split(',')
              d = dict(zip(header, fields2))
             movie data.append(d)
In [12]: movie_data[0]
         {'Movie_ID': '1', 'Year': '2003', 'Name': 'Dinosaur Planet'}
Out[12]:
In [13]:
         movie_data[0]['Movie_ID']
          '1'
Out[13]:
In [14]:
         k = [item for item in movie_data if item['Movie_ID']=='1']
Out[14]: [{'Movie_ID': '1', 'Year': '2003', 'Name': 'Dinosaur Planet'}]
In [15]: for i in movie_data:
              if i['Movie_ID'] == '1':
                  print(i)
                  break
          {'Movie ID': '1', 'Year': '2003', 'Name': 'Dinosaur Planet'}
In [16]: type(movie_data), type(movie_data[0])
Out[16]: (list, dict)
```

Part 2: Finding Similarities Predict a rating to a new movie based on the ratings given to movies by a user and the movie names. We can also calculate the total votes and helpful votes for each movie.

```
In [17]: # users per movie refer to the no. of Netflix users who watched and rated a movie
# movies per user refer to the no. of movies that were rated by netflix users.
UsersPerMovie = defaultdict(set)
MoviesPerUser = defaultdict(set)

MovieNames = {}

for d in dataset:
    user,movie = d['User_ID'], d['Movie_ID']
    UsersPerMovie[movie].add(user)
    MoviesPerUser[user].add(movie)
```

Functions to find Similarities:

Jaccard function calculates similarity between two movies: by dividing the number of users who watched both the movies by the number of users who watched either movie.

MostSimilar function: takes an input of a movie id "m_ID" and a value n that is the number of similar movies (i.e. movie ids) that we need to output from the function. This function will then return the n most similar movies to the movie 'm_ID'

```
In [18]: def Jaccard(s1,s2):
    numerator = len(s1.intersection(s2))
```

```
denominator = len(s1.union(s2))
    return numerator / denominator

In [19]:

def MostSimilar(m_ID,n):
    similarities = []
    users = UsersPerMovie[m_ID]
    for i in UsersPerMovie:
        if i == m_ID: continue
        sim = Jaccard(users,UsersPerMovie[i])
        # this is the similarity between number of users who watched movie m_ID and similarities.append((sim,i))
    similarities.sort(reverse=True)
```

```
In [20]: UsersPerMovie[3] # number of users who watched movie 3
```

return similarities[:n]

```
{1687564,
Out[20]:
           2334738,
           704538,
           294943,
           1130533,
           2015275,
           2646060,
           2170930,
           2531380,
           966716,
           983123,
           2588755,
           2154579,
           1056859,
           2646115,
           1204327,
           458859,
           966771,
           1269875,
           1081461,
           540794,
           32902,
           2318471,
           540807,
           1859725,
           368786,
           565401,
           303270,
           532649,
           2113709,
           2564278,
           1925306,
           2375867,
           1876156,
           745661,
           2359486,
           2572475,
           1007809,
           2490563,
           745688,
           2138332,
           1949919,
           262367,
           745706,
           1269998,
           1704175,
           1630448,
           966899,
           2253048,
           868600,
           237824,
           2105602,
           565510,
           786695,
           2269450,
           254222,
           401681,
           1646880,
           57633,
           2523426,
           2253090,
           1392933,
           835881,
           2031917,
```

2040110, 360757, 2384185, 352571, 1859908, 1130826, 2072907, 524628, 311641, 868700, 1868129, 2589029, 950631, 606570, 2597239, 794999, 2425210, 344444, 1270144, 762240, 1171843, 1507727, 2613654, 1565082, 41371, 2326945, 1450405, 1573289, 1589677, 156078, 1196471, 2630072, 1114552, 1278394, 1204665, 2539966, 2212303, 1040848, 25049, 2384355, 2531820, 213486, 1614320, 2040306, 1982967, 2171387, 2384389, 983558, 2621962, 1532433, 1163795. 2007573, 442911, 2032162, 573995, 639533, 2130480, 238130, 1401399, 115267, 2122313, 2433609, 2490971,

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201338, 2232958, 2601604, 340618, 1806991, 234141, 553632, 373416, 823979, 4783, 586421, 373441, 406219, 2241241, 709342, 439011, 1045221, 250597, 2142951, 1594095, 1389295, 316155, 1364733, 1086213, 2437901, 504593, 2331421, 1733406, 2519847, 2224936, 504624, 2331444, 2470712, 2118461, 299857, 2446163, 78684, 2126686, 545639, 979820, 1012590, 86901, 1446775, 2282361, 152441, 2495357, 2192258, 2216837, 1799047, 1749903, 1241999, 2012052, 2274199, 766872, 2331547, 586652, 127911, 1897386, 693162, 1717162, 1168312, 2200505, 1037245, 1373119, 1684416,

