Wednesday, Sep 18

In this lecture I will demonstrate how to implement some of the methods we have discussed using the **survey** package for R. To try this yourself you will need to install R. It is highly recommended that you use the RStudio integrated development environment (IDE) when using R. Note that both of these are free and available for a variety of operating systems.

Set-Up

We will be using the **survey** package and a data set included with the **SDaA** package. You can install these packages using the **install.packages** command.

```
install.packages("survey")
install.packages("SDaA")
```

Note that install.packages only needs to be done once on a given installation of R. To access the contents of these packages we need to use the library command each time we start a R session.

```
library(survey)
library(SDaA)
```

We will use the data set otters from the **SDaA** package for a few demonstrations. We can see the first few rows of this data set using head.

```
head(otters)
```

	section	habitat	holts	habtype	N	agricultural	W	srswghts	stratwghts
1	1	4	6	notpeat	47	no	2.238095	2.890244	2.238095
2	3	2	0	agricultural	61	yes	3.050000	2.890244	3.050000
3	4	1	8	cliffs	89	no	4.684211	2.890244	4.684211
4	8	1	0	cliffs	89	no	4.684211	2.890244	4.684211
5	11	1	0	cliffs	89	no	4.684211	2.890244	4.684211
6	19	2	0	${\tt agricultural}$	61	yes	3.050000	2.890244	3.050000

These data were collected using stratified random sampling, where the strata are four habitat types (cliff, agricultural, peat, and non-peat). The elements are 5 km by 110 m sections along the coast. The target variable is the number of holts (otter dens).

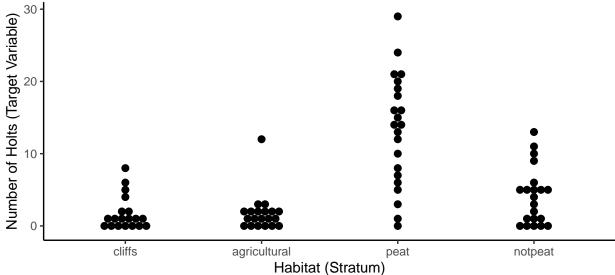
The next step is optional, but useful for keeping track of the strata. Here I change a new variable habtype from habitat with more clear labels.

```
otters$habtype <- factor(otters$habitat, levels = 1:4,
  labels = c("cliffs", "agricultural", "peat", "notpeat"))
head(otters)</pre>
```

	section	habitat	holts	habtype	N	agricultural	W	srswghts	stratwghts
1	1	4	6	notpeat	47	no	2.238095	2.890244	2.238095
2	3	2	0	agricultural	61	yes	3.050000	2.890244	3.050000
3	4	1	8	cliffs	89	no	4.684211	2.890244	4.684211
4	8	1	0	cliffs	89	no	4.684211	2.890244	4.684211
5	11	1	0	cliffs	89	no	4.684211	2.890244	4.684211
6	19	2	0	agricultural	61	ves	3.050000	2.890244	3.050000

Another optional step, but it might be nice to visualize the data using the **ggplot2** package.

```
library(ggplot2) # install this package with install.packages("ggplot2")
p <- ggplot(otters, aes(x = habtype, y = holts)) + theme_classic() +
    geom_dotplot(binaxis = "y", stackdir = "center") +
    labs(x = "Habitat (Stratum)", y = "Number of Holts (Target Variable)")
plot(p)</pre>
```



And yet another optional step would be to compute some basic descriptive statistics using the dplyr package.

```
library(dplyr) # install this package with install.packages("dplyr")
otters %>% group_by(habtype) %>% summarize(mean = mean(holts), sd = sd(holts), n = n())
```

```
# A tibble: 4 x 4
 habtype
                         sd
                mean
                                n
  <fct>
               <dbl> <dbl> <int>
                       2.33
1 cliffs
                 1.74
                               19
2 agricultural
               1.75
                       2.61
                               20
               13.3
                       7.67
                               22
3 peat
4 notpeat
                4.10 3.95
```

This computes the sample mean (\bar{y}_j) , sample standard deviation (s_j) , and sample size (n_j) for each sample from each stratum.

