

## ASSIGNMENT 3

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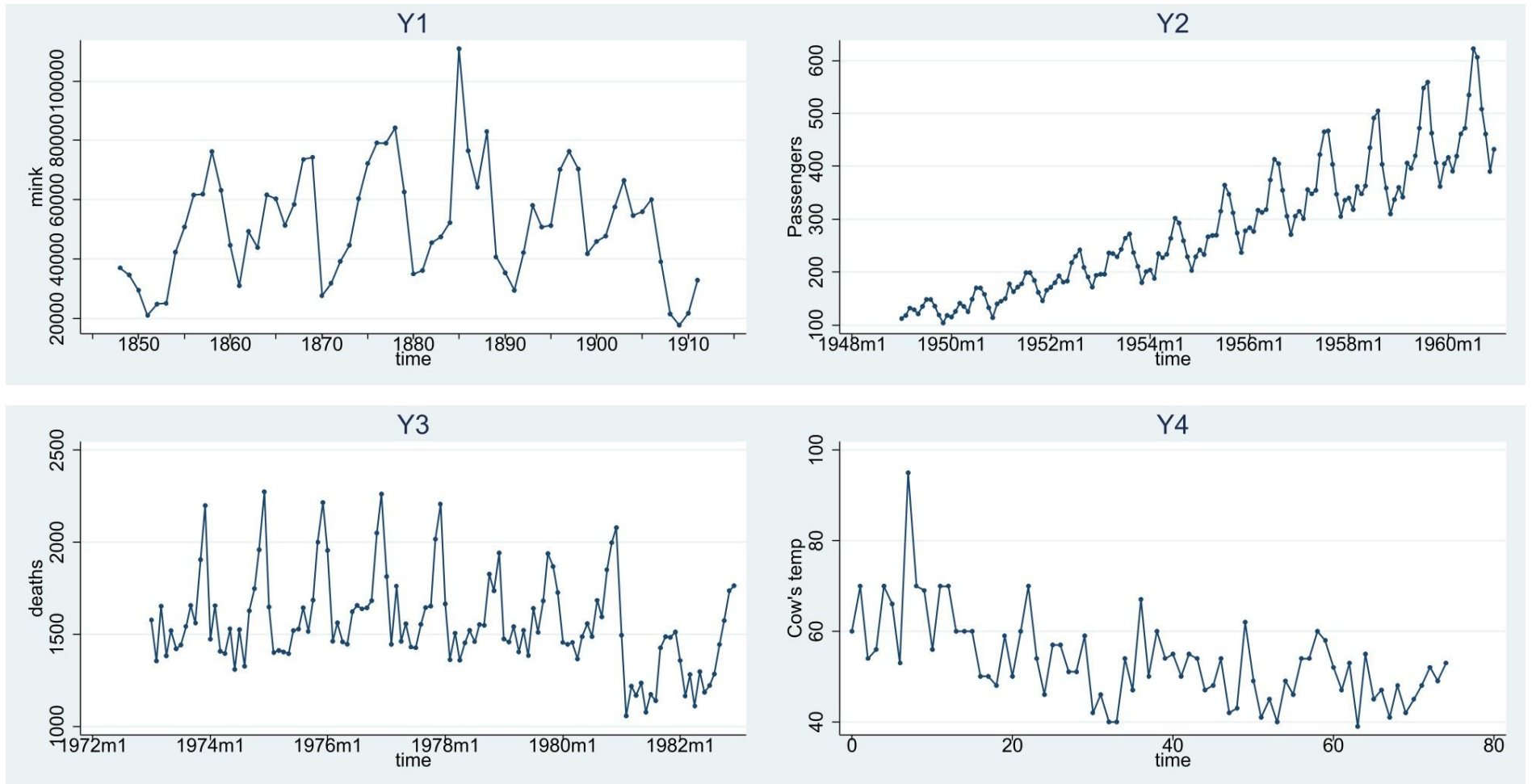
**Question 1 (20 points):** Prove that this time deterministic process is not stationary:

$$Y_t = \beta_0 + Y_{t-1} + \varepsilon_t$$

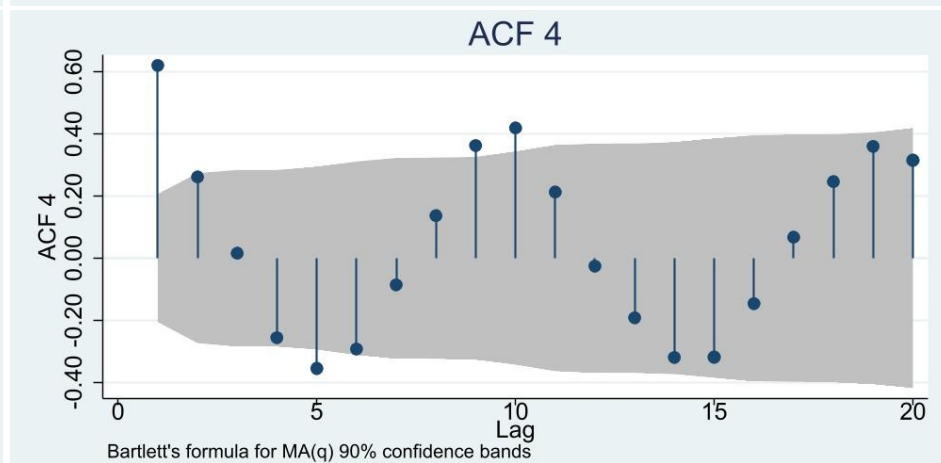
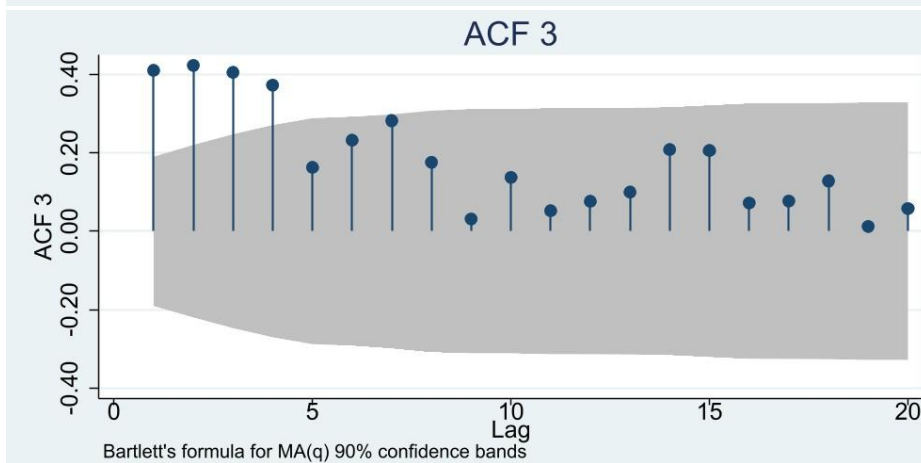
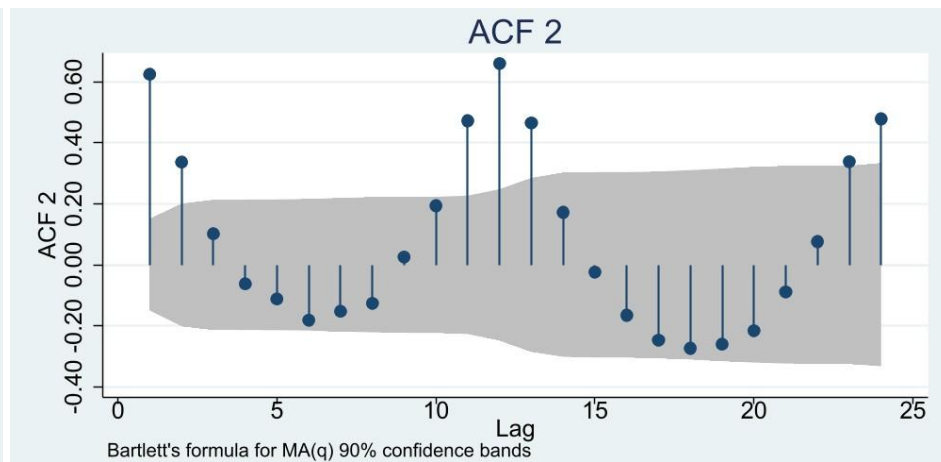
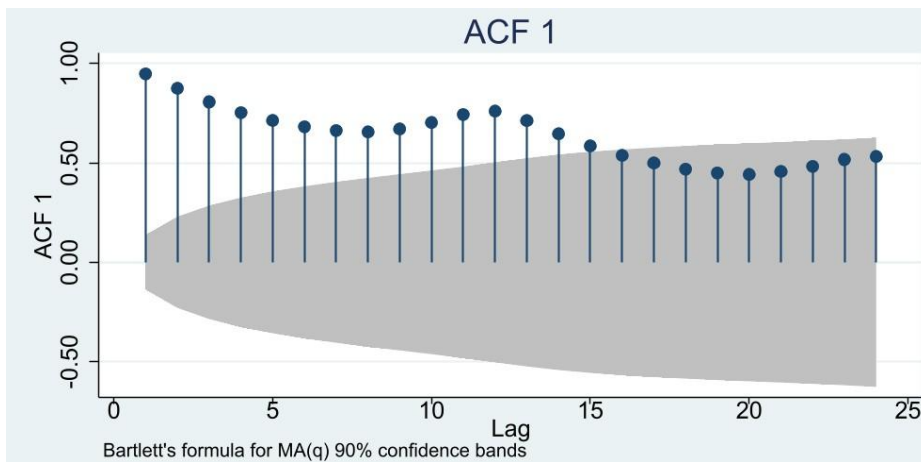
**Question 1 (30 points):** There are four time series plots and ACF plots for four variables:  $y_{1t}$ ,  $y_{2t}$ ,  $y_{3t}$ ,  $y_{4t}$ . Identify which ACF plot corresponds to each time series variable. Information about each time series:

- $y_1$ : Number of minks trapped in northern Canada, 1848–1911.
- $y_{2t}$ : Number of airline passengers, 1949–1960.
- $y_{3t}$ : Number of deaths from accidents in the U.S., 1973–1982.
- $y_{4t}$ : Morning temperature of a cow over a period of 75 days.

## Time plots:



## ACF plots:



**Questions 3 (50 points):** Import these four variables (from the specified sheets):

1. Stock prices of Vinamilk — sheet *VNM*.
2. Seasonally adjusted US CPI — sheet *PC*.
3. Seasonally adjusted US unemployment rate — sheet *PC*.
4. Non-seasonally adjusted US CPI — sheet *PC*.

Then perform these tasks:

- i. Provide the appropriate data format for each variable.
- ii. Plot each time series and its sample autocorrelation function (ACF).
- iii. Conduct unit-root tests to determine whether each variable is stationary at level ( $I(0)$ ) or requires first differencing ( $I(1)$ ). You may apply transformations to achieve stationarity where appropriate (examples: first differences, log differences, or seasonal differences).  
For each variable:
  - Report which tests you used (e.g., Augmented Dickey–Fuller (ADF), Phillips–Perron, KPSS) and the test specification (trend/constant/no constant and lag selection method).
  - Present test results in a concise table showing: test name, test statistic, p-value (or critical values), and your stationarity decision at conventional significance levels (e.g., 1%, 5%, 10%).
  - A short interpretation (3–5 sentences) summarizing final results and how you transformed each variable for stationarity.