```
86987,
480206,
2307036,
2569181,
136160,
660454,
168939,
2159596,
1561588,
586741,
2135038,
332805,
46086,
496645,
2552842,
2421781,
513050,
963611,
1872926,
668703,
1045551,
37939,
1250364,
701514,
2331728,
78931,
308307,
2159701,
2249828,
1627242,
1217660,
283774,
357507,
1307784,
152713,
1741962,
603277,
46222,
971925,
570522,
...}
```

```
In [21]: # the following gives the number of movies in the dictionary UsersPerMovie.
# against each movie i, we have a list of users who watched and rated that
# movie
for i in UsersPerMovie:
    print(i)
```

13/6

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```
4485
4488
4490
4492
4493
```

Getting a recommendation:

```
In [22]: m_ID = 3
          MostSimilar(m_ID,5)
Out[22]: [(0.12352209085252022, 3301),
           (0.11056751467710371, 4450),
           (0.08810335546384353, 1479),
           (0.08634175691937425, 3404),
           (0.08425055033019811, 4155)]
In [23]:
          print(i)
          m_ID
          4496
Out[23]:
In [24]: # Now, we need to find the movie names using the the dataset: movie_data
          # MovieNames[movie data[movie]] = d['Name']
          MovieNames = [movie data[i[1]-1] for i in MostSimilar(m ID,5)]
In [25]:
          #MostSimilar(m ID,5)[0][1]
          #MostSimilar(m ID,5)[0]
          MostSimilar(m_ID,5)
Out[25]: [(0.12352209085252022, 3301),
           (0.11056751467710371, 4450),
           (0.08810335546384353, 1479),
           (0.08634175691937425, 3404),
           (0.08425055033019811, 4155)]
          MovieNames
In [26]:
          [{'Movie_ID': '3301', 'Year': '1994', 'Name': 'Burnt by the Sun'}, {'Movie_ID': '4450', 'Year': '1987', 'Name': 'Pelle the Conqueror'},
Out[26]:
           {\mbox{'Movie\_ID': '1479', 'Year': '2002', 'Name': 'Man on the Train'},}
           {'Movie_ID': '3404', 'Year': '2000', 'Name': 'Not One Less'},
           {'Movie_ID': '4155', 'Year': '2000', 'Name': 'East/West'}]
```