Simple Random Sampling

The otters data were collected using a *stratified* random sampling design, but for this example we will (incorrectly) assume that the data were collected using *simple* random sampling. Note that data do not know how they were collected. It is the responsibility of the survey researcher to correctly communicate the design to the software.

The first step is to specify the *sampling design*. But before we do that we need to add more information to the data set. Namely we need to specify the *population size* (which is 237 sections). This is done by creating a new variable.

```
otters$N <- 237
head(otters)
```

```
section habitat holts habtype N agricultural w srswghts stratwghts 1 1 4 6 notpeat 237 no 2.238095 2.890244 2.238095
```

2	3	2	0 agricultural	237	yes 3.050000 2.890244 3.05000)0
3	4	1	8 cliffs	237	no 4.684211 2.890244 4.68421	١1
4	8	1	0 cliffs	237	no 4.684211 2.890244 4.68421	١1
5	11	1	0 cliffs	237	no 4.684211 2.890244 4.68421	١1
6	19	2	0 agricultural	237	yes 3.050000 2.890244 3.05000	0

Now the design can be specified using the svydesign function.

```
ottersrs <- svydesign(id = ~1, data = otters, fpc = ~N)
```

The id = ~1 is used to indicate a variable that identifies the *sampling unit* for cluster sampling designs (more on that later), but for element sampling we specify it as above. The data argument is the data frame containing sample data, and the fpc argument is used to indicate the variable that holds the population size(s). The object ottersrs now contains information necessary for any inference calculations assuming a simple random sampling design.

Recall that an estimator of μ for simple random sampling is the sample mean,

$$\bar{y} = \frac{1}{n} \sum_{i \in \mathcal{S}} y_i.$$

We can compute the estimate from this estimator using the svymean function.

```
svymean(~holts, design = ottersrs)
```

mean SE holts 5.439 0.6031

The SE is the (estimated) *standard error*, which is simply the standard deviation of the estimator and thus the square root of the variance of the estimator. The (estimated) variance is computed as

$$\widehat{V}(\bar{y}) = \left(1 - \frac{n}{N}\right) \frac{s^2}{n},$$

where s^2 is the variance of the observations in the sample, defined as

$$s^2 = \frac{1}{n-1} \sum_{i \in \mathcal{S}} (y_i - \bar{y})^2.$$

It is being used here as an estimate of σ^2 . We have defined the bound on the error of estimation for \bar{y} as (approximately) $B = 2\sqrt{V(\bar{y})}$. So we could obtain the (estimated) bound on the error of estimation by simply doubling the standard error reported by svymean. The confidence interval for μ is $\bar{y} \pm B$. We can compute this by passing the result of svymean to the confint function.

```
confint(svymean(~holts, design = ottersrs))
```

2.5 % 97.5 % holts 4.256935 6.621114

The confint function does not necessarily define the bound on the error of estimation as exactly twice the standard error as it tries to use a multiplier to come closer to a 95% confidence level, but in practice it'll usually be close to two. You can also change the confidence level to a different value (e.g., 99%).

0.5 % 99.5 % holts 3.885496 6.992553

 $^{^{1}}$ The 'survey' package will try to compute a more accurate multiplier using a t distribution.

Recall that an estimator of τ under simple random sampling is

$$\hat{\tau} = \frac{N}{n} \sum_{i \in \mathcal{S}} y_i = N\bar{y},$$

and the (estimated) variance of $\hat{\tau}$ is

$$\widehat{V}(\widehat{\tau}) = N^2 \left(1 - \frac{n}{N} \right) \frac{s^2}{n}.$$

We can use the svytotal function for inferences about τ based on this estimator.

```
svytotal(~holts, design = ottersrs)
total SE
```

confint(svytotal(~holts, design = ottersrs))

2.5 % 97.5 % holts 1008.894 1569.204

1289 142.94

holts

Domain Estimation

To estimate domain means or totals, we can use the svyby function.

```
svyby(~holts, by = ~habtype, design = ottersrs, FUN = svymean)
```

```
habtype holts se
cliffs cliffs 1.736842 0.4232673
agricultural agricultural 1.750000 0.4634253
peat peat 13.272727 1.2994362
notpeat notpeat 4.095238 0.6841975
```

habtype holts se cliffs cliffs 95.37805 27.99661 agricultural agricultural 101.15854 31.20485 peat peat 843.95122 150.03694 notpeat notpeat 248.56098 56.33427

