Wednesday, Mar 2

Estimation Equations

Parameter	Point Estimate	Standard Error	Margin of Error	Confidence Interval	Design
p	\hat{p}	$\sqrt{rac{\hat{p}(1-\hat{p})}{n}}$	$z\sqrt{rac{\hat{p}(1-\hat{p})}{n}}$	$\hat{p} \pm z \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$	A
μ	$ar{x}$	$\frac{s}{\sqrt{n}}$	$t\frac{s}{\sqrt{n}}$	$\bar{x} \pm t \frac{s}{\sqrt{n}}$	A
μ	$ar{x}$	$\frac{s}{\sqrt{n}}\sqrt{1-\frac{n}{N}}$	$t\frac{s}{\sqrt{n}}\sqrt{1-\frac{n}{N}}$	$\bar{x} \pm t \frac{s}{\sqrt{n}} \sqrt{1 - \frac{n}{N}}$	В
au	$Nar{x}$	$N\frac{s}{\sqrt{n}}\sqrt{1-\frac{n}{N}}$	$tN\frac{s}{\sqrt{n}}\sqrt{1-\frac{n}{N}}$	$N\bar{x} \pm t\dot{N}\frac{s}{\sqrt{n}}\sqrt{1-\frac{n}{N}}$	В

Design A: Sampling with replacement, an infinite number of observational units, or N is much larger than n.

Design B: Sampling without replacement.

Assumptions when Using these Equations

We are making certain assumptions about the sampling distribution of a point estimate when using the equations above. We assume that the statistic is unbiased, that we can compute (approximately) the correct standard error, and that the shape of the sampling distribution is approximately normal.

The Mean of the Statistic

A statistic is **unbiased** if *its mean equals the parameter being estimated*, otherwise the statistic is said to be **biased**.

Sources of bias:

- 1. **Sampling bias**: Failure to account for the fact that some units are more or less likely to be included in the sample.
- 2. Non-response bias: Failure to observe some observational units that were intended to be observed.
- 3. Response bias: Errors in observation/measurement of the variable of interest.

In surveys, *sampling bias* can be eliminated through the use of a *random sampling* design (aka "probability sampling" or "scientific sampling"). One example is what is known as a **simple random sampling** design where *every possible sample of n units is equally likely*. Our formulas assume that the survey sampling design is simple random sampling.

The Standard Deviation of the Statistic

Recall that the *standard deviation of a statistic* is also called the **standard error**, which is used to compute the *margin of error*, the *confidence interval*, and *test statistics* (which we will discuss after the third examination).

The design can affect the standard error (e.g., sampling with versus without replacement).

The Shape of the Statistic's Sampling Distribution

To have a sampling distribution that is (approximately) normal in shape, we need at least one of the following two conditions:

- 1. The population distribution is (approximately) normal in shape.
- 2. The sample size (n) is sufficiently large.

Shape of the Sampling Distribution of \hat{p}

- 1. The population distribution is *never* normal in shape. Why?
- 2. The sampling distribution is "sufficiently large" if both $n\hat{p} \ge 15$ and $n(1-\hat{p}) \ge 15$. We can explore why this is necessary.

Example: A researcher obtains 100 seeds from a distributor. She plants those seeds and finds that 70 out of the 100 seeds germinate. She wants to estimate the probability that a seed obtained form this distributor will germinate using a confidence interval. Is the sample size large enough? What if she obtained 10 seeds and observed that 7 out of 10 germinated?

Shape of the Sampling Distribution of \bar{x}

- 1. The population distribution might be approximately normal in shape.
- 2. The sampling distribution will be approximately normal if n is large enough.

Example: Here is a sample of n = 272 observations of the eruption duration of Old Faithful. Would we conclude that the *population distribution* is approximately normal? Would we conclude that the *sampling distribution* is approximately normal? Why or why not?