Part 3: Collaborative - Filtering Based Rating Estimation

This part is to make predictions about user's ratings. Specifically, a user's rating for a movie is assumed to be a weighted sum of their previous ratings, weighted by how similar the query movie is to each of their previous views.

```
In [27]: ratingsPerUser = defaultdict(list)

for d in dataset:
    user,movie = d['User_ID'], d['Movie_ID']
    ratingsPerUser[user].append(d)
    ratingsPerMovie[movie].append(d)
```

```
# Calculate the mean rating of the entire dataset
In [28]:
          import numpy as np
          mean_rating = np.mean([dataset[i]['Rating'] for i in range(len(dataset))])
          mean_rating
          3.590569909383486
Out[28]:
In [29]:
          dataset[15]
          {'User_ID': 1694958, 'Rating': 3, 'Movie_ID': 3}
Out[29]:
In [30]: # Function to predict rating of a movie based on a user and a movie
          def PredictRating(user, movie):
              ratings = []
              similarities = []
              for d in ratingsPerUser[user]: # i.e. all the movies and ratings by the user.
                  i = d['Movie ID']
                  if i == movie: continue
                  ratings.append(d['Rating'])
                  users = UsersPerMovie[movie]
                  similarities.append(Jaccard(users,UsersPerMovie[i]))
              if(sum(similarities) > 0):
                  weightedRatings = [(x*y) \text{ for } x,y \text{ in } zip(ratings, similarities)]
                  return sum(weightedRatings) / sum(similarities)
              else:
                  return mean rating
          user, movie = dataset[10]['User ID'], dataset[10]['Movie ID']
In [31]:
          PredictRating(user, movie)
          3.553601713242338
Out[31]:
          dataset[0]
In [32]:
         {'User_ID': 712664, 'Rating': 5, 'Movie_ID': 3}
Out[32]:
          Part 4: Evaluating Performance By calculating MSE
In [33]:
         def MSE(predictions, labels):
              differences = [(x-y)**2 \text{ for } x,y \text{ in } zip(predictions, labels)]
              return sum(differences) / len(differences)
In [34]: p_mean = [mean_rating for d in dataset]
In [36]: # To reduce computation time, the size of the dataset has been reduced to 100
          predictions = []
          count = 0
          for d in dataset[:1000]:
              predictions.append(PredictRating(d['User_ID'], d['Movie_ID']))
              count= count+1
          count
In [37]:
          1000
Out[37]:
          PredictRating(d['User_ID'], d['Movie_ID'])
In [38]:
```

In this case, our rating prediction model was better in terms of MSE than predicting the mean rating.

Latent Factor based Recommender Systems

```
In [43]: # This is from above:
          ratingsPerUser = defaultdict(list)
          ratingsPerMovie = defaultdict(list)
          for d in dataset:
              user,movie = d['User_ID'], d['Movie_ID']
              ratingsPerUser[user].append(d)
              ratingsPerMovie[movie].append(d)
In [44]: # Get the Length of the dataset and the above dictionaries
          # due to computational issue, the size of the dataset was reduced
          dataset = dataset[:1000]
          N = len(dataset)
          nUsers = len(ratingsPerUser) # number of users
          nMovies = len(ratingsPerMovie) # number of movies
          # Get the list of keys
          users = list(ratingsPerUser.keys())
         movies = list(ratingsPerMovie.keys())
          # calculate the variables of our model: alpha, userBiases and MovieBiases
          alpha = sum([d['Rating'] for d in dataset])/ len(dataset)
          UserBiases = defaultdict(float)
         MovieBiases = defaultdict(float)