Recall that we discussed two ways to estimate a domain total $(\hat{\tau}_d)$ in the context of stratified random sampling, depending on whether or not we know the size of the domain (i.e., N_d). Here svyby is using the estimator that does not require knowing the domain size, which is

$$\hat{\tau}_d = \frac{N}{n} n_d \bar{y}_d.$$

If we did know the domain size we could estimate the domain total with the other estimator, which is

$$\hat{\tau}_d = N_d \bar{y}_d.$$

A way to use this estimator is via post-stratification (see below). Confidence intervals for domain means or totals can be obtained by using confint.

```
confint(svyby(~holts, by = ~habtype, design = ottersrs, FUN = svytotal))
```

```
2.5 % 97.5 % cliffs 40.50571 150.2504 agricultural 39.99815 162.3189 peat 549.88422 1138.0182 notpeat 138.14783 358.9741
```

Categorical Target Variable

Now suppose instead that target variable was the *habitat type* rather than the number of holts. We can estimate the *proportion* of each habitat type as follows.

```
svymean(~habtype, design = ottersrs)
```

```
        mean
        SE

        habtypecliffs
        0.23171
        0.0379

        habtypeagricultural
        0.24390
        0.0386

        habtypepeat
        0.26829
        0.0398

        habtypenotpeat
        0.25610
        0.0392
```

We can also estimate the *number* of sections of each habitat type as follows.

```
svytotal(~habtype, design = ottersrs)
```

```
total SE
habtypecliffs 54.915 8.9853
habtypeagricultural 57.805 9.1452
habtypepeat 63.585 9.4356
habtypenotpeat 60.695 9.2952
```

Of course this would only be necessary if the researchers did not know how many sections there were of each type.

Stratified Random Sampling

As mentioned earlier, the otters data were collected using a *stratified sampling design*, not simple random sampling. Here we will see how to specify this design and make inferences assuming a stratified sampling design.

For stratified random sampling we need to specify the size of each stratum.

```
otters$N[otters$habtype == "cliffs"] <- 89
otters$N[otters$habtype == "agricultural"] <- 61
otters$N[otters$habtype == "peat"] <- 40
otters$N[otters$habtype == "notpeat"] <- 47
head(otters)</pre>
```

```
section habitat holts
                             habtype N agricultural
                                                             w srswghts stratughts
                                                                          2.238095
1
        1
                4
                             notpeat 47
                                                  no 2.238095 2.890244
2
        3
                2
                      0 agricultural 61
                                                 yes 3.050000 2.890244
                                                                          3.050000
3
        4
                1
                      8
                              cliffs 89
                                                  no 4.684211 2.890244
                                                                          4.684211
4
       8
                1
                      0
                              cliffs 89
                                                  no 4.684211 2.890244
                                                                          4.684211
5
                              cliffs 89
                1
                      0
                                                  no 4.684211 2.890244
                                                                          4.684211
       11
6
       19
                      0 agricultural 61
                                                 yes 3.050000 2.890244
                                                                          3.050000
```

Another way you can do this is with the case_when function from the dplyr package.

```
otters <- otters %% mutate(N = case_when(
  habtype == "cliffs" ~ 89,
  habtype == "agricultural" ~ 61,
  habtype == "peat" ~ 40,
  habtype == "notpeat" ~ 47))
head(otters)</pre>
```

```
      section habitat holts
      habtype
      N agricultural
      w srswghts
      stratwghts

      1
      1
      4
      6
      notpeat 47
      no 2.238095
      2.890244
      2.238095

      2
      3
      2
      0 agricultural 61
      yes 3.050000
      2.890244
      3.050000
```

3	4	1	8	cliffs	89	no 4.684211 2.890244 4.684211
4	8	1	0	cliffs	89	no 4.684211 2.890244 4.684211
5	11	1	0	cliffs	89	no 4.684211 2.890244 4.684211
6	19	2	0 a	gricultural	61	yes 3.050000 2.890244 3.050000

Now we can specify the design using svydesign.

```
otterstrat <- svydesign(id = ~1, strata = ~habtype, fpc = ~N, data = otters)
```

