

## Second Examination Study Guide

1. Understand what is meant by *random variables*, and *discrete* versus *continuous* quantitative random variables.
  2. Understand what is meant by the *probability distribution* of a discrete random variable.
  3. Understand what is meant by a *population distribution* and a *sampling distribution*.
  4. Be able to compute the *mean*, *variance*, and *standard deviation* of a discrete random variable from its probability distribution (when given as a table of values and probabilities).
  5. Know how to compute probabilities using the probability distribution of a *discrete* random variable.
  6. Know how to compute probabilities using the probability distribution of a *continuous* random variable.
  7. Know how to compute probabilities using a *normal* probability distribution (with [statdistributions.com](http://statdistributions.com)).
  8. Know how to *derive* a sampling distribution using the five-step method.
  9. Know how to use the *binomial distribution* to derive the sampling distribution of  $\hat{p}$ .
  10. Know how to find/compute the mean and standard deviation of  $\bar{x}$  and  $\hat{p}$ .
  11. Know how to find the interval that has a probability of approximately 0.95 of containing  $\bar{x}$  or  $\hat{p}$ .
  12. Understand what it means to say that a statistic is *unbiased*.
  13. Understand what is meant by the *standard error* of a statistic.
  14. Understand what is implied by the *central limit theorem*.
  15. Why do we divide by  $n - 1$  rather than  $n$  when computing  $s^2$ ?
  16. Be sure you know the notation (i.e., symbols) we have used (e.g.,  $\mu$ ,  $\sigma$ ,  $\sigma^2$ ,  $p$ ,  $\bar{x}$ ,  $\hat{p}$ ,  $n$ ,  $\mu_x$ ,  $\mu_{\bar{x}}$ ,  $\mu_{\hat{p}}$ ,  $\sigma_x$ ,  $\sigma_{\bar{x}}$ ,  $\sigma_{\hat{p}}$ ).
- Formulas/expressions you should understand when and how to use.

$$\mu = \sum_x xP(x) \quad \sigma^2 = \sum_x (x - \mu)^2 P(x) \quad \sigma = \sqrt{\sum_x (x - \mu)^2 P(x)}$$

$$z = \frac{x - \mu}{\sigma}$$

$$P(s) = \frac{n!}{s!(n-s)!} p^s (1-p)^{n-s}$$

$$\sigma_{\bar{x}} = \sigma_x / \sqrt{n} \quad \sigma_{\hat{p}} = \sqrt{p(1-p)/n}$$