          def MSE(predictions, labels):
              differences = [(x-y)**2 \text{ for } x,y \text{ in } zip(predictions, labels)]
              return sum(differences)/len(differences)
In [45]: # LFM = Latent Factor Model
          def Prediction_LFM(user,movie):
              return alpha + UserBiases[user] + MovieBiases[movie]
In [46]: # unpack function to unpack the vector theta into the offset and bias terms
          def unpack(theta):
              global alpha
```

```
global UserBiases
              global MovieBiases
              alpha = theta[0]
              UserBiases = dict(zip(users, theta[1:nUsers+1])) # is the +1 reqd here?
              MovieBiases = dict(zip(movies, theta[1+nUsers:]))
In [47]: # we will find theta such that the foll cost function is optimised:
          # this gives the regularized MSE of the solution:
          def cost(theta, labels, lamb):
              unpack(theta)
              predictions = [Prediction_LFM(d['User_ID'], d['Movie_ID']) for d in dataset]
              cost = MSE(predictions, labels)
              print("MSE = " + str(cost))
              for u in UserBiases:
                 cost += lamb*UserBiases[u]**2
              for i in MovieBiases:
                 cost += lamb*MovieBiases[i]**2
              return cost
In [48]:
         # the derivative function:
          def derivative(theta, labels, lamb):
             unpack(theta)
              N = len(dataset)
              dalpha = 0
              dUserBiases = defaultdict(float)
              dMovieBiases = defaultdict(float)
              for d in dataset:
                  u,i = d['User_ID'], d['Movie_ID']
                  pred = Prediction_LFM(u,i)
                  diff = pred - d['Rating']
                  dalpha += 2/N*diff
                  dUserBiases[u] += 2/N*diff
                  dMovieBiases[i] += 2/N*diff
              for u in UserBiases:
                 dUserBiases[u] += 2*lamb*UserBiases[u]
              for i in MovieBiases:
                  dMovieBiases[i] += 2*lamb*MovieBiases[i]
              dtheta = [alpha] + [dUserBiases[u] for u in users] + [dMovieBiases[i] for i in
              return numpy.array(dtheta)
In [49]: # MSE when always predicting mean
          p_mean = [alpha for d in dataset]
          labels = [d['Rating'] for d in dataset]
         MSE(p_mean, labels)
         0.9525439999999995
Out[49]:
         # The gradient descent model using scipy:
In [50]:
          scipy.optimize.fmin_l_bfgs_b(cost, [alpha] + [0.0]*(nUsers+nMovies),
                                       derivative, args = (labels, 0.001))
```

```
MSE = 0.95254399999999995
         MSE = 1.951199431486239
         MSE = 0.9805295329824282
         MSE = 0.9536613460427796
         MSE = 0.9525871148504756
         MSE = 0.9525446716409175
         MSE = 0.9525437663728146
         MSE = 0.9525439339219235
         MSE = 0.9525439853029469
         MSE = 0.952543996863862
         MSE = 0.952543999336417
         MSE = 0.9525439998598355
         MSE = 0.9525439999704095
         MSE = 0.9525439999937427
         MSE = 0.952543999998686
         MSE = 0.952543999999725
         MSE = 0.9525439999999505
         MSE = 0.9525439999999831
         MSE = 0.95254400000000086
         MSE = 0.9525439999999844
         MSE = 0.952543999999936
Out[50]: (array([3.616, 0. , 0.
                                    , ..., 0. , 0. , 0. ]),
          0.9525439999999936,
          {'grad': array([ 3.616e+00, -2.768e-03, -7.680e-04, ..., 0.000e+00, 0.000e+00,
                   0.000e+00]),
            'task': 'ABNORMAL TERMINATION IN LNSRCH',
            'funcalls': 21,
            'nit': 0,
            'warnflag': 2})
```