Inferences can be obtained using the same commands as earlier, although note that the results are not the same because the assumed design is different. Recall that an estimator of μ under stratified random sampling is

$$\hat{\mu} = \frac{N_1}{N} \bar{y}_1 + \frac{N_2}{N} \bar{y}_2 + \dots + \frac{N_L}{N} \bar{y}_L = \sum_{i=1}^L \frac{N_j}{N} \bar{y}_j,$$

which has an estimated variance of

$$\widehat{V}(\widehat{\mu}) = \frac{1}{N^2} \sum_{j=1}^{L} N_j^2 \left(1 - \frac{n_j}{N_j} \right) \frac{s_j^2}{n_j}.$$

These formulas are used to obtain the following (recall that the standard error is the square root of the variance).

svymean(~holts, design = otterstrat)

mean SE holts 4.1549 0.3119

An estimator of τ under stratified random sampling is

$$\hat{\tau} = N_1 \bar{y}_1 + N_2 \bar{y}_2 + \dots + N_L \bar{y}_L = \sum_{i=1}^L N_j \bar{y}_j,$$

which has an estimated variance of

$$\hat{V}(\hat{\tau}) = \sum_{j=1}^{L} N_j^2 \left(1 - \frac{n_j}{N_j} \right) \frac{s_j^2}{n_j}.$$

These formulas are used to obtain the following.

svytotal(~holts, design = otterstrat)

total SE holts 984.71 73.921

Confidence intervals can be obtained in the same way as before.

confint(svytotal(~holts, design = otterstrat))

2.5 % 97.5 % holts 839.8317 1129.597

The optional argument deff = TRUE will estimate the design effect for the stratified sampling design.

svytotal(~holts, design = otterstrat, deff = TRUE)

total SE DEff holts 984.714 73.921 0.3572 The total sample size is n = 82. So the effective sample size of this design is estimated to be $82/0.3572 \approx 230$. Estimates of domain means and totals can be obtained as follows.

```
svyby(~holts, by = ~habtype, design = otterstrat, FUN = svymean)
                  habtype
                              holts
                   cliffs 1.736842 0.4739725
agricultural agricultural 1.750000 0.4790589
                     peat 13.272727 1.0964954
peat
notpeat
                  notpeat 4.095238 0.6408521
svyby(~holts, by = ~habtype, design = otterstrat, FUN = svytotal)
                  habtype
                             holts
                   cliffs 154.5789 42.18355
agricultural agricultural 106.7500 29.22259
peat
                     peat 530.9091 43.85982
                  notpeat 192.4762 30.12005
notpeat
```

The estimator of μ_d is the same for simple random sampling and stratified random sampling (i.e., \bar{y}_d), but the standard errors are not because the design is different. Also here the estimator being used for τ_d is the estimator that uses a known N_d , since the domains are the strata and the strata sizes are provided. The formulas for the (estimated) variances of the domain estimators are the same as those for simple random sampling applied to each sample.

Further Inferences Concerning Strata

The above shows how to make inferences concerning individual strata parameters. We can also consider (a) how to make inferences about two or more strata *combined* and also (b) how to make inferences about *differences* between strata parameters.

Suppose we wanted to make inferences about the total number of holts in non-agricultural sections (i.e., cliffs, peat, or not peat). There are a couple of ways this can be done. One is to use the **subset** function which communicates that we only want to make inferences about a particular sub-population.

```
notagg <- subset(otterstrat, habtype %in% c("cliffs", "peat", "notpeat"))
svytotal(~holts, design = notagg)

total SE
holts 877.96 67.9</pre>
```

If there was a variable in the original data that identifies the non-agricultural sections we can use that instead.

```
otters <- otters %>%
  mutate(agricultural = ifelse(habtype %in% c("cliffs", "peat", "notpeat"), "no", "yes"))
head(otters)
```

```
section habitat holts
                             habtype N agricultural
                                                              w srswghts stratwghts
                                                   no 2.238095 2.890244
                                                                           2.238095
1
                4
                             notpeat 47
        1
                      0 agricultural 61
                                                  yes 3.050000 2.890244
        3
                2
                                                                           3.050000
2
                                                   no 4.684211 2.890244
3
        4
                               cliffs 89
                1
                      8
                                                                           4.684211
4
        8
                1
                      0
                               cliffs 89
                                                   no 4.684211 2.890244
                                                                           4.684211
5
                1
                      0
                               cliffs 89
                                                   no 4.684211 2.890244
                                                                           4.684211
       11
                                                                           3.050000
                      0 agricultural 61
                                                  yes 3.050000 2.890244
otterstrat <- svydesign(id = ~1, strata = ~habtype, fpc = ~N, data = otters)
svyby(~holts, by = ~agricultural, design = otterstrat, FUN = svytotal)
```

```
agricultural holts se
```

```
no no 877.9642 67.89958
yes yes 106.7500 29.22259
```

This approach also works for simple random sampling.

```
notagg <- subset(ottersrs, habtype %in% c("cliffs", "peat", "notpeat"))
svytotal(~holts, design = notagg)</pre>
```

```
total SE holts 1187.9 146.28
```

The estimate is different here because svytotal is using the estimator that does not use the (in this case known) size of the domain. But you can use the estimator that does know the size of the domain if you use post-stratification (as shown below).

Here is another approach using the svycontrast function which is quite general because it allows us to specify many different kinds of functions of stratum or domain means or totals. Here I will show how we can estimate the difference in the stratum means between the peat and non-peat strata.

```
tmp <- svyby(~holts, by = ~habtype, design = otterstrat, FUN = svymean)
tmp
                  habtype
                              holts
cliffs
                   cliffs 1.736842 0.4739725
agricultural agricultural 1.750000 0.4790589
peat
                     peat 13.272727 1.0964954
notpeat
                  notpeat 4.095238 0.6408521
svycontrast(tmp, quote(peat - notpeat))
          nlcon
contrast 9.1775 1.27
confint(svycontrast(tmp, quote(peat - notpeat)))
            2.5 %
                    97.5 %
contrast 6.688263 11.66672
```

Post-Stratification

Now assume that the sampling design was simple random sampling, but that we want to post-stratify based on the habitat auxiliary variable because we know how many sections are within each habitat. To do this we first need to create another data set that holds the known sizes of the strata.

```
habitatfreq <- data.frame(habtype = c("cliffs", "agricultural", "peat", "notpeat"),
   Freq = c(89,61,40,47))
habitatfreq</pre>
```

```
habtype Freq
1 cliffs 89
2 agricultural 61
3 peat 40
4 notpeat 47
```

This information can then be passed to the postStratify function which will effectively re-weight the observations.

```
otterpost <- postStratify(design = ottersrs, strata = ~habtype, population = habitatfreq)</pre>
```

Now we can estimate μ and τ as well as the domain means and totals.

```
svymean(~holts, design = otterpost)
        mean
                 SE
holts 4.1549 0.3256
svytotal(~holts, design = otterpost)
       total
                 SE
holts 984.71 77.162
svyby(~holts, by = ~habtype, design = otterpost, FUN = svymean)
                  habtype
                              holts
cliffs
                   cliffs 1.736842 0.4232673
agricultural agricultural 1.750000 0.4634253
peat
                     peat 13.272727 1.2994362
notpeat
                  notpeat 4.095238 0.6841975
svyby(~holts, by = ~habtype, design = otterpost, FUN = svytotal)
                  habtype
                             holts
cliffs
                   cliffs 154.5789 37.67079
agricultural agricultural 106.7500 28.26895
                     peat 530.9091 51.97745
peat
notpeat
                  notpeat 192.4762 32.15728
```

Note that the mean and total *estimates* are the same as those from stratified random sampling, but the standard errors are not. This is because the variances for estimators are not computed the same under post-stratification as they are under stratified random sampling. Note also that after post-stratification the estimator for a domain *total* uses the estimator that uses the known domain size. This also happens below where we estimate the number of holts in non-agricultural sections.

```
notagg <- subset(otterpost, habtype %in% c("cliffs", "peat", "notpeat"))
svytotal(~holts, design = notagg)

total SE</pre>
```

Note that the estimate is the same as when the design was specified as stratified random sampling, but the standard error is not.

Sampling Weights

holts 877.96 71.797

We can compute sampling weights using the weights function. For simple random sampling we know that all elements have a weight of N/n.

```
otters$w <- weights(ottersrs)
head(otters)</pre>
```

```
section habitat holts
                              habtype N agricultural
                                                               w srswghts stratwghts
                       6
                                                    no 2.890244 2.890244
                                                                             2.238095
1
        1
                4
                              notpeat 47
                       0 agricultural 61
                                                   yes 2.890244 2.890244
2
        3
                2
                                                                             3.050000
3
        4
                       8
                               cliffs 89
                                                    no 2.890244 2.890244
                                                                             4.684211
                1
4
        8
                1
                       0
                               cliffs 89
                                                    no 2.890244 2.890244
                                                                             4.684211
5
       11
                1
                       0
                               cliffs 89
                                                    no 2.890244 2.890244
                                                                             4.684211
                2
                       0 agricultural 61
                                                   yes 2.890244 2.890244
                                                                             3.050000
6
```

Remember that we changed the variable N earlier for the stratified random sampling design. For the weights for simple random sampling N = 237 and n = 82. For stratified random sampling an element has a weight of

 N_j/n_j if it is form the j-th stratum.

```
otters$w <- weights(otterstrat)
head(otters)</pre>
```

	section	${\tt habitat}$	holts	habtype	N	agricultural	W	srswghts	stratwghts
1	1	4	6	notpeat	47	no	2.238095	2.890244	2.238095
2	3	2	0	agricultural	61	yes	3.050000	2.890244	3.050000
3	4	1	8	cliffs	89	no	4.684211	2.890244	4.684211
4	8	1	0	cliffs	89	no	4.684211	2.890244	4.684211
5	11	1	0	cliffs	89	no	4.684211	2.890244	4.684211
6	19	2	0	agricultural	61	yes	3.050000	2.890244	3.050000

When we use post-stratification we change the weights to match those for stratified random sampling.

```
otters$w <- weights(otterpost)
head(otters)</pre>
```

	${\tt section}$	${\tt habitat}$	holts	habtype	N	agricultural	W	srswghts	stratwghts
1	1	4	6	notpeat	47	no	2.238095	2.890244	2.238095
2	3	2	0	agricultural	61	yes	3.050000	2.890244	3.050000
3	4	1	8	cliffs	89	no	4.684211	2.890244	4.684211
4	8	1	0	cliffs	89	no	4.684211	2.890244	4.684211
5	11	1	0	cliffs	89	no	4.684211	2.890244	4.684211
6	19	2	0	agricultural	61	yes	3.050000	2.890244	3.050000

A property of sampling weights (if they have not been modified) is that they sum to the number of elements in the population (for simple random sampling) and to the number of elements in each stratum (for stratified random sampling).

There are useful ways that weights can be used that we will discuss later in the course.

Double Sampling (Two-Phase Sampling)

40

47

3 peat

4 notpeat

I am going to use another data set to demonstrate double sampling for strata with unknown sizes. The data are in a the **trtools** package which can be installed using the following command, provided you have already installed the **devtools** package (which can be installed using install.packages(devtools)).

```
devtools::install_github("trobinj/trtools")
```

The data set is called **ismail**. The elements are veterans. They were evaluated quickly in the first phase to classify them as disabled or not. Those veterans sampled in the second phase where then assessed by

psychiatrists to determine whether or not they had alcohol, sleep, or psychiatric disorders.

```
library(trtools)
ismail$N <- 53462
head(ismail, 20)</pre>
```

```
disabled alcohol sleep psych
1
          no
                 <NA>
                        <NA>
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19
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                              <NA> 53462
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20
                 <NA>
                        <NA>
                              <NA> 53462
          no
```

The variable disabled is the stratification variable. The target variables (all categorical) are alcohol, sleep, and psych. The missing values (the <NA>) are due to the double sampling. First we specify a two-phase sampling design using twophase. Note that many of the arguments have two parts, one for each phase.

```
ismail2phase <- twophase(id = list(~1, ~1), strata = list(NULL, ~disabled),
  fpc = list(~N, NULL), subset = ~!is.na(sleep), data = ismail)</pre>
```

Inferences can then be obtained the usual way. Note that here because sleep is categorical, totals are the estimated *number* of veterans in the population with sleep disorders, and the means are the estimated *proportions* of veterans in the population with sleep disorders.