The Complete Latent Factor Model:

```
In [51]: # For each user and item, we now have an additional low-dimensional
         # descriptor of user's preferences of dimension K = gamma_u. And, a
         # K dimensional representation of each item = gamma k
         # Model: f(u,i) = alpha + beta u + beta i + qamma u*qamma i
         # the gamma term is the interaction term which tries to answer :
         # Are the user preferences consistent with the item's properties?
         UserBiases = defaultdict(float)
         MovieBiases = defaultdict(float)
         UserGamma = {}
         MovieGamma = {}
         K = 2
In [52]: for u in ratingsPerUser:
             UserGamma[u] = [random.random()*0.1 - 0.05 for k in range(K)]
         for i in ratingsPerMovie:
             MovieGamma[i] = [random.random()*0.1 - 0.05 for k in range(K) ]
         # unpack function taking into account additional terms
In [53]:
         def unpack(theta):
             global alpha
             global UserBiases
             global MovieBiases
             global UserGamma
             global MovieGamma
             index = 0
             alpha = theta[index]
             index += 1
```

```
UserBiases = dict(zip(users, theta[index: index+nUsers]))
              index += nUsers
              MovieBiases = dict(zip(movies,theta[index:index+nMovies]))
              index += nMovies
              for u in users:
                  UserGamma[u] = theta[index:index+K]
                  index+=K
              for m in movies:
                 MovieGamma[m] = theta[index:index+K]
                  index += K
In [54]: def inner(x,y):
              return sum([a*b for a,b in zip(x,y)])
In [55]: def prediction(user, movie):
              return alpha + UserBiases[user] + MovieBiases[movie] + inner(UserGamma[user],
          def cost(theta,labels, lamb):
              unpack(theta)
              predictions = [prediction(d['User ID'], d['Movie ID'])]
              cost = MSE(predictions, labels)
              print("MSE=" + str(cost))
              for u in users:
                  cost+=lamb*UserBiases[u]**2
                  for k in range(K):
                      cost += lamb*UserGamma[u][k]**2
              for i in movies:
                  cost += lamb* MovieBiases[i] **2
                  for k in range(K):
                      cost += lamb*MovieGamma[i][k]**2
              return cost
In [56]: def derivative(theta, labels, lamb):
              unpack(theta)
              N = len(dataset)
              dalpha = 0
              dUserBiases = defaultdict(float)
              dMovieBiases = defaultdict(float)
              dUserGamma = {}
              dMovieGamma = {}
              for u in ratingsPerUser:
                  dUserGamma[u] = [0.0 for k in range(K)]
              for i in ratingsPerMovie:
                  dMovieGamma[i] = [0.0 for k in range(K)]
              for d in dataset:
                  u,i = d['User_ID'], d['Movie_ID']
                  pred = prediction(u, i)
                  diff = pred - d['Rating']
                  dalpha += 2/N*diff
                  dUserBiases[u] += 2/N*diff
                  dMovieBiases[i] += 2/N*diff
                  for k in range(K):
                      dUserGamma[u][k] += 2/N*MovieGamma[i][k]*diff
                      dMovieGamma[i][k] += 2/N*UserGamma[u][k]*diff
              for u in UserBiases:
                  dUserBiases[u] += 2*lamb*UserBiases[u]
                  for k in range(K):
                      dUserGamma[u][k] += 2*lamb*UserGamma[u][k]
              for i in MovieBiases:
                  dMovieBiases[i] += 2*lamb*MovieBiases[i]
                  for k in range(K):
                      dMovieGamma[i][k] += 2*lamb*MovieGamma[i][k]
              dtheta = [dalpha] + [dUserBiases[u] for u in users] + [dMovieBiases[i] for i ir
```

```
for u in users:
                  dtheta += dUserGamma[u]
              for i in movies:
                  dtheta += dMovieGamma[i]
              return numpy.array(dtheta)
         MSE(p_mean, labels)
In [57]:
         0.9525439999999995
Out[57]:
In [58]:
         scipy.optimize.fmin_l_bfgs_b(cost, [alpha] +
                                              [0.0]*(nUsers+nMovies) +
                                              [random.random() * 0.1 - 0.05 for k in range(K*(
                                       derivative, args = (labels, 0.001), maxfun = 10, maxit
         MSE=1.9148411401272962
         MSE=1.9135443686957903
         MSE=1.908351404372158
         MSE=49.902015833867964
         MSE=7.554367849469394
         MSE=2.0606398692270873
         MSE=1.9104139175357417
         MSE=1.9083790176369813
         MSE=1.9083517740075149
         MSE=1.908351409320141
         MSE=1.9083514044383916
         MSE=1.908351404373045
         MSE=1.90835140437217
         MSE=1.908351404372158
         MSE=1.9083514043721652
         MSE=1.908351404372158
         MSE=1.908351404372158
         MSE=1.9083514043721617
         MSE=1.908351404372158
         MSE=1.908351404372158
         MSE=1.9083514043721603
         MSE=1.908351404372158
         MSE=1.908351404372158
         MSE=1.9346718047939926
         MSE=1.908799954878752
         MSE=1.9083590345464339
         MSE=1.9083515341630124
         MSE=1.908351406579925
         MSE=1.9083514044097125
         MSE=1.9083514043727972
         MSE=1.908351404372169
         MSE=1.908351404372158
         MSE=1.9083514043721652
         MSE=1.908351404372158
         MSE=1.9083514043721628
         MSE=1.908351404372158
         MSE=1.908351404372158
         MSE=1.9083514043721603
         MSE=1.908351404372158
         MSE=1.908351404372158
         MSE=1.9083514043721592
         MSE=1.908351404372158
         MSE=1.908351404372158
```

Using the latent factor method, the rating prediction model is worse than predicting ratings using the dataset mean rating in terms of the MSE.

In]:	
In	[]:	
In